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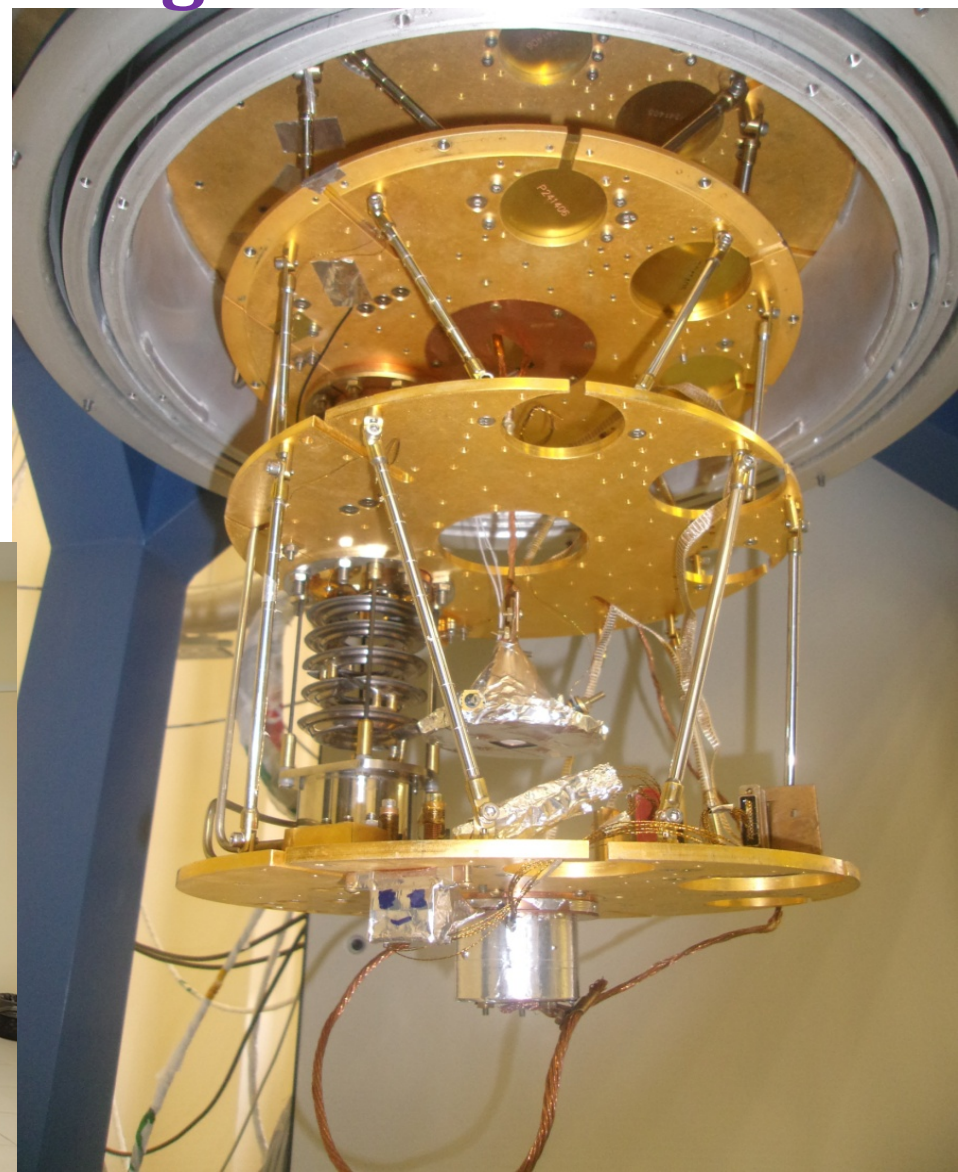


**НИЖЕГОРОДСКИЙ ГОСУДАРСТВЕННЫЙ
УНИВЕРСИТЕТ им. Н.И. ЛОБАЧЕВСКОГО**
Национальный исследовательский университет

Noise-induced transitions in nonlinear systems

Andrey L. Pankratov

Laboratory of Superconducting Nanoelectronics



Triton 200: Heating of **BB** source, attached to 4 K plate, up to **58 K** at stabilized low plate temperature of **0.3K**

Obituary of L. S. Kuzmin, JLTP

L.S. Kuzmin's academic career began at the Department of Physics at the Moscow State University in 1964. He did his both undergraduate and doctoral studies under supervision by Professor Konstantin Likharev. He defended his PhD thesis in 1977, with the title “Nondegenerate single-frequency parametric amplification using Josephson junctions with selfpumping” and presented his post-doctoral research in 1997 on “Correlated Tunneling of Electrons and Cooper Pairs in Ultrasmall Tunnel Junctions”. During late 1980's, Leonid gradually moved to Chalmers University of Technology. The first visit took place during a Gothenburg winter in 1989, and eventually continued all the way to a professorship at Chalmers in 2004.

During 1983, Likharev's group has initiated investigations of the tunneling processes in small Josephson tunnel junctions. Leonid was devoted to the study and, together with K.K. Likharev, discovered the discrete correlated single-electron tunneling in a double junction structure published in JETP Lett. vol. 45, pp. 389-390, 1987. This effect was simultaneously observed at Bell Labs, by T. Fulton and G. Dolan and their manuscript was submitted for publication just on the same day, March 6, 1987. Later, detection of the so-called Bloch oscillations in arrays of Josephson junctions was a discovery that had a major impact.

<https://link.springer.com/article/10.1007/s10909-022-02923-5>

L. S. Kuzmin, and K. K. Likharev,
Direct experimental-observation of discrete correlated single-electron tunneling
[JETP Letters](#), 45, 8, 495-497 (1987).

L. S. Kuzmin, P. Delsing, T. Claeson, and K. K. Likharev,
Single-electron charging effects in one-dimensional arrays of ultrasmall tunnel junctions,
[Phys. Rev. Lett.](#) 62, 2539 (1989).

P. Delsing, K. K. Likharev, **L. S. Kuzmin**, and T. Claeson,
Effect of high-frequency electrodynamic environment on the single-electron tunneling in
ultrasmall junctions
[Phys. Rev. Lett.](#) 63, 1180 (1989).

P. Delsing, K. K. Likharev, **L. S. Kuzmin**, and T. Claeson,
Time-correlated single-electron tunneling in one-dimensional arrays of ultrasmall tunnel
junctions,
[Phys. Rev. Lett.](#) 63, 1861 (1989).

L. S. Kuzmin and D. B. Haviland,
Observation of the Bloch oscillations in an ultrasmall Josephson junction
[Phys. Rev. Lett.](#) 67, 2890 (1991).

Professor **Yuri Pashkin**, Lancaster University,
is the most famous former PhD student of Professor **Leonid Kuzmin**

Y. Nakamura, **Yu. A. Pashkin** & J. S. Tsai

Coherent control of macroscopic quantum states in a single-Cooper-pair box

[Nature](#) 398, 786–788 (1999), 13k Accesses, 1944 Citations

New detectors with internal cooling of a nanoabsorber – the Cold-Electron Bolometer

Leonid S.Kuzmin

On the concept of a hot-electron microbolometer with capacitive coupling to the antenna,

[Physica B](#), 284–288, 2129-2130 (2000).

D.S. Golubev, **L.S. Kuzmin**,

Nonequilibrium theory of a hot-electron bolometer with normal metal-insulator-superconductor tunnel junction,

[Journal of Applied Physics](#) 89, 6464 (2001)

Ultimate cold-electron bolometer with strong electrothermal feedback

Leonid Kuzmin

[SPIE Proceedings](#), V. 5498, Millimeter and Submillimeter Detectors for Astronomy II; (2004)

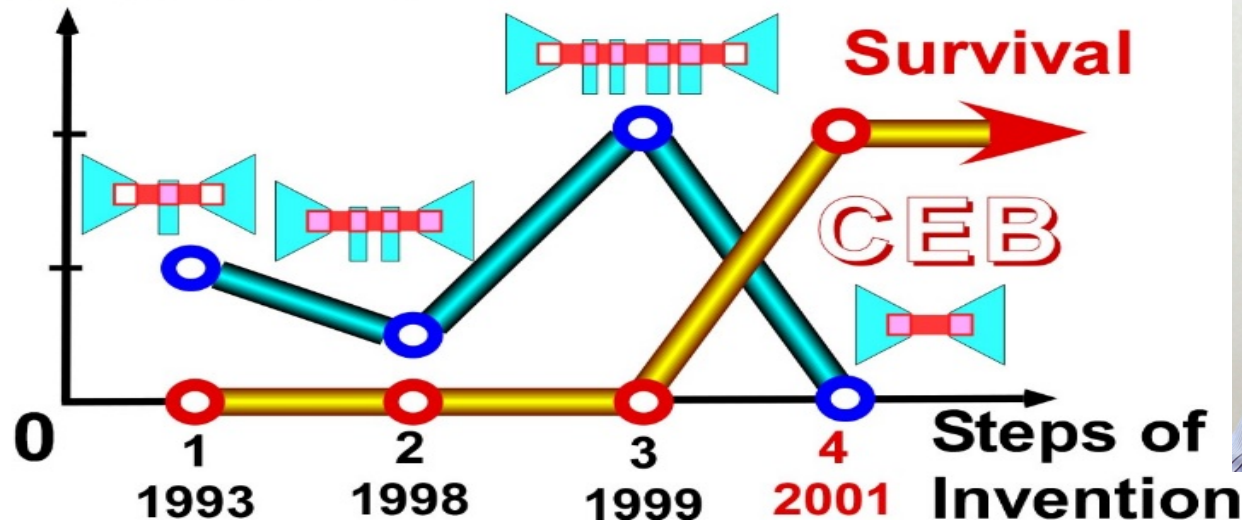
<https://doi.org/10.1117/12.554317>

Comment in **Nature Research Communities** blog [BEHIND THE PAPER](https://astronomycommunity.nature.com/channels/1490-behind-the-paper/posts/53529-story-of-the-invention-of-a-cold-electron-bolometer)
with CEB progress description

«Story of the Invention of a Cold-Electron Bolometer»

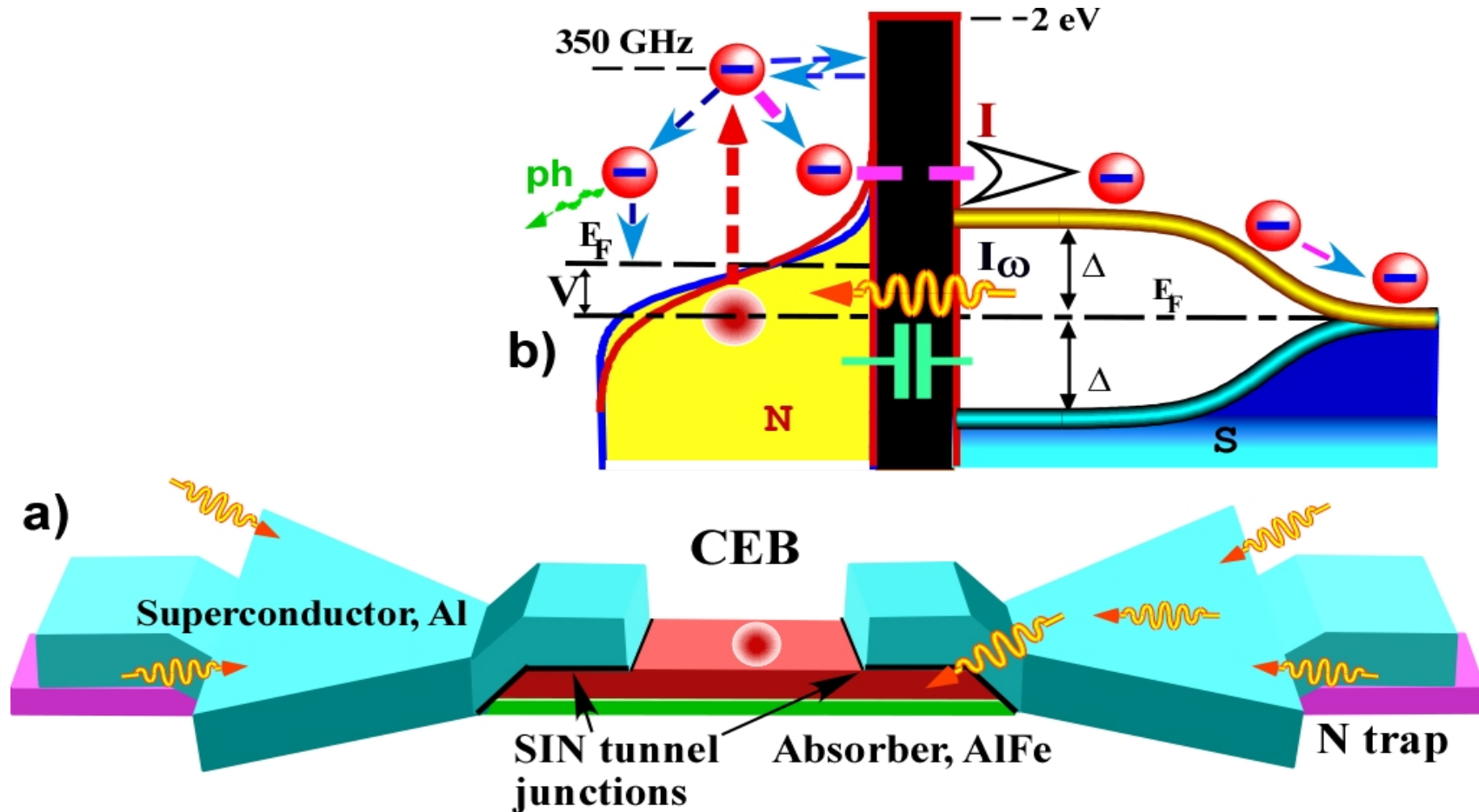
<https://astronomycommunity.nature.com/channels/1490-behind-the-paper/posts/53529-story-of-the-invention-of-a-cold-electron-bolometer>

Complexity & Awkwardness



4. Cold-Electron Bolometer (CEB) with SIN tunnel junctions as the thermometer, electron cooler, RF capacitive coupling and thermal isolation. L. Kuzmin (2002).

Cold-Electron Bolometers for Radio Astronomy



Tunnel SIN junctions perform 4 functions:

- 1) capacitive AC connection,
- 2) thermal isolation,
- 3) thermometry
- 4) electron cooling.

Advantages: background limited; record cosmic rays immunity.



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Photon-noise-limited cold-electron bolometer based on strong electron self-cooling for high-performance cosmology missions

A scanning electron microscope image of the Cold-Electron Bolometer with on-chip self-cooling, integrated into a gold antenna. Credit: Leonid Kuzmin

Announcement

Travel Grant for Early Career Researchers

Early Careers and no funds to attend your dream conference? Applications are now open for grants to support travel in 2020.



Announcement

Dario Bercioux joins our Editorial Board

A warm welcome to our new Editorial Board Member Dario Bercioux. Dario will work with the journal editors in... [show more](#)



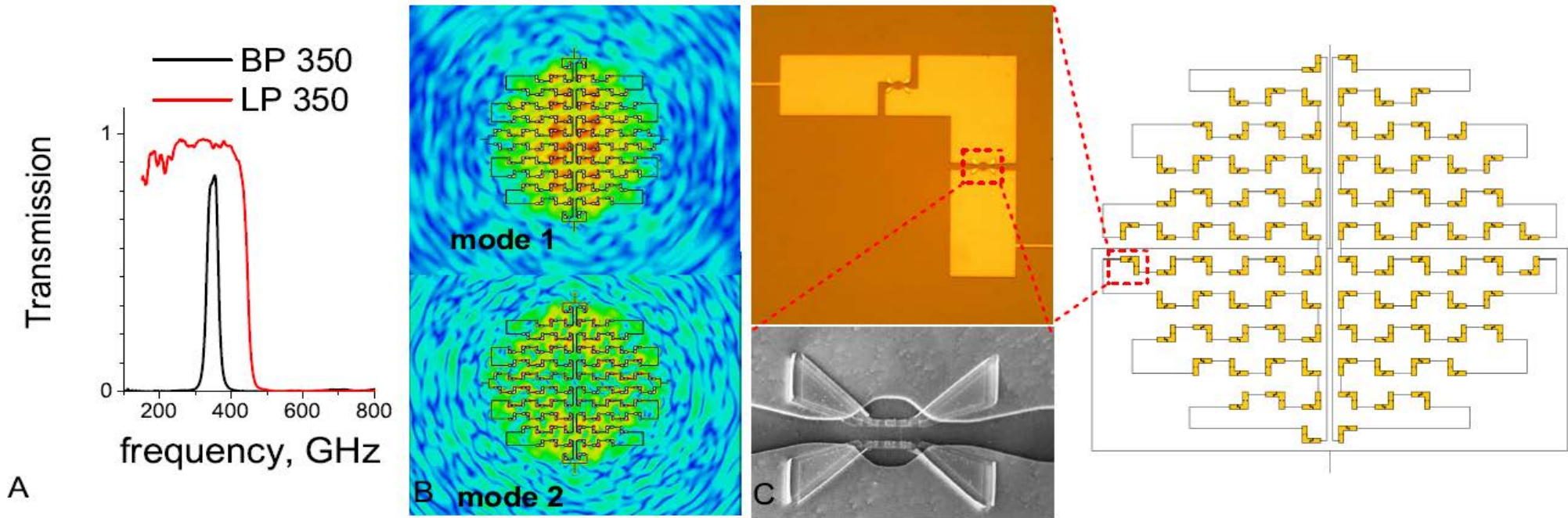
Announcement

Carl Ganter is our reviewer of the month

Carl Ganter provided an exceptionally thorough review, stretching to verify the calculations presented in the paper.

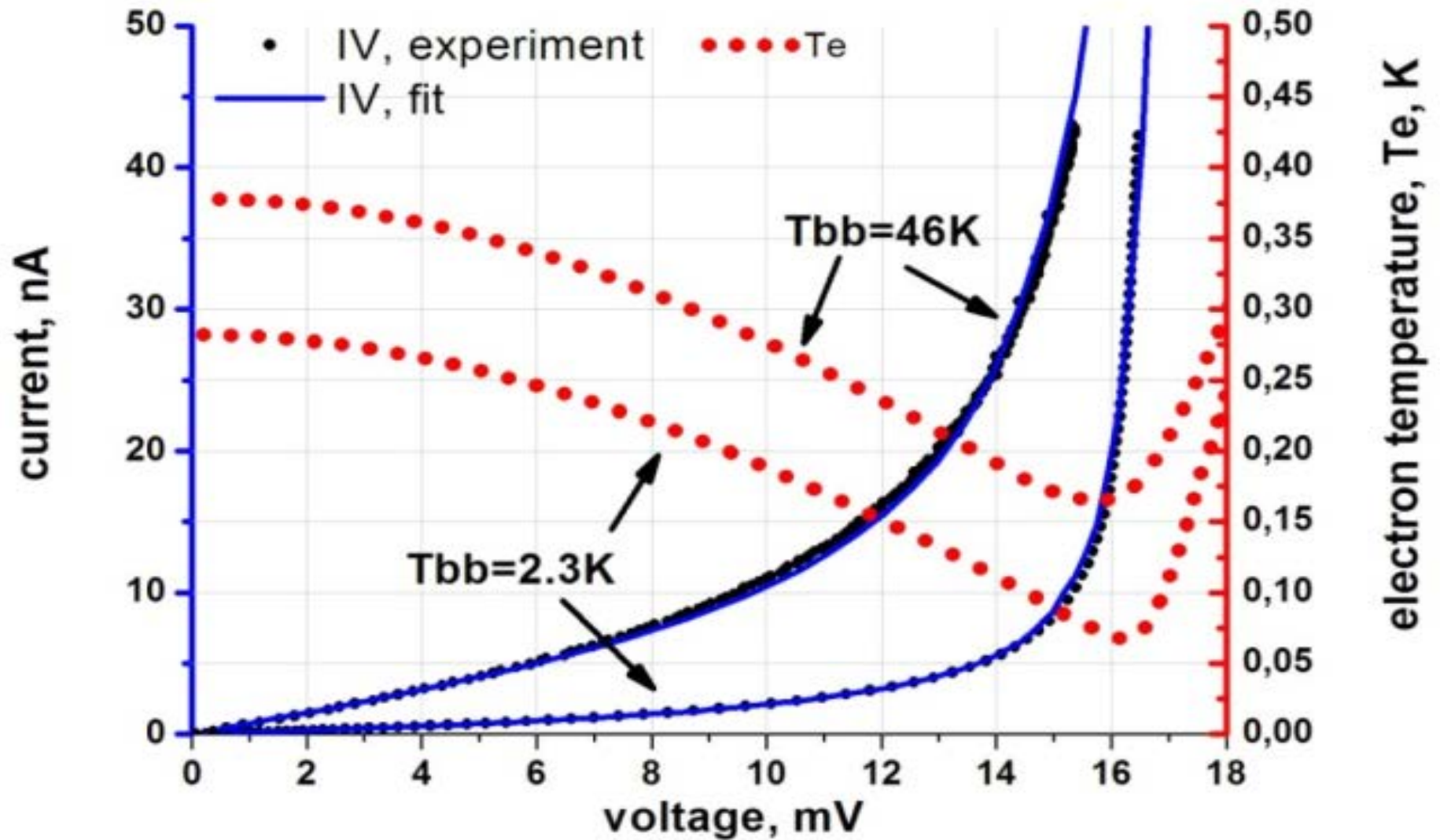


Many antenna – many absorber receiving system for a high power load



L.S. Kuzmin, A.L. Pankratov, A.V. Gordeeva, V.O. Zbrozhek, V.A. Shamporov, L.S. Revin, A.V. Blagodatkin, S. Masi, P. de Bernardis, **Photon-noise-limited cold-electron bolometer based on strong electron self-cooling for high-performance cosmology missions**, **Comm. Phys.**, 2, 104 (2019).

G2 OS7-34
310mK



Current-voltage characteristics of CEB
at various black-body temperatures.

Ultimate sensitivity – background limited operation: photon noise contribution is dominating

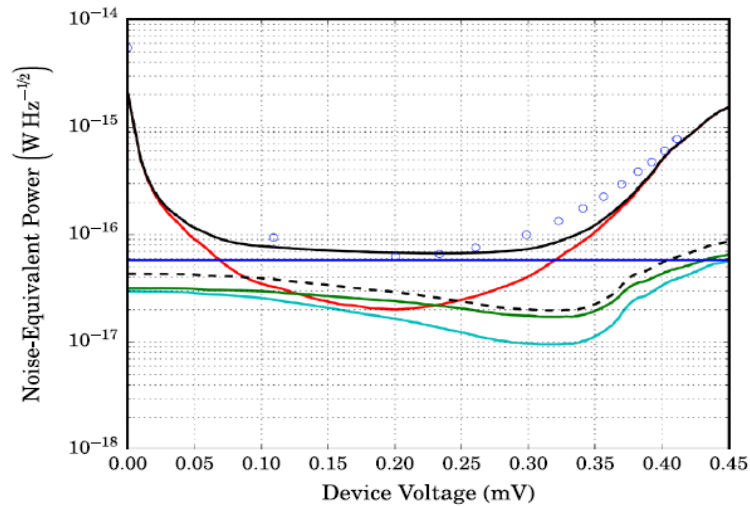
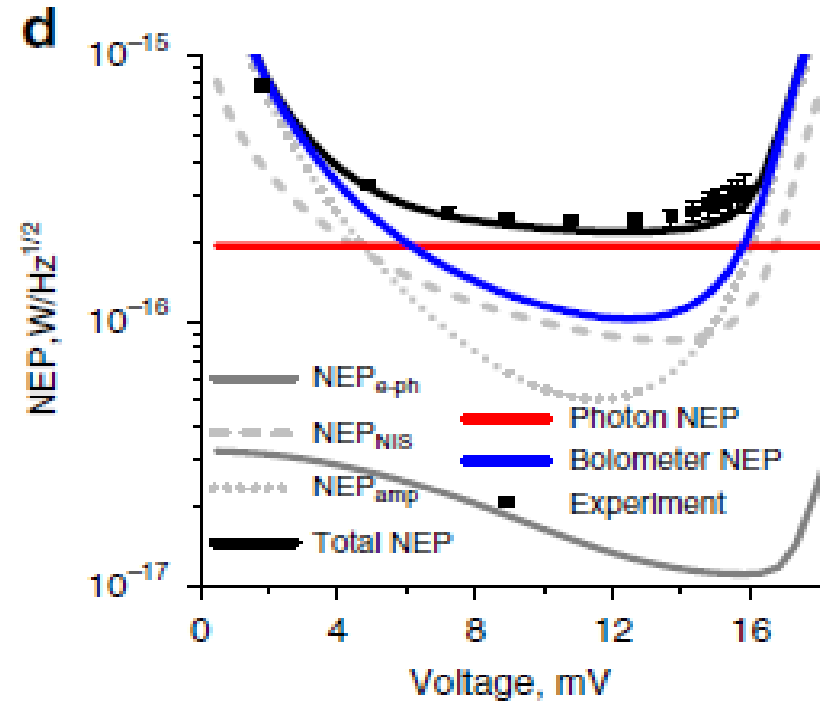


Fig. 4 Example of measured and modelled noise for the strained detector observing a 77-K source. Noise modelled using Eqs. 5 and 6. Lines modelled data, red—amplifier noise, green—tunnelling noise, cyan—e-ph noise, blue—photon noise, dashed black—total device noise (sum of tunnelling and e-ph noise), black—total modelled noise level. Circles measured data. Overall the model and data are in good agreement and show that the device is photon-noise limited from approximately 0.1–0.3 mV (Color figure online)

T.L.R. Brien, P.A.R. Ade, P.S. Barry, C.J. Dunscombe, D.R. Leadley, D.V. Morozov, M. Myronov, E.H.C. Parker, M.J. Prest, M. Prunnila, R.V. Sudiwala, T.E. Whall, P. D. Mauskopf, *J. Low. Temp. Phys.* 184, 231–237 (2016)

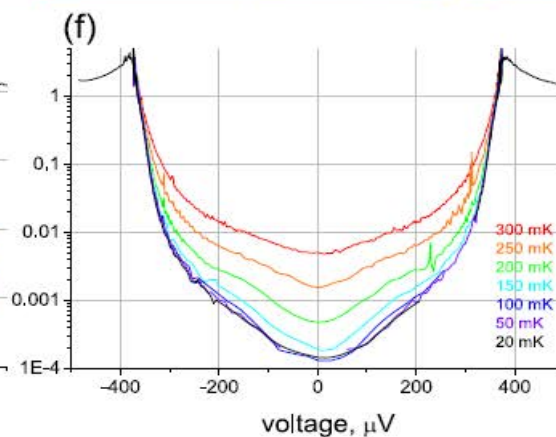
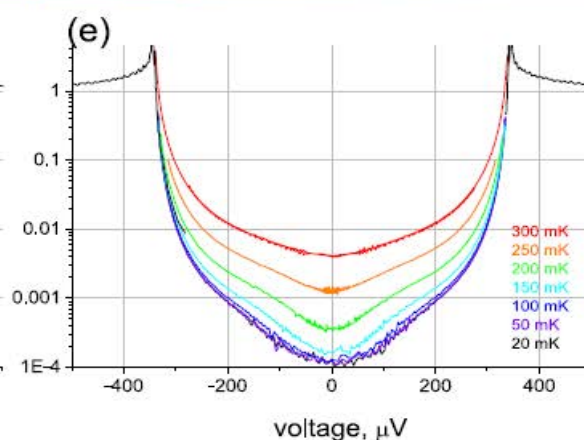
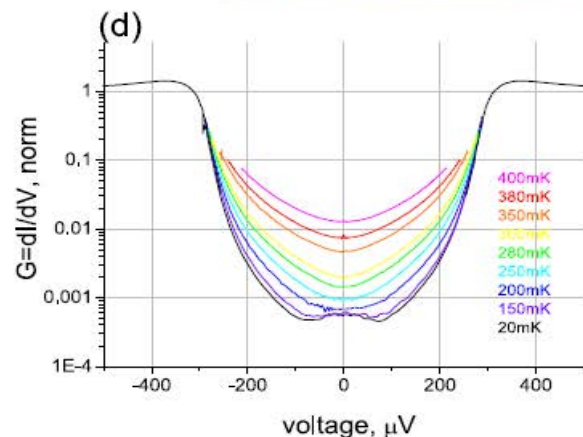
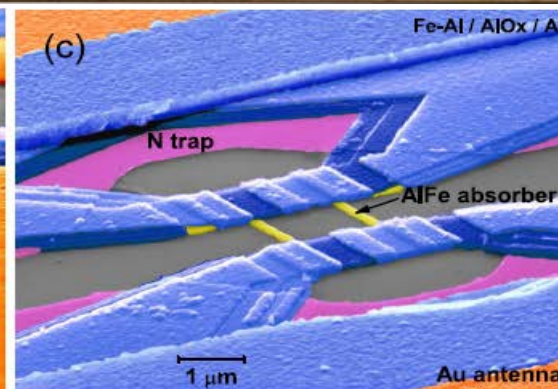
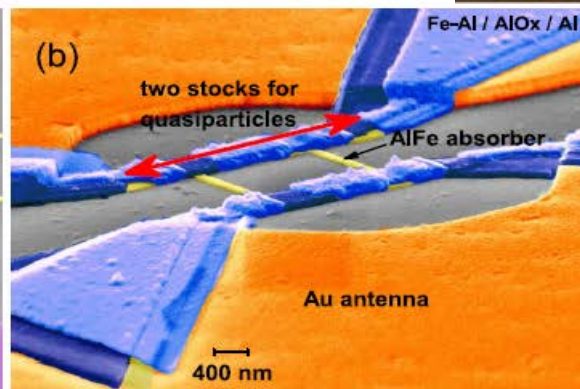
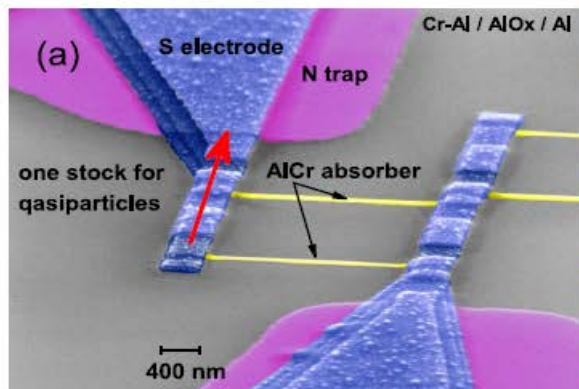
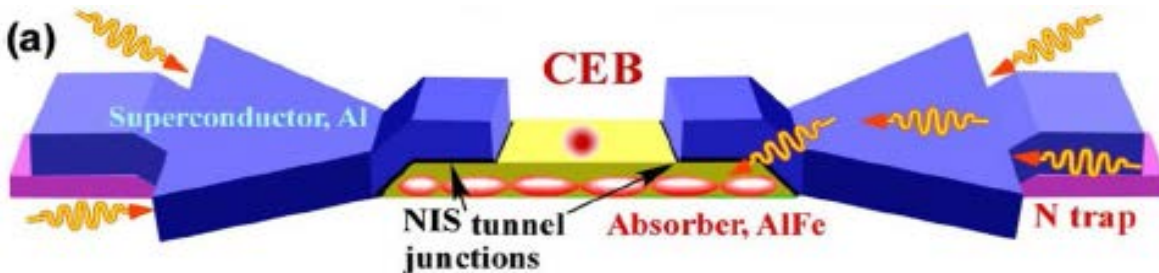
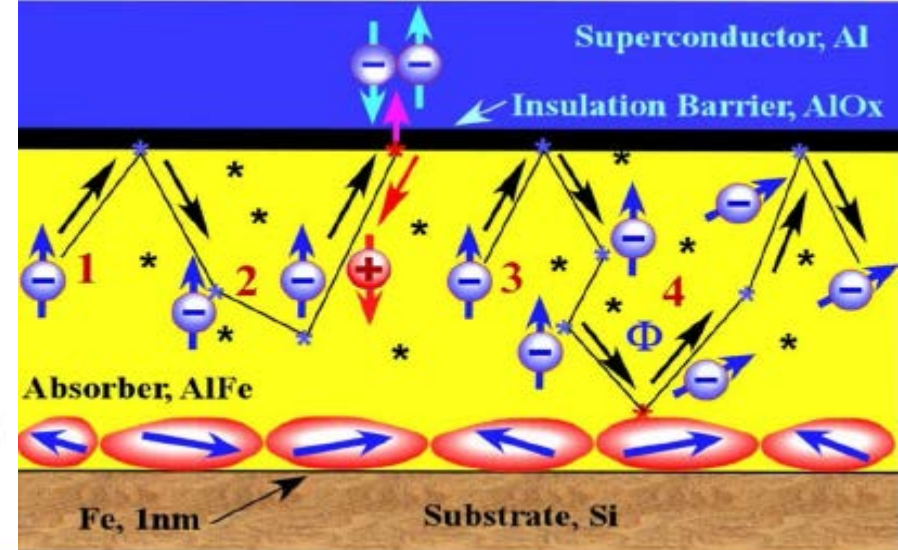


L.S. Kuzmin, A.L. Pankratov, A.V. Gordeeva, V.O. Zbrozhek, V.A. Shamporov, L.S. Revin, A.V. Blagodatkin, S. Masi, P. de Bernardis, *Communications Physics*, 2, 104 (2019).

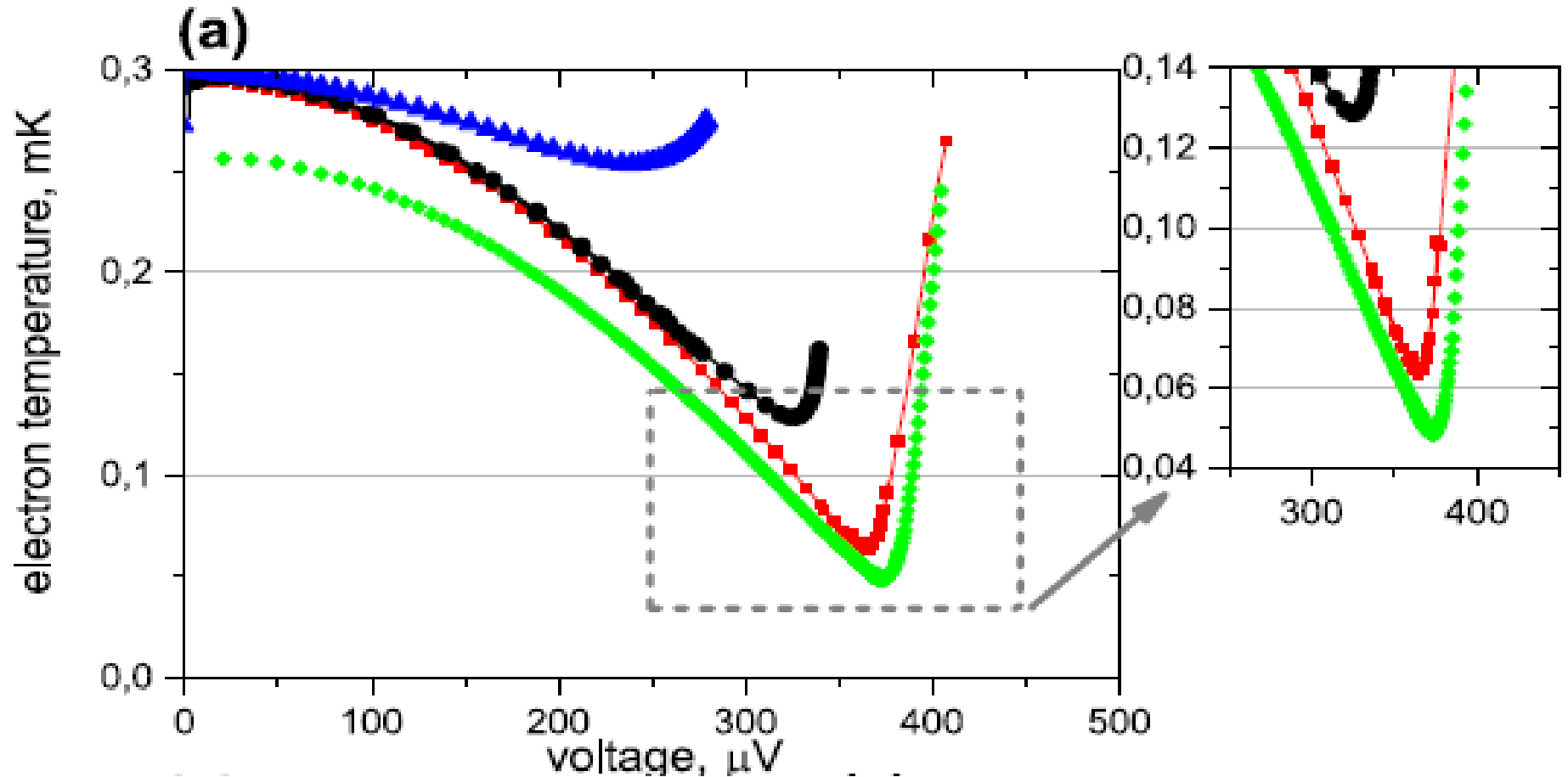
$$\text{NEP}_{\text{ph}} = \sqrt{P_0 h f + P_0^2 / \delta f}$$

with $f=350$ GHz, $\delta f=33$ GHz, P_0 – accepted power of a signal.

Suppression of Andreev heating current



Design 1 - Design 2 - Design 3



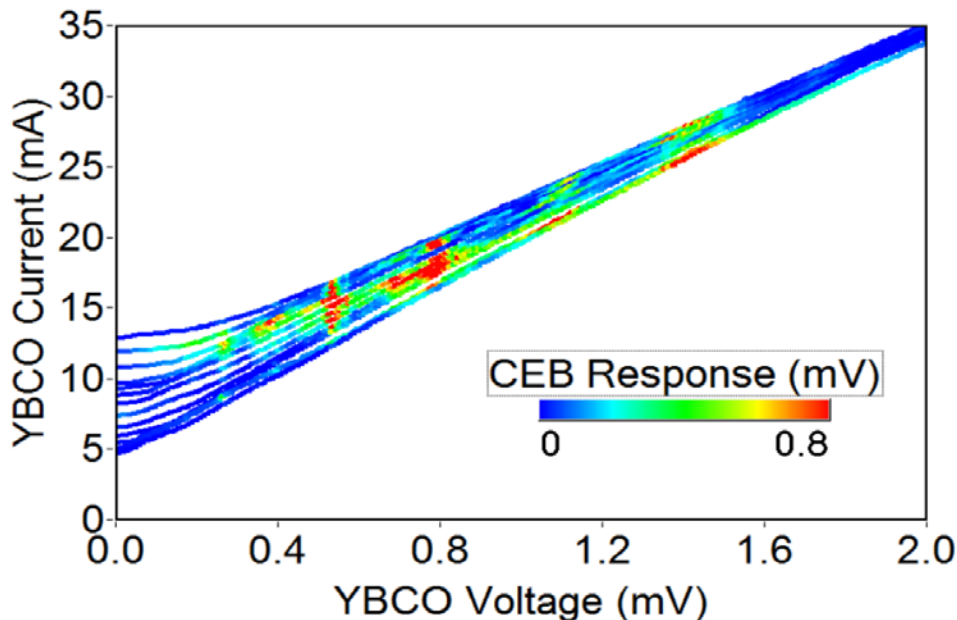
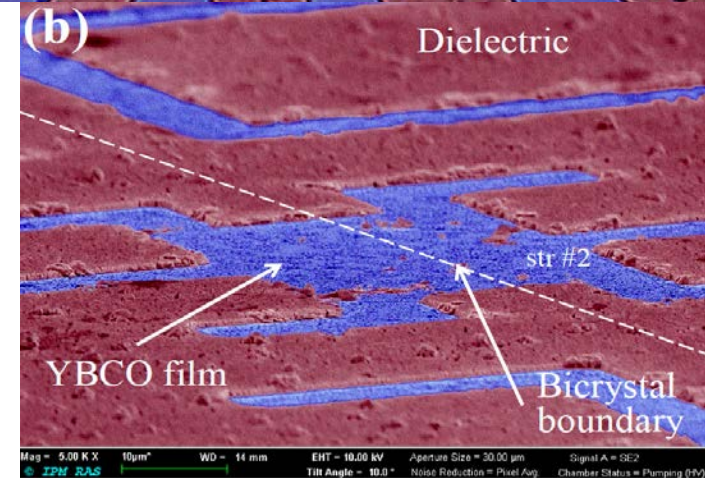
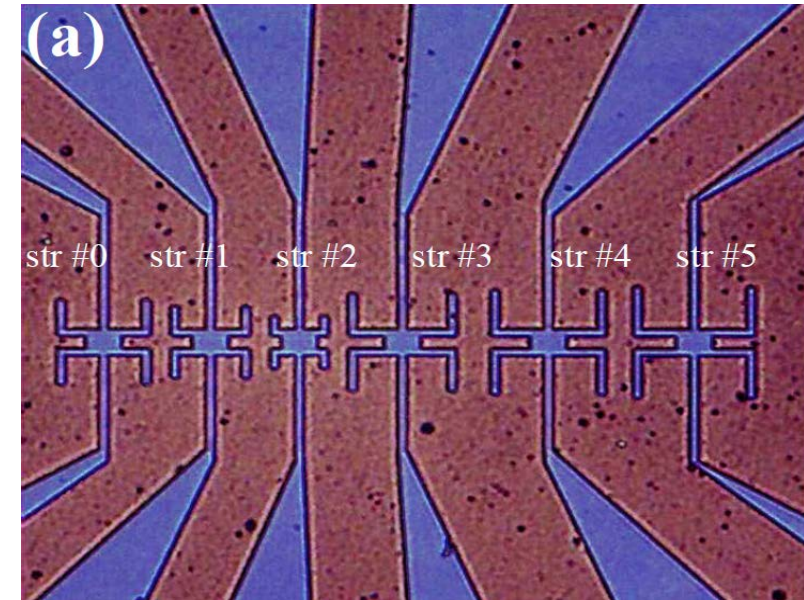
Record electron cooling from 300 to 65 mK!
And from 256 to 48 mK, by a factor of 5.3!

A.V. Gordeeva, A.L. Pankratov, et al, **Scientific Reports**, 10, 21961 (2020)

<https://www.nature.com/articles/s41598-020-78869-z>

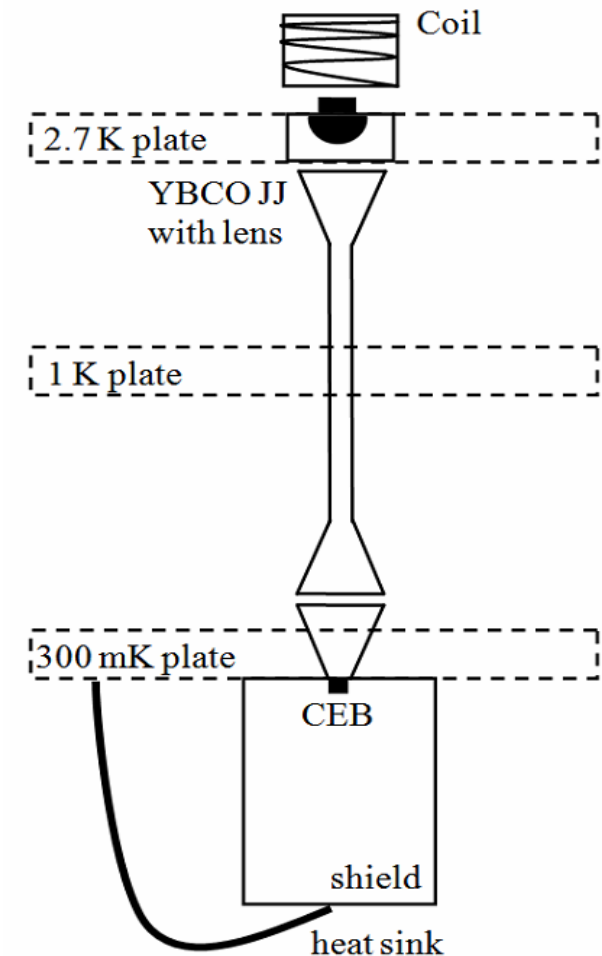
Investigations of YBCO HTSC Josephson junctions

The preliminary mask technology has been developed for the formation of YBCO structures (patent No. 188983). The topology of the superconducting structure is formed at the stage of YBCO deposition into local windows of the preliminary mask - superconducting elements are formed in the mask windows, and insulating regions are formed between them. **The operation of etching the YBCO film is eliminated. The number of defects is reduced.** This technology makes it possible to carry out multiple cycles of YBCO deposition, increasing the film thickness.



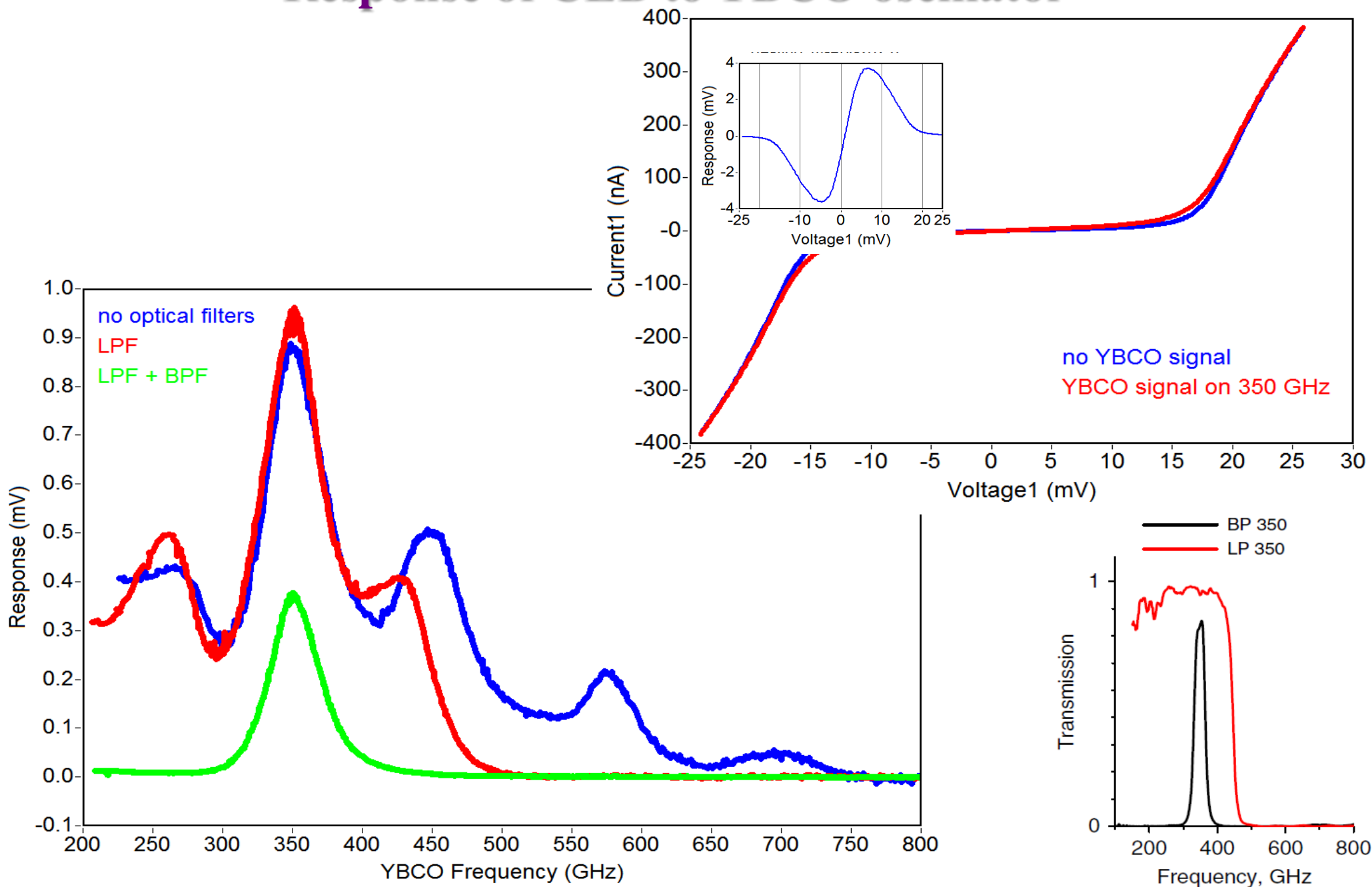
Above are SEM images of structures with dipole antennas. On the left, in blue – the family of current-voltage characteristics of the sample, in red – the signal power received by the bolometer.

Experimental setup

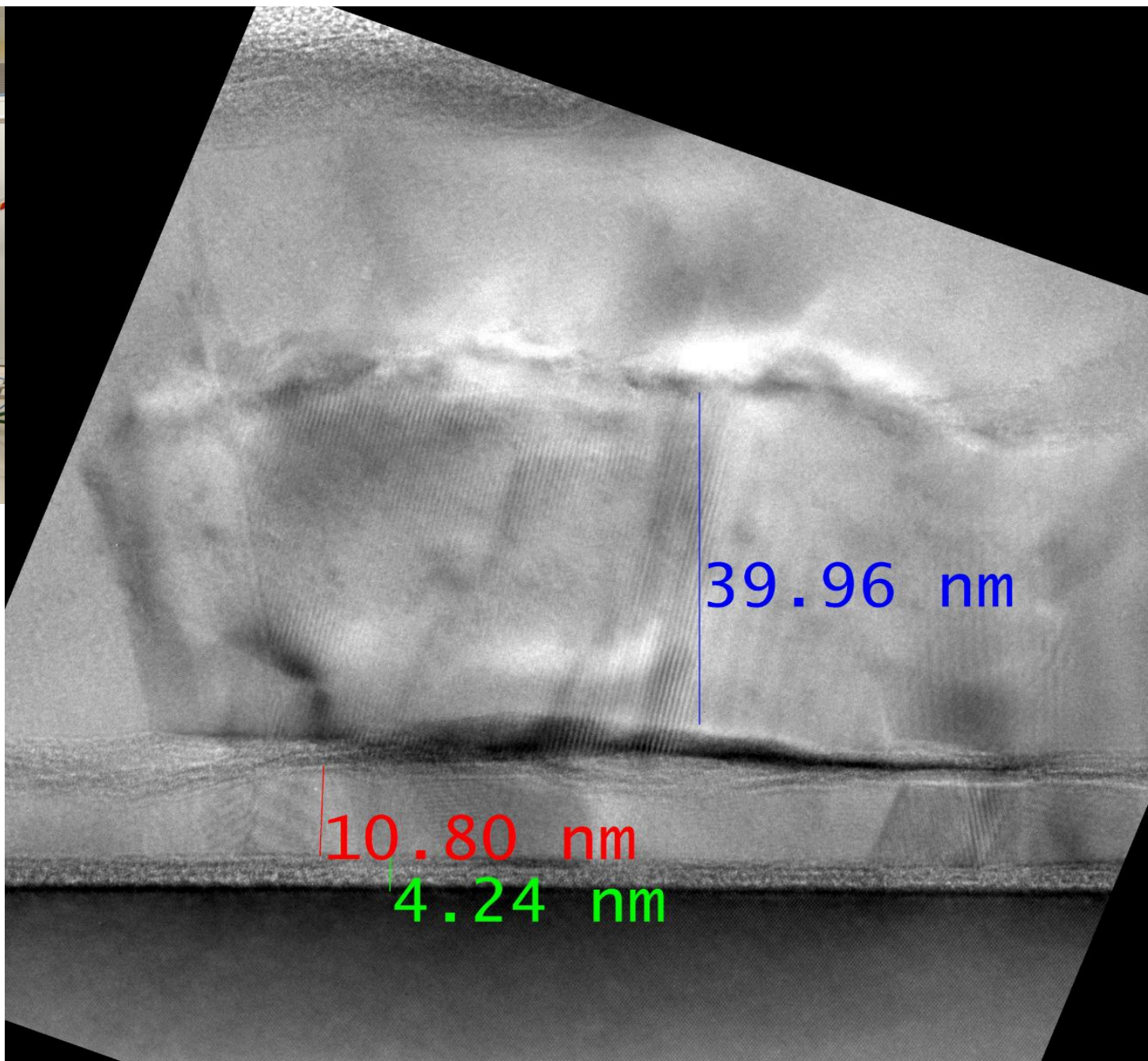


L. Revin, D. Masterov, A. Parafin, S. Pavlov, D. Pimanov, A. Chiginev, et al.,
A Bunch of YBCO Josephson Generators for the Analysis of Resonant Cold-
Electron Bolometers, [Applied Sciences](#) 12, 11960 (2022).

Response of CEB to YBCO oscillator



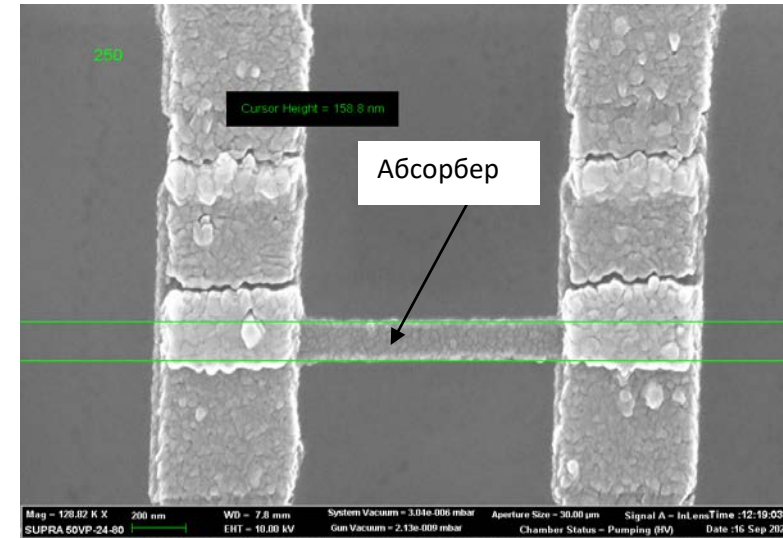
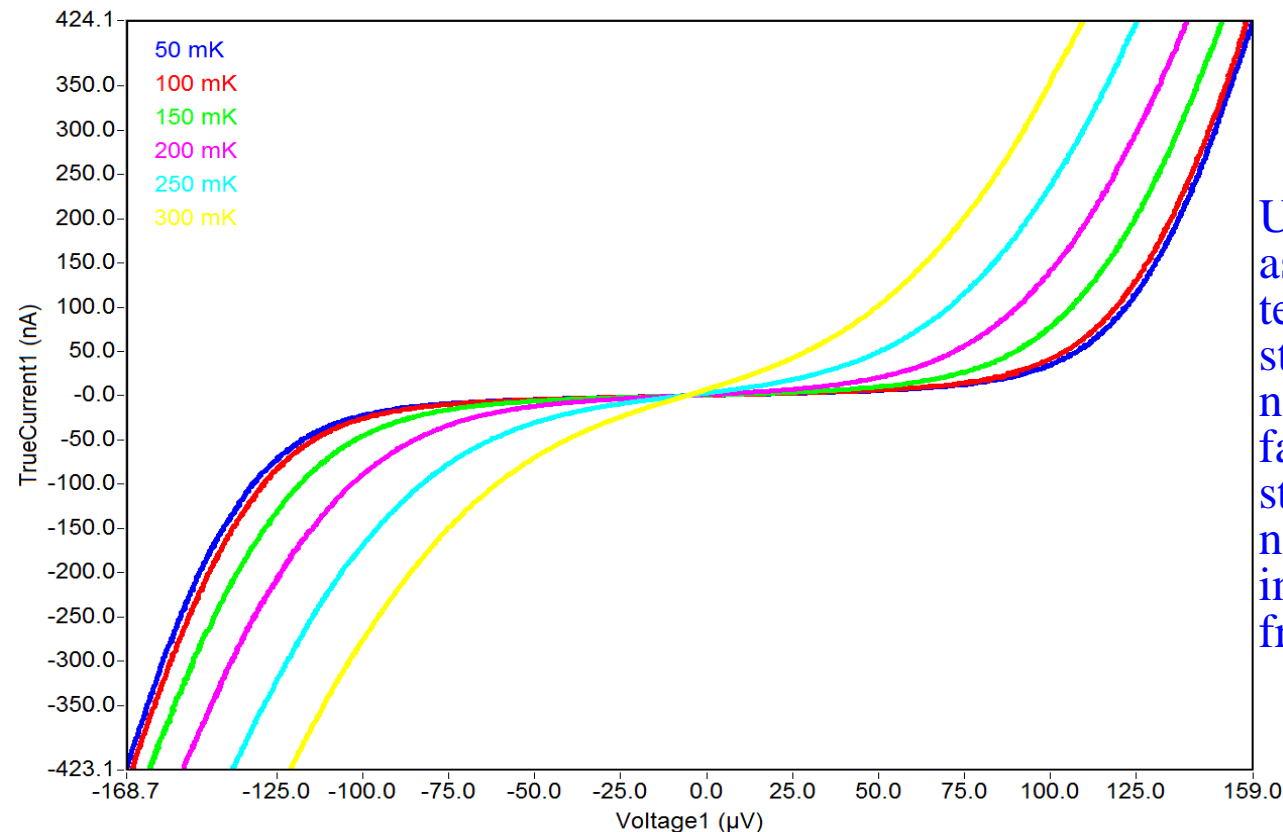
Transfer of technologies to Nizhny Novgorod



Transfer of technologies to Nizhny Novgorod

Transfer of technologies for creating superconducting tunnel junction nanostructures from Chalmers University of Technology is underway. Using the technological base of the Center for Collective Use of the IPM RAS and the Center for Quantum Technologies of the Nizhny Novgorod State Technical University, the first test structures of superconductor-insulator-normal metal contacts were fabricated.

(testing, 2-Jun-2022)



Using electron- and photo- lithographies, as well as the shadow evaporation technique, the first Nizhny Novgorod structures with superconductor-insulator-normal metal tunnel junctions were fabricated. Top – SEM image of the structure with an absorber width of 150 nm, left – IVC of the structure measured in a dilution cryostat at temperatures from 50 to 300 mK.

Hierarchy of noise

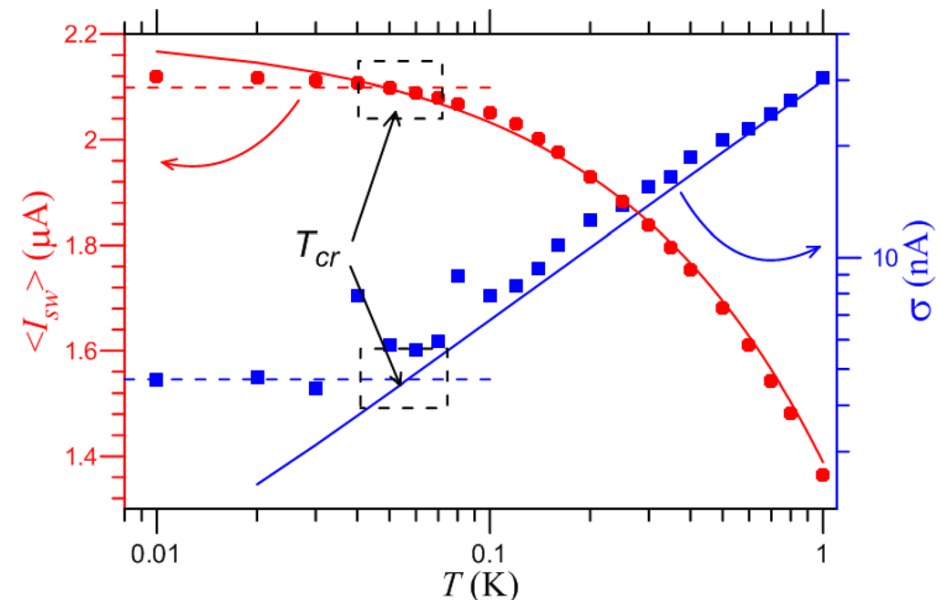
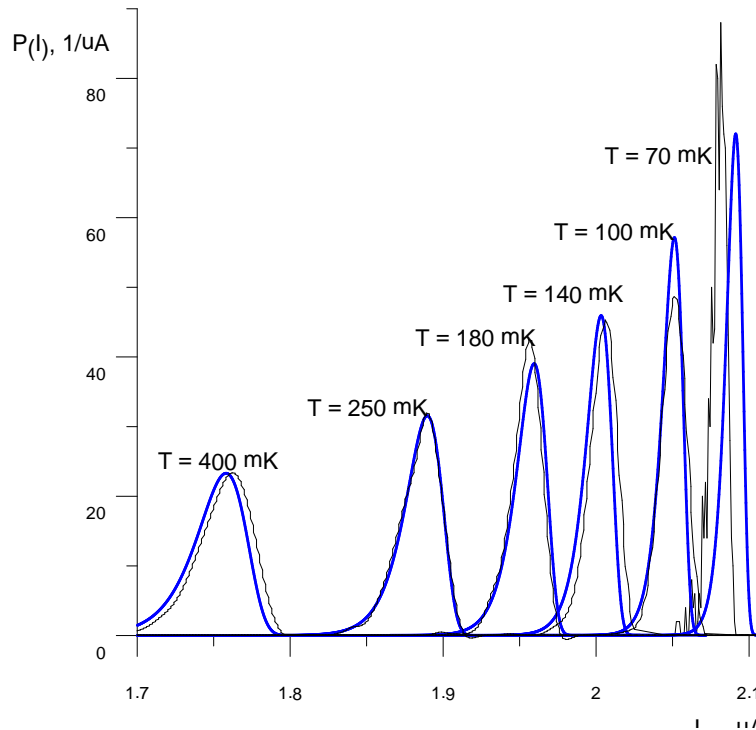
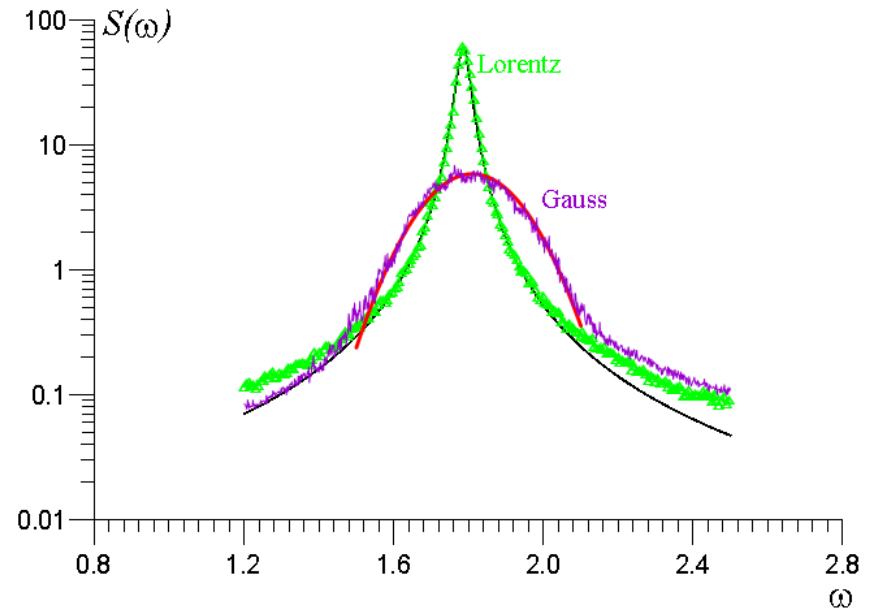
Technical noises (narrow band)

Natural noises (broad band):

Thermal noise $S_I(\omega) \sim kT/R$

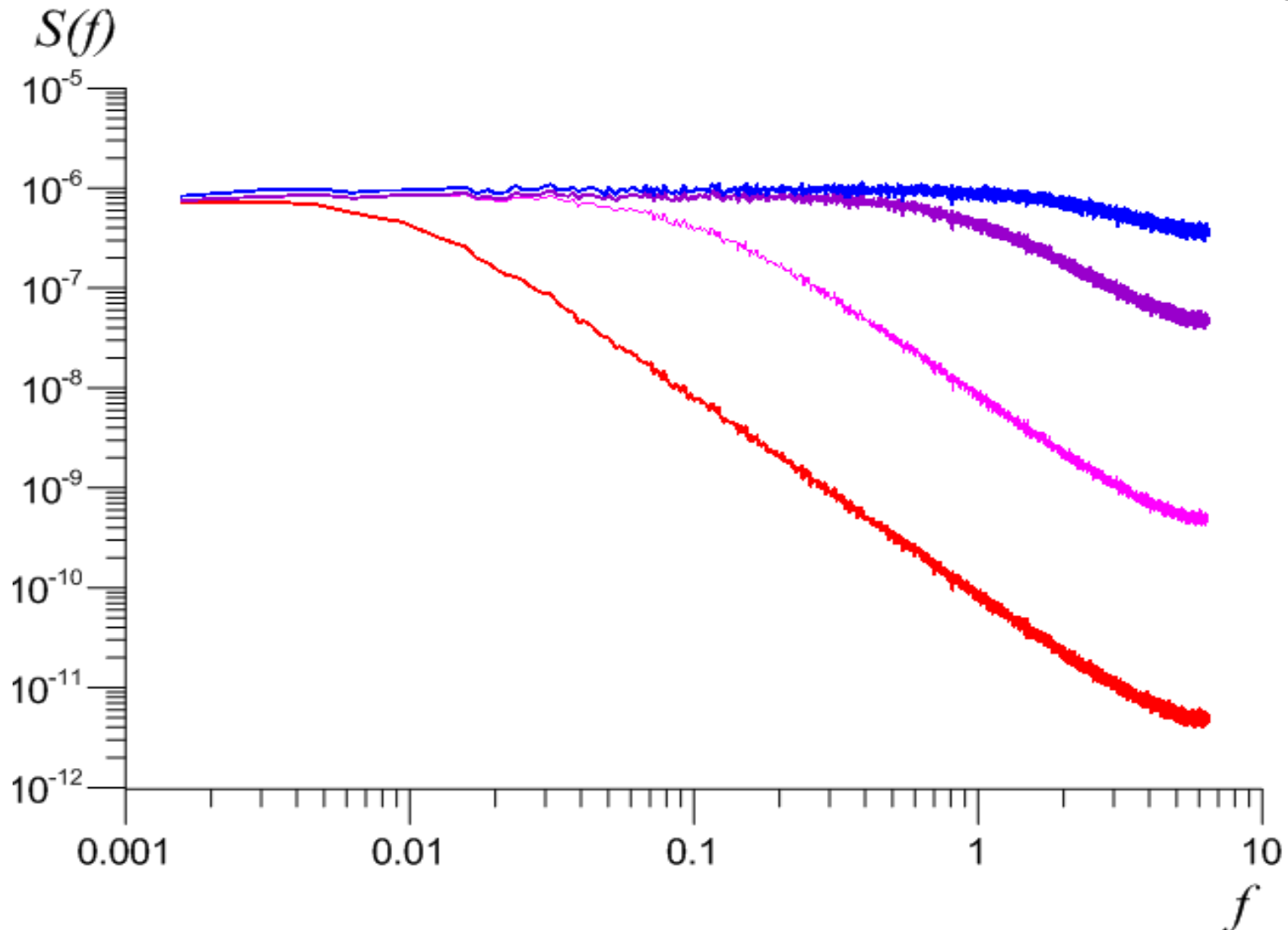
Shot noise $S_I(\omega) \sim eI/2$

Quantum noise $S_I(\omega) \sim h\omega/R$



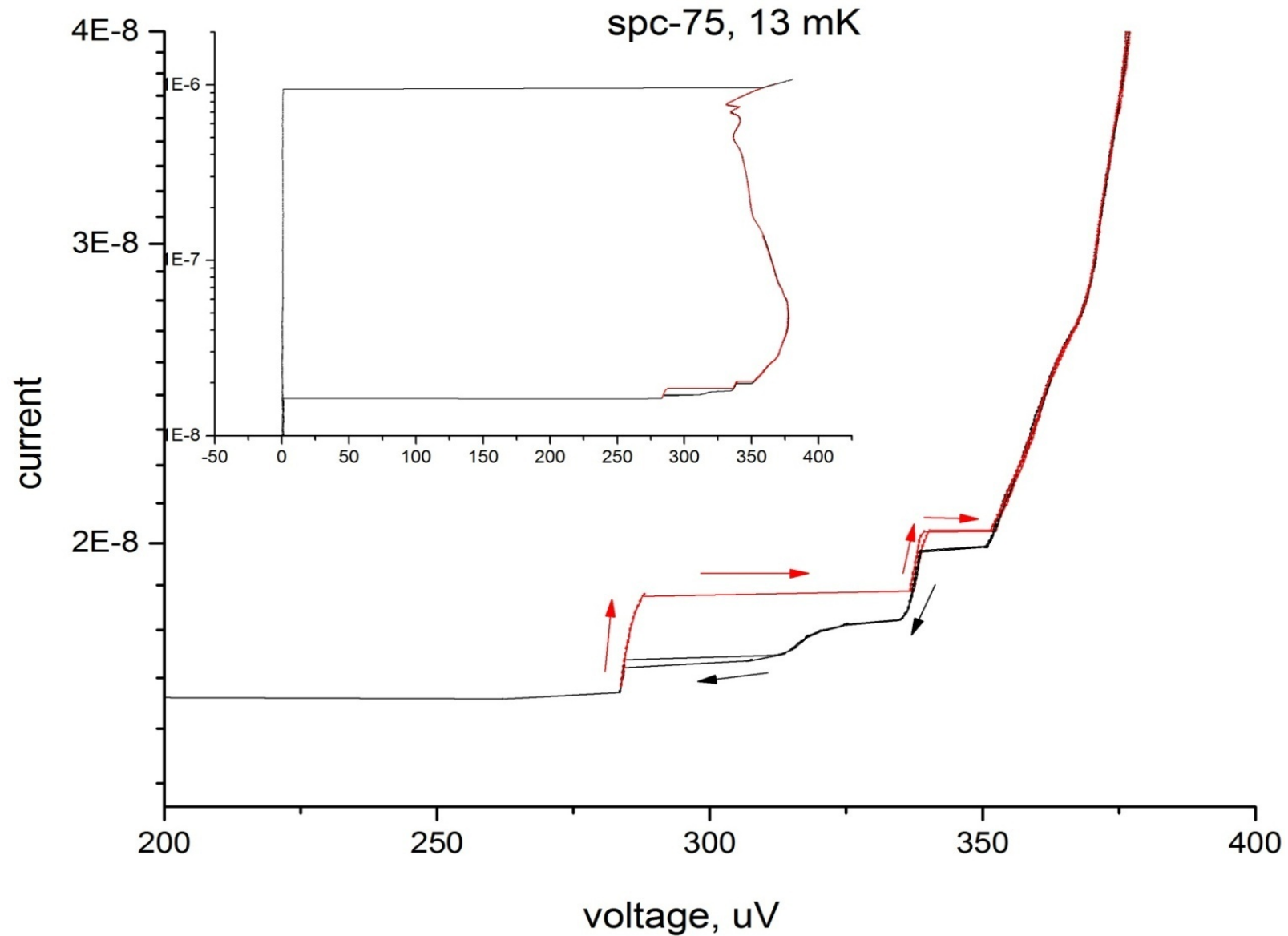
Pink noise – realistic noise model

$$dx/dt = -ax + \xi(t), \quad \langle \xi(t)\xi(t+\tau) \rangle = D\delta(\tau)$$





Current-voltage characteristics of SIS junction



Langevin and Fokker-Planck equations

$$\frac{dx(t)}{dt} = -\frac{1}{h} \frac{dU(x)}{dx} + \xi(t)$$

$$\langle \xi(t) \rangle = 0, \quad \langle \xi(t) \xi(t + \tau) \rangle = D \delta(\tau), \quad D = 2kT/h$$

$$\frac{\partial W(x, t)}{\partial t} = -\frac{\partial G(x, t)}{\partial x} = \frac{1}{B} \frac{\partial}{\partial x} \left[\frac{du(x)}{dx} W(x, t) + \frac{\partial}{\partial x} W(x, t) \right]$$

$$B = 1/D, \quad u(x) = U(x)/kT, \quad W(c, t) = 0, \quad G(d, t) = 0.$$

- Dimensionless FP equation

$$\frac{\partial W(x, t)}{\partial t} = D \frac{\partial}{\partial x} \left[\frac{du(x)}{dx} W(x, t) + \frac{\partial}{\partial x} W(x, t) \right]$$

- Change of variables:

$$W(x, t) = \Psi(x, t) e^{-\frac{u(x)}{2}}$$

- Change of time:

$$t = i\tau$$

- Dimensionless Schroedinger equation

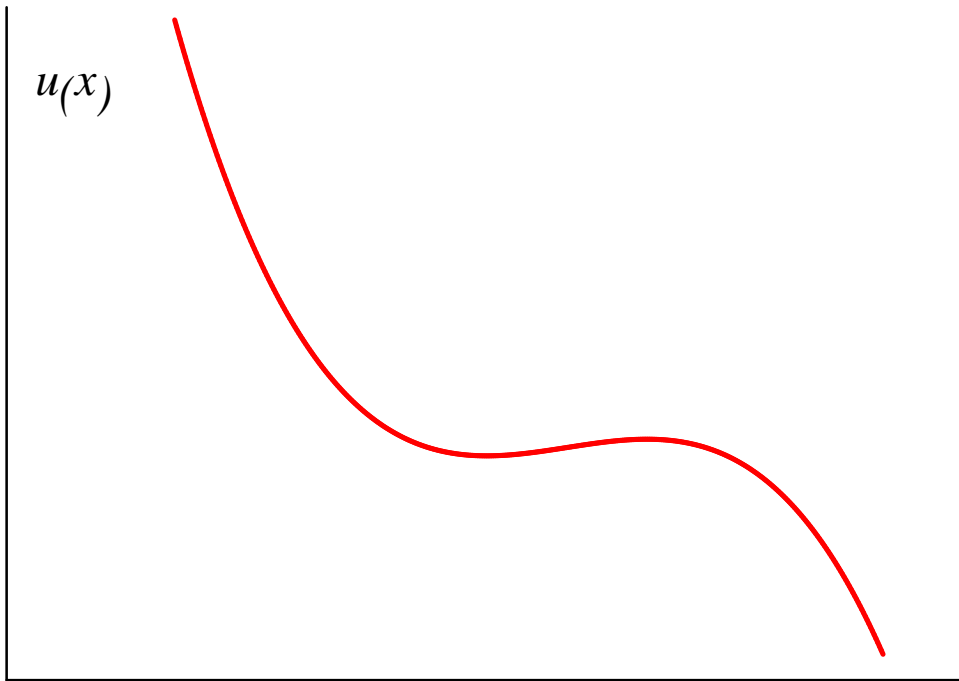
$$\frac{\partial \psi(x, \tau)}{\partial \tau} = iD \left[\frac{\partial^2 \psi(x, \tau)}{\partial x^2} - V(x) \psi(x, \tau) \right]$$

- Connection between potentials in FP and Schroedinger equations

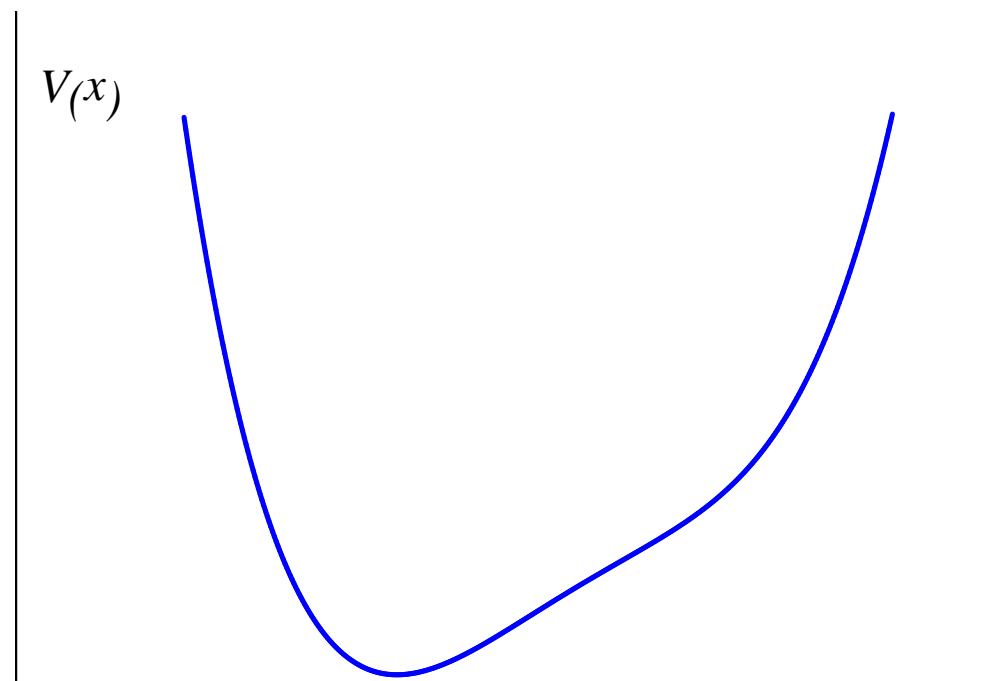
$$V(x) = -\frac{1}{2} \frac{d^2 u(x)}{dx^2} + \left(\frac{1}{2} \frac{du(x)}{dx} \right)^2$$

M. Bernstein and L.S. Brown, Supersymmetry and the Bistable Fokker-Planck Equation, Phys. Rev. Lett., **52**, 1933 (1984).

$$\frac{\partial W(x,t)}{\partial t} = D \frac{\partial}{\partial x} \left[\frac{du(x)}{dx} W(x,t) + \frac{\partial}{\partial x} W(x,t) \right] \quad \frac{\partial \psi(x,\tau)}{\partial \tau} = iD \left[\frac{\partial^2 \psi(x,\tau)}{\partial x^2} - V(x) \psi(x,\tau) \right]$$

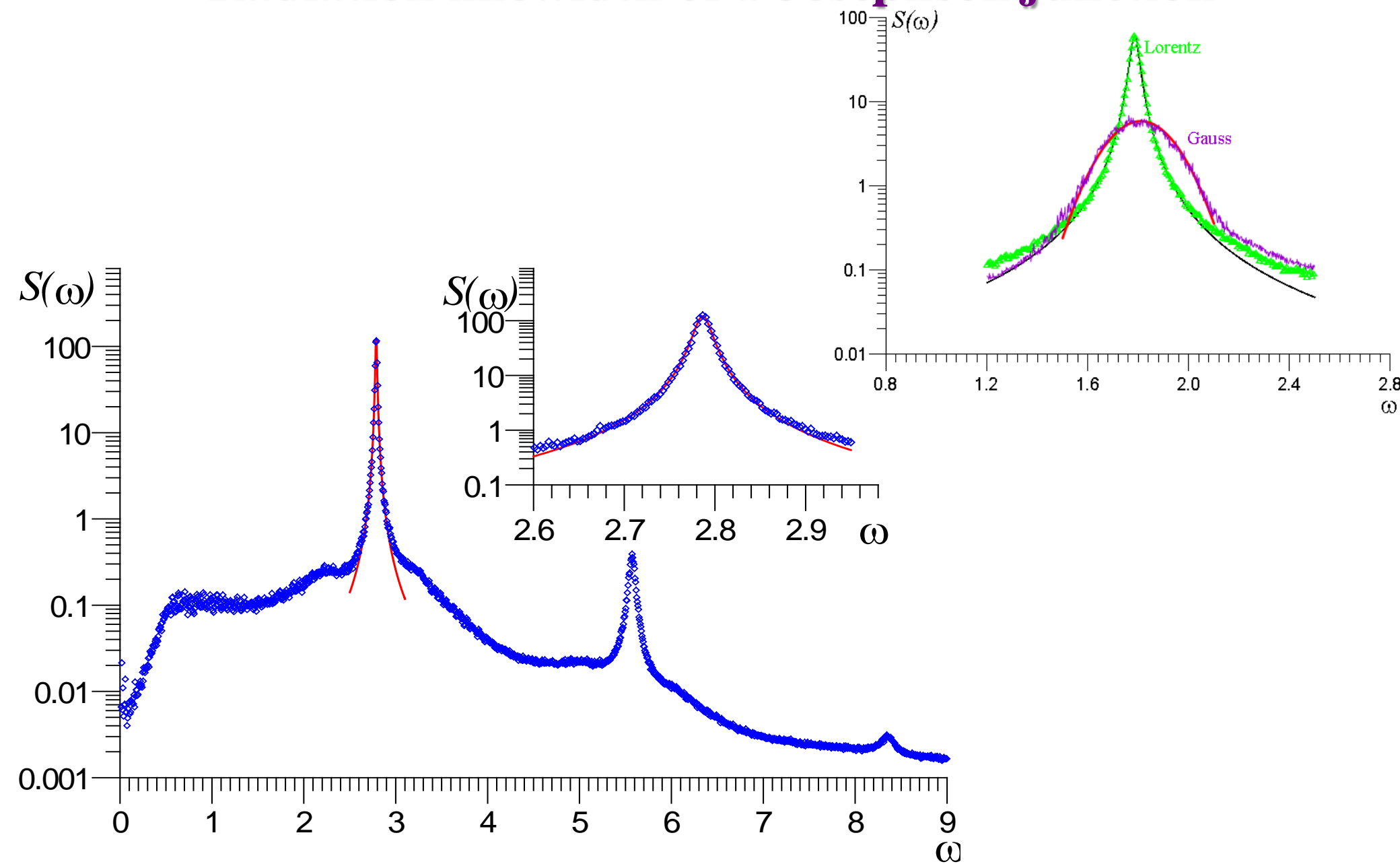


$$u(x) = x^2 - x^3$$



$$V(x) = (3x^2/2 - x)^2 + 3x - 1$$

Radiation linewidth of a Josephson junction



VOLTAGE DUE TO THERMAL NOISE IN THE dc JOSEPHSON EFFECT

Vinay Ambegaokar*

Laboratory of Atomic and Solid State Physics, Cornell University, Ithaca, New York 14850

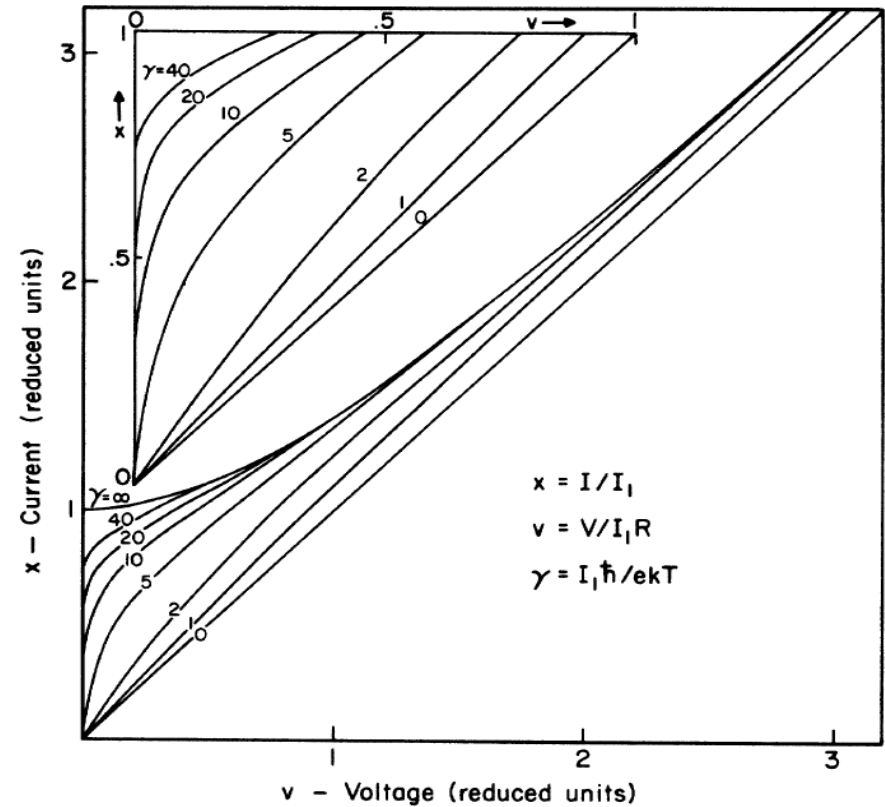
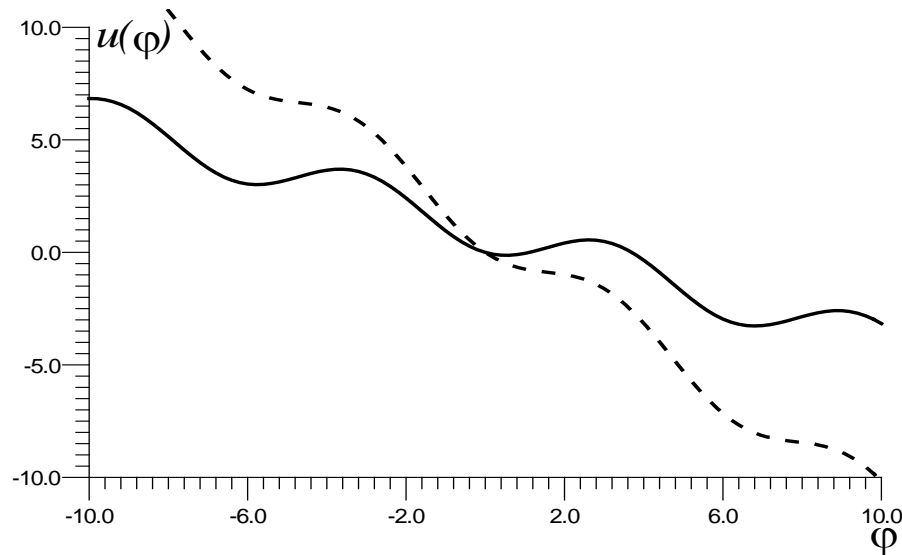
and

B. I. Halperin

Bell Telephone Laboratories, Murray Hill, New Jersey 07974

(Received 25 April 1969)

$$\frac{\partial W(\varphi, t)}{\partial t} = \frac{1}{B} \frac{\partial}{\partial \varphi} \left[\frac{du(\varphi)}{d\varphi} W(\varphi, t) + \frac{\partial}{\partial \varphi} W(\varphi, t) \right]$$



Method of reduced phase

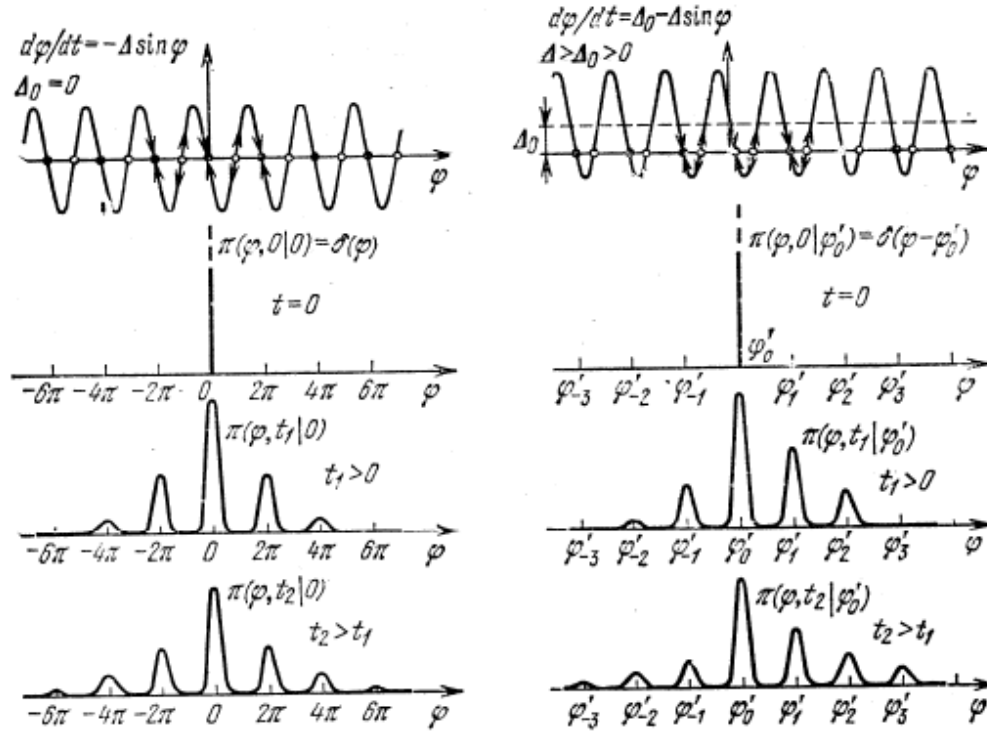


Рис. 22.3. Качественный характер изменения плотности вероятности полной фазы во времени при $\Delta_0 = 0$ и $\Delta > \Delta_0 > 0$.

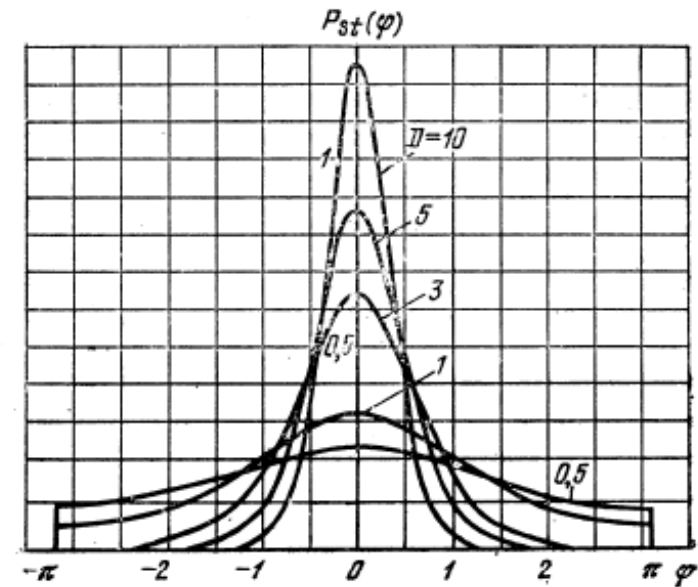


Рис. 22.4. Стационарные плотности вероятности приведенной разности фаз в отсутствие начальной расстройки ($\Delta_0 = 0$).

Radiation linewidth of a short Josephson junction

VOLUME 22, NUMBER 26

PHYSICAL REVIEW LETTERS

30 JUNE 1969

LINEWIDTH OF THE RADIATION EMITTED BY A JOSEPHSON JUNCTION*

A. J. Dahm,[†] A. Denenstein,[‡] D. N. Langenberg, W. H. Parker,[§] D. Rogovin, and D. J. Scalapino

Department of Physics and Laboratory for Research on the Structure of Matter,

University of Pennsylvania, Philadelphia, Pennsylvania

(Received 18 April 1969)

backward junction currents. For the low-frequency region of interest, it follows from an analysis of the Josephson-Maxwell equations⁶ (and it is clear on physical grounds) that the junction impedance is simply the dynamic resistance $R_D = (dI/dV)^{-1}$, so that

$$\langle \delta V^2 \rangle = R_D^2 \int_0^\infty P_{Iqp}(\omega) d\omega. \quad (7)$$

Using Eq. (1), Eq. (3), and standard frequency-modulation noise theory,⁷ we obtain for the quasiparticle contribution to the linewidth

$$\Delta \omega_{qp} = (2e/\hbar)^2 R_D^2 I_{qp} (V_0) \coth(\frac{1}{2}\beta V_0). \quad (8)$$

$$\Delta \nu = \Delta \omega / 2\pi = (4\pi R_D^2 kT / V_0) (2e/h)^2 (I_{qp} + I_p).$$

ing Eq. (9) arises because pairs of electrons are coherently transferred. The expression for the linewidth including both the quasiparticle and the pair contributions is⁹

$$S_I \sim kT / R_N$$

$$S_I \sim kT(I_{qp} + I_p) / V = kTI / V = kT / R_S$$

Radiation linewidth of a short Josephson junction

$$I = I_c \sin \varphi + VG_N + C \frac{dV}{dt} + I_F(t).$$

$$\varphi_0 = \frac{2e}{\hbar} V, \quad \omega_p = \sqrt{\frac{2eI_c}{\hbar C}}, \quad \omega_c = \frac{2eR_N I_c}{\hbar}.$$

$$V = \bar{V} + \tilde{V}, \quad \varphi = \omega_j t + \tilde{\varphi}, \quad \tilde{\varphi} = \frac{2e}{\hbar} \int \tilde{V} dt$$

$$\omega_j = 2e\bar{V} / \hbar = 2\pi\bar{V} / \Phi_0$$

$$V(t) = \bar{V} + \text{Im} \sum_{k>0} V_k \exp(jk\theta), \quad \varphi_0 = \omega_j = \tilde{\varphi}_0$$

Small fluctuations: $\Delta f \ll \omega_j$

Large damping:

$$\beta = (\omega_c / \omega_p)^2 = 2e / \hbar I_c R_N^2 C \ll 1$$

$$S_I(\omega) = kT / \pi R_N = \text{const}$$

$$\frac{1}{\omega_c} \frac{d\varphi}{dt} = i - \sin \varphi + i_F(t)$$

$$\langle i_F(t) \rangle = 0, \quad \langle i_F(t) i_F(t + \tau) \rangle = 2\gamma \delta(\tau)$$

$$\gamma \equiv \frac{2ekT}{\hbar I_c} = \frac{I_T}{I_c}$$

$\tilde{\varphi}$ - small phase increments

φ_0 - solution in the absence of fluctuations

$$\omega_c^{-1} \varphi_0 + \sin \varphi = i,$$

$$\varphi_0 = 2 \text{Arctg} \left\{ \left[v / (i + 1) \right] \text{tg} \frac{\theta}{2} \right\} - \pi/2,$$

$$\omega_c^{-1} \tilde{\varphi} + \cos \varphi_0 \tilde{\varphi} = \tilde{i}, \quad \tilde{i} = i_F = I_F / I_c$$

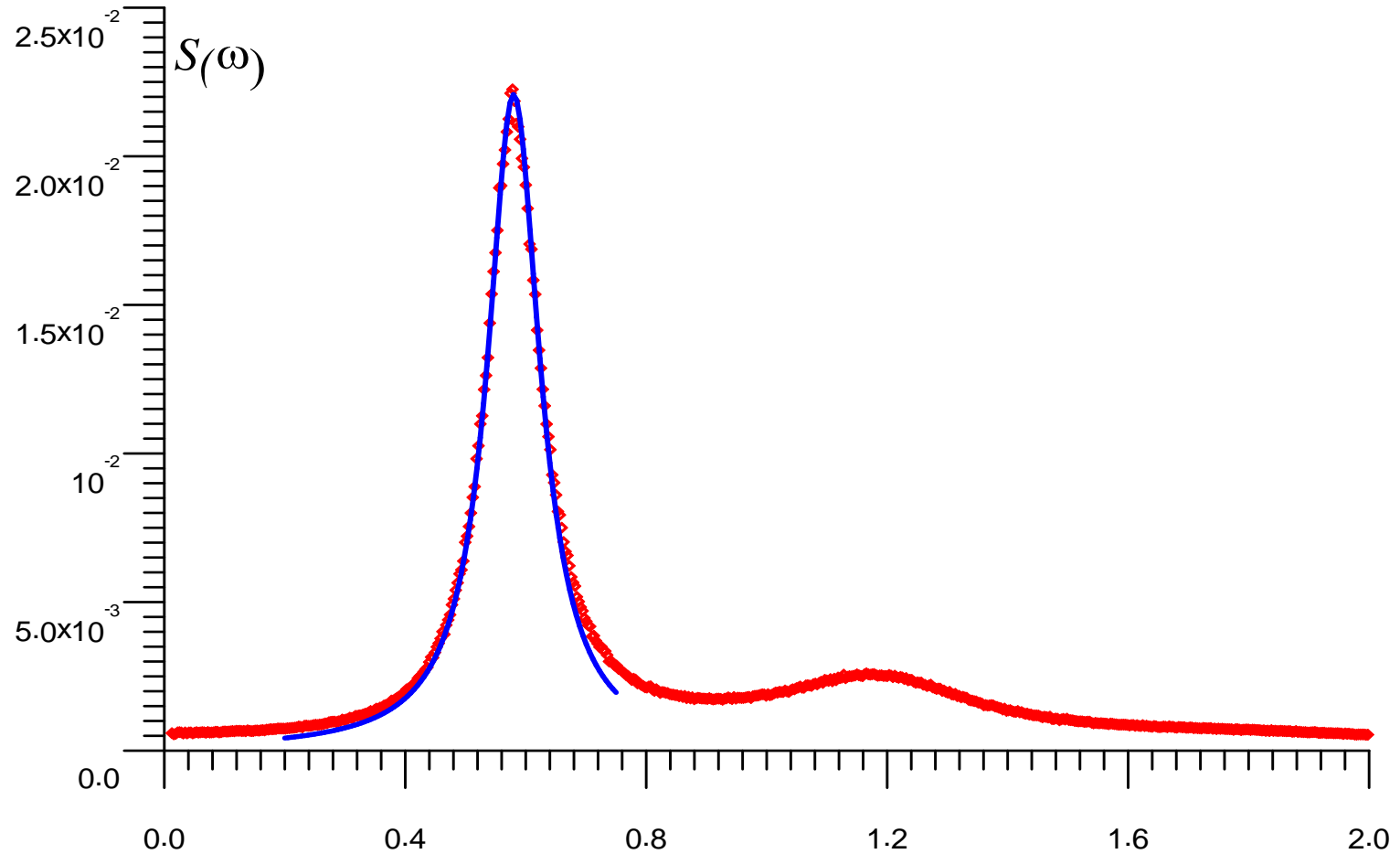
$$S_V(0) = R_d^2 S_I'(0);$$

$$S_I'(0) = S_I(0) + (I_c^2 / 2I^2) S_I(\omega_j)$$

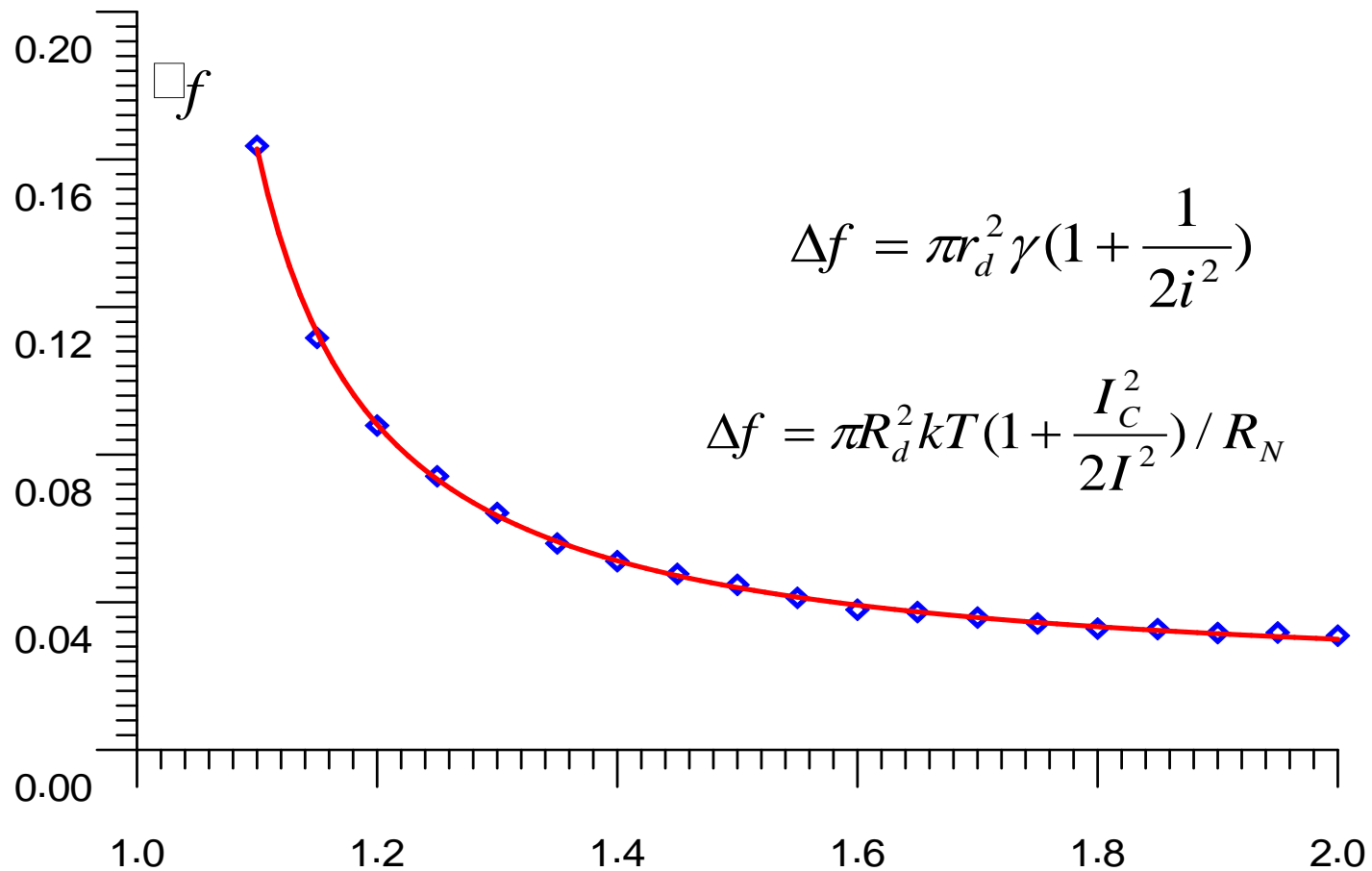
$$\Delta f = \pi r_d^2 \gamma (1 + \frac{1}{2i^2}) \quad r_d = \frac{dv}{di} = \frac{i}{\sqrt{i^2 - 1}}$$

$$\Delta f = \pi R_d^2 kT (1 + \frac{I_c^2}{2I^2}) / R_N$$

Radiation linewidth of a short Josephson junction



Radiation linewidth of a short Josephson junction



Shamporov V.A., Myasnikov A.S., Pankratova E.V., Pankratov A.L. (2017): Spectral linewidth of parallel Josephson junction array with intermediate-to-large damping, [Physical Review B](#), 96, 064522.

Radiation linewidth of a long Josephson junction

$$\frac{\partial^2 \varphi}{\partial t^2} + \alpha \frac{\partial \varphi}{\partial t} - \frac{\partial^2 \varphi}{\partial x^2} = \eta - \sin(\varphi); \quad \frac{\partial \varphi(0, t)}{\partial x} = \frac{\partial \varphi(L, t)}{\partial x} = H$$

$$\frac{\partial^2 \varphi}{\partial \tau^2} + \beta \frac{\partial \varphi}{\partial \tau} - \frac{\partial^2 \varphi}{\partial z^2} = \beta - \varepsilon \sin(\varphi); \quad \tau = (\eta/\alpha)t$$
$$\varepsilon = (\alpha/\eta)^2 \ll 1$$

$$\frac{\partial^2 \varphi_0}{\partial \tau^2} + \beta \frac{\partial \varphi_0}{\partial \tau} - \frac{\partial^2 \varphi_0}{\partial z^2} = \beta;$$

$$\frac{\partial^2 \varphi_1}{\partial \tau^2} + \beta \frac{\partial \varphi_1}{\partial \tau} - \frac{\partial^2 \varphi_1}{\partial z^2} = -\sin(\omega_J \tau + hz);$$

$$\frac{\partial^2 \varphi_2}{\partial \tau^2} + \beta \frac{\partial \varphi_2}{\partial \tau} - \frac{\partial^2 \varphi_2}{\partial z^2} = -\varphi_{1p}(\tau) \cos(\omega_J \tau + hz).$$

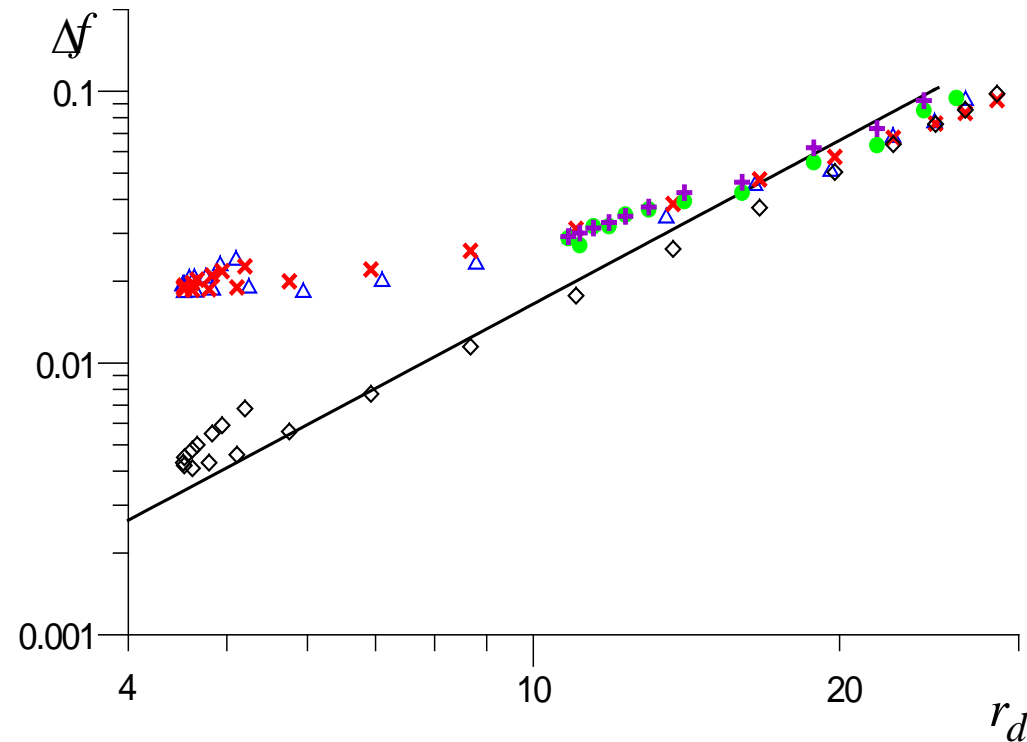
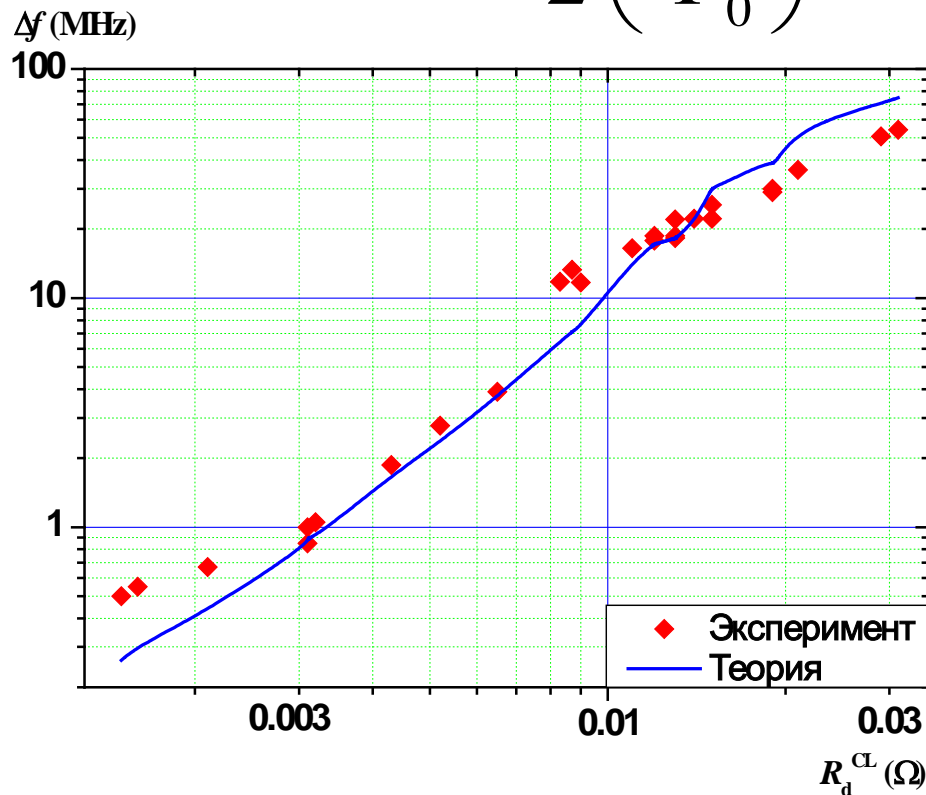
Radiation linewidth of a long Josephson junction

A.L. Pankratov, Phys. Rev. B 65, 054504 (2002).

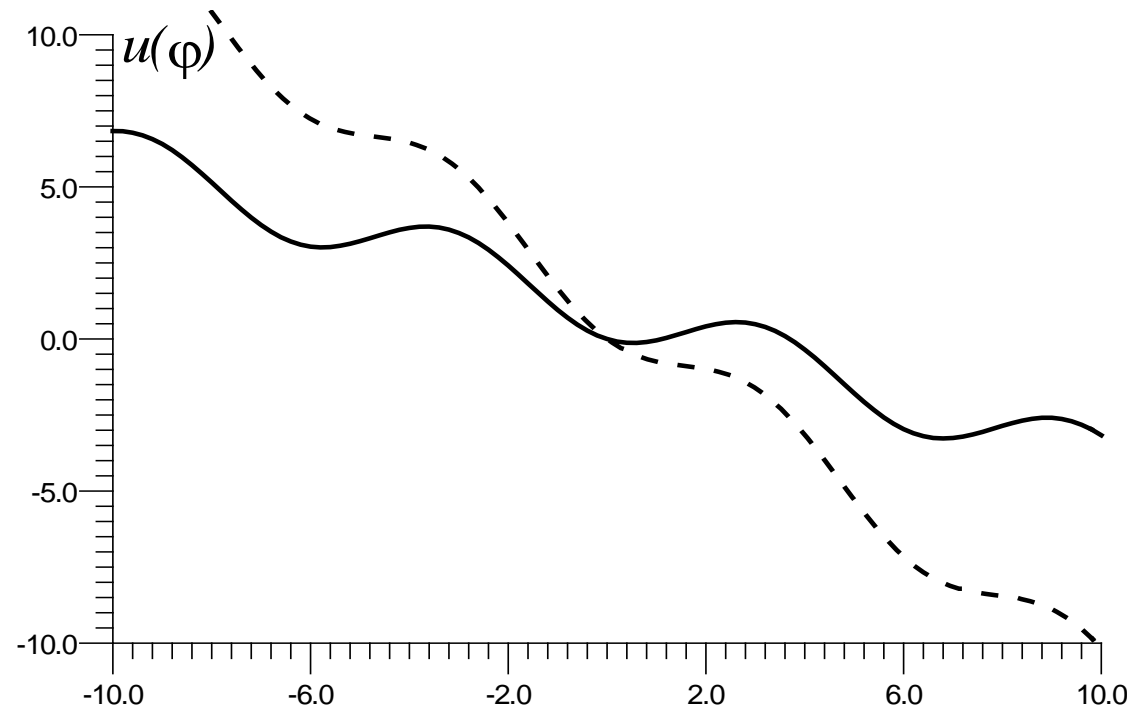
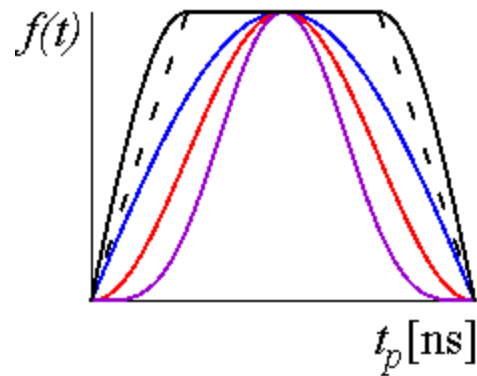
A.L. Pankratov, Appl. Phys. Lett. 92, 082504 (2008).

A.L. Pankratov, Phys. Rev. B 78, 024515 (2008).

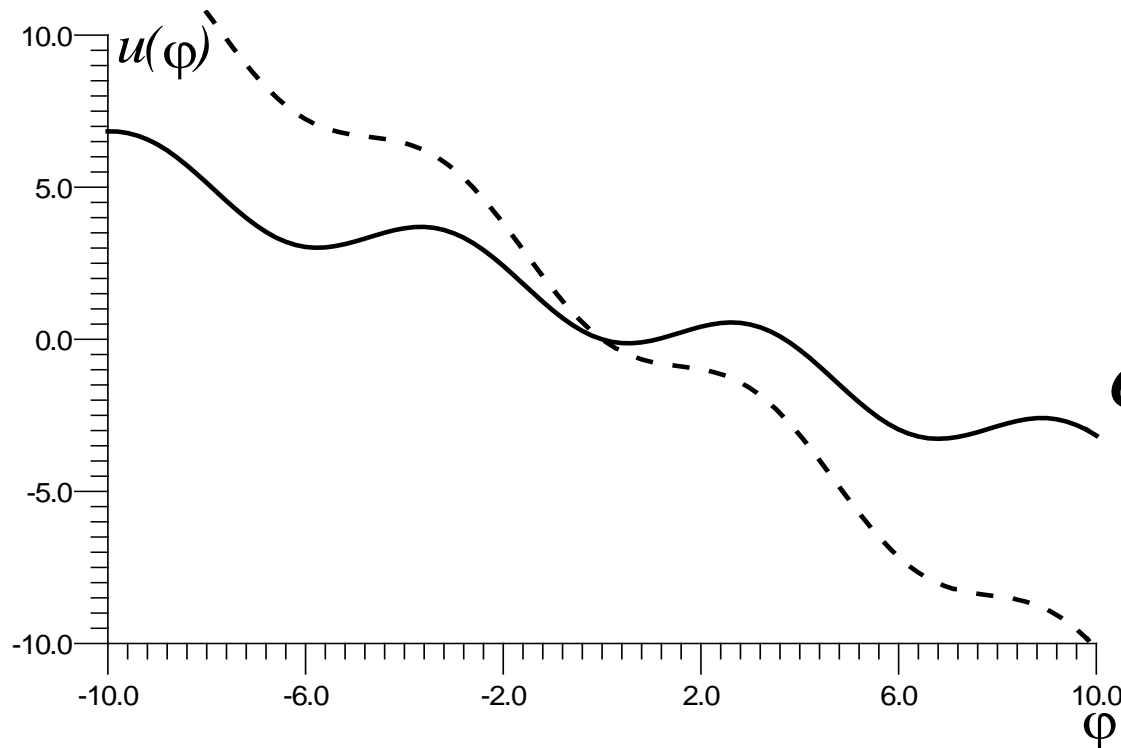
$$\Delta f_{FFO} = \frac{1}{2} \left(\frac{2\pi}{\Phi_0} \right)^2 \left(R_d + K R_d^{CL} \right)^2 \frac{kT}{R_N} (1 + H_0)$$



What do we mean under switching?



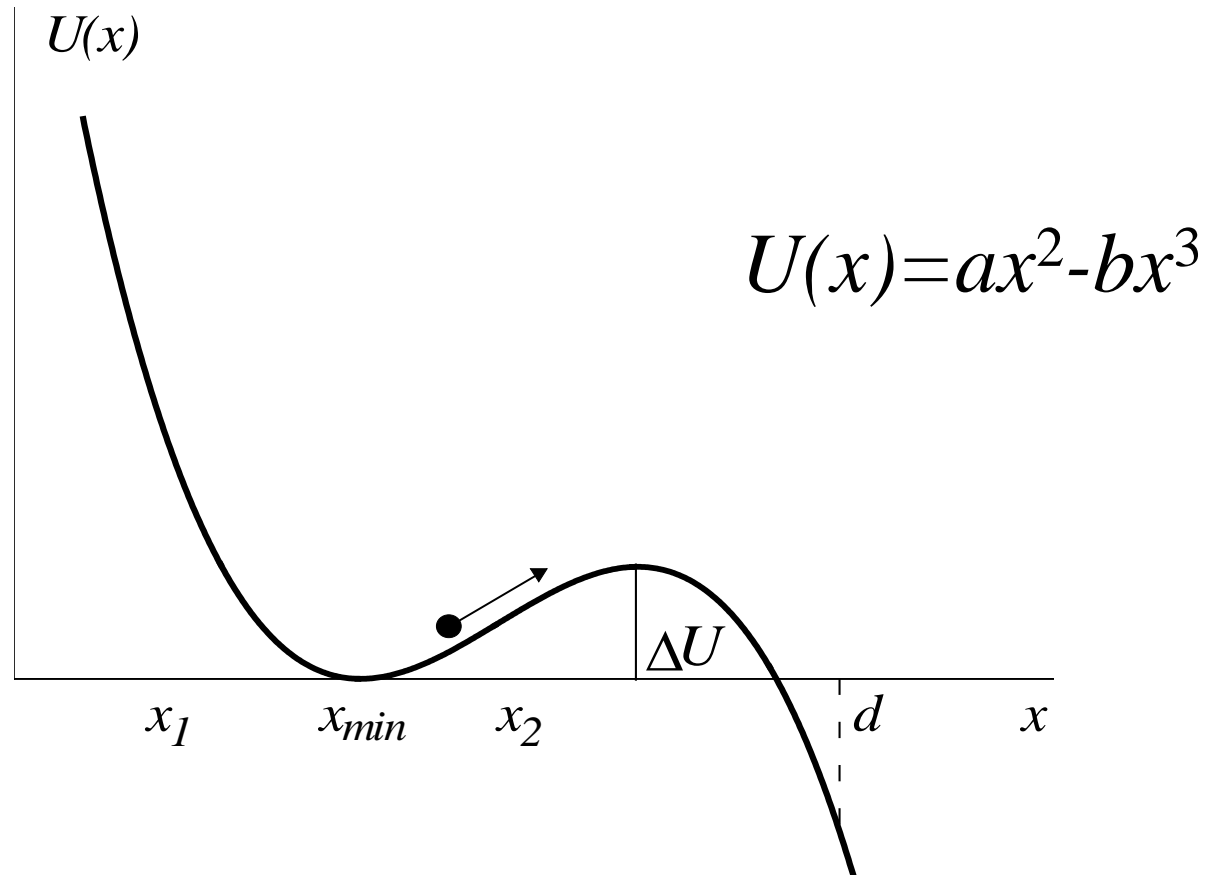
What do we mean under minimization of noise?



$$\sigma \sim e^{\Delta U / kT}$$

$$\sigma \sim \sqrt{kT}$$

Kramers' problem



H.Kramers, Physica 7, 284 (1940).

P. Hanggi, P. Talkner, M. Borkovec, Reaction-rate theory: fifty years after Kramers, Rev. Mod. Phys. 62, 251-341 (1990).

V.I. Melnikov, The Kramers problem: Fifty years of development, Phys. Rep. 209, 1-71 (1991).

A.N. Malakhov, A.L. Pankratov, Evolution times of probability distributions and averages

- Exact solutions of the Kramers' problem, Adv. in Chem. Phys., 121, 357-438 (2002).

Temporal characteristics

1. The moments of First Passage Time

(Pontryagin, Andronov, Vitt, JETP, 1933)

2. Kramers' method: $\theta \sim \exp(\Delta U/kT)$, Physica, 1940

3. Effective eigenvalue (Risken, Yung, Garanin)

4. Generalized moment expansion (Nadler, Schulten)

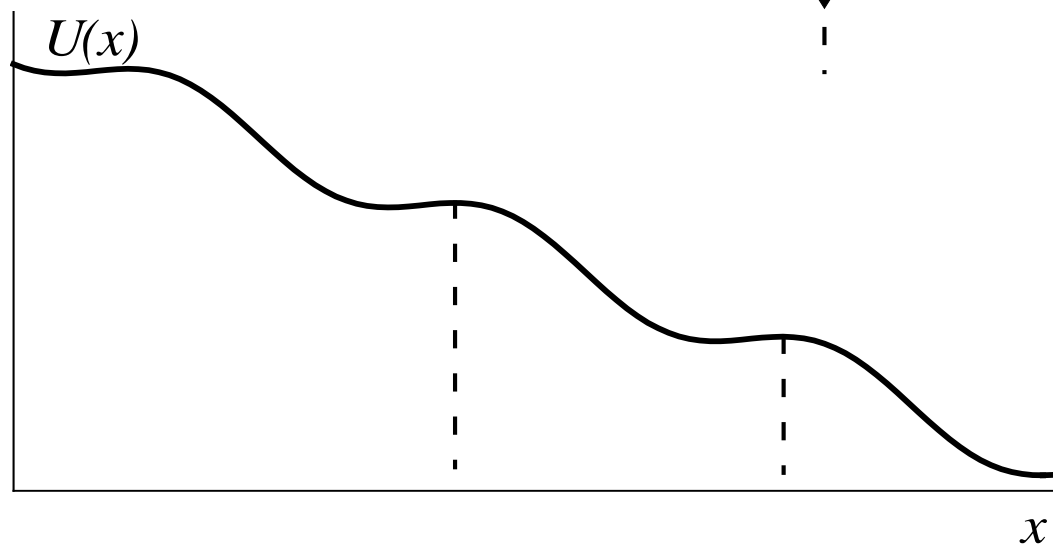
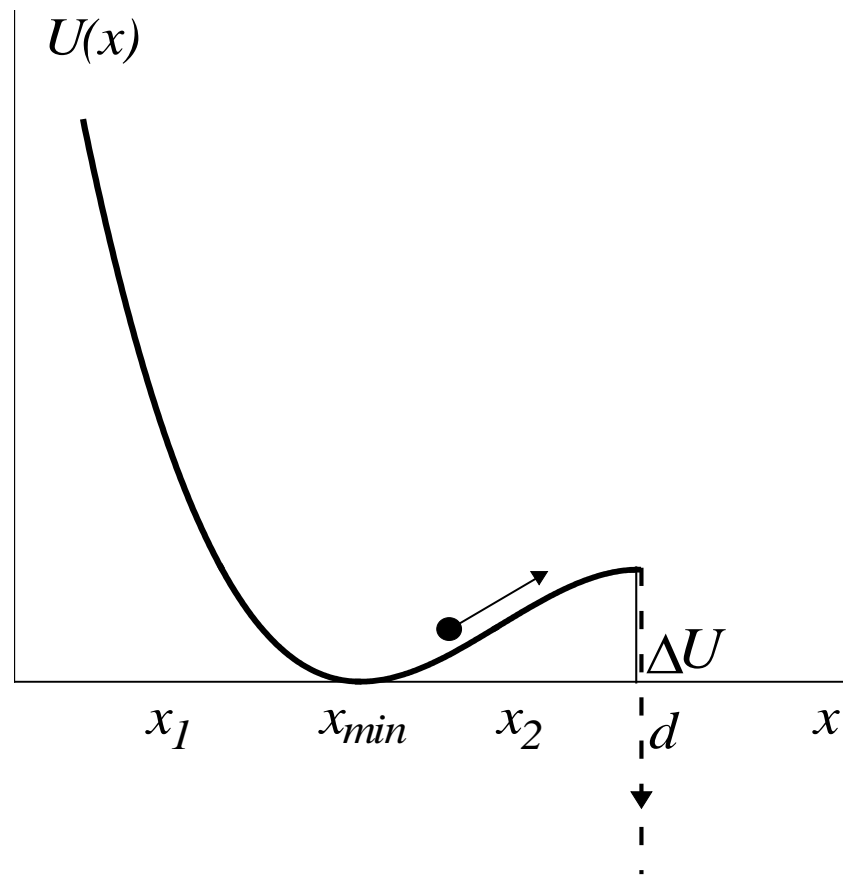
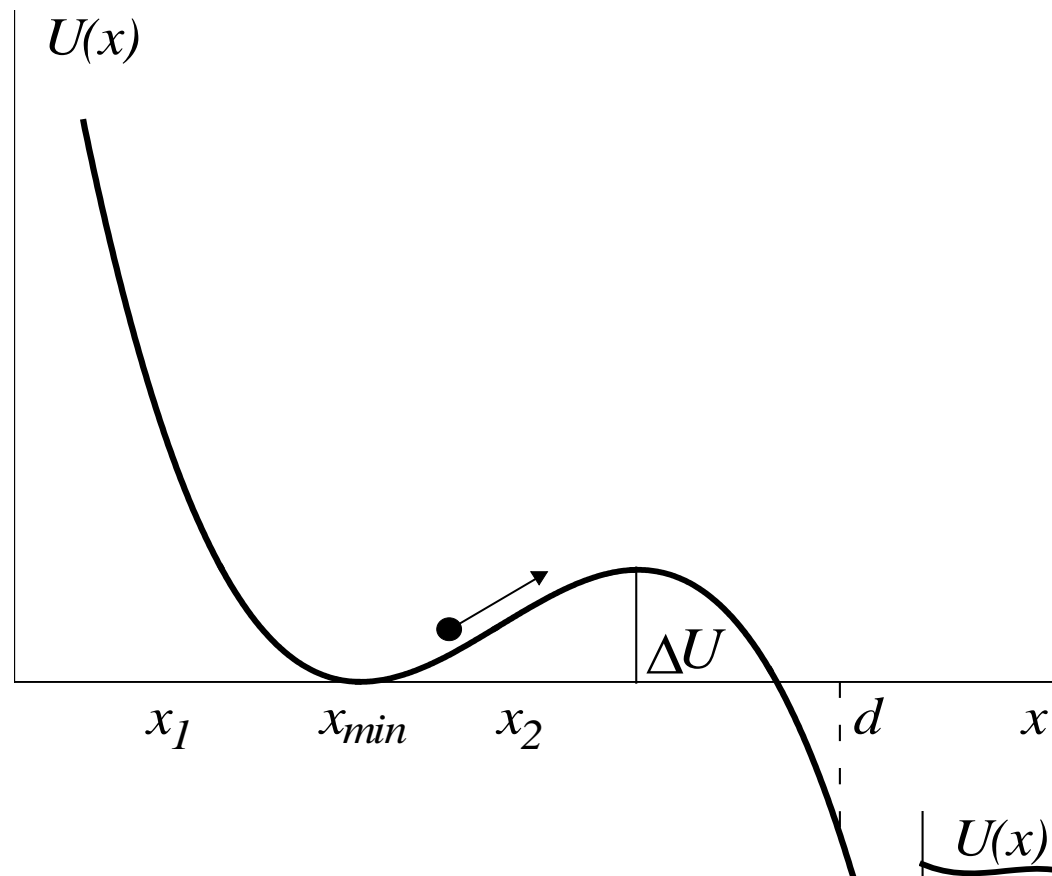
5. Integral relaxation time (Coffey, Kalmykov, Titov)

$$\theta = \frac{\int_0^{\infty} [P(t) - P(\infty)] dt}{P(0) - P(\infty)}$$

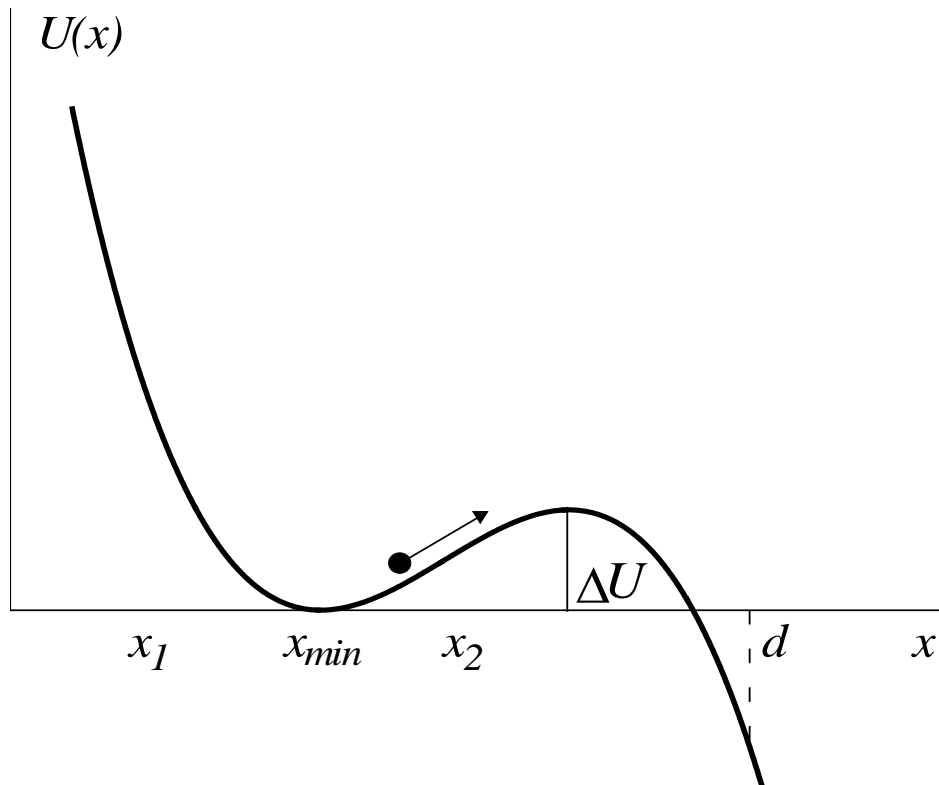
$$\langle t^n \rangle = \int_0^{\infty} t^n w(t) dt$$

$$P(t) = \int_c^d W(x, t) dx$$

probability to find a particle
in the area (c, d)



Kramers' time



$$\tau = \tau_0(kT)e^{\Delta U/kT}$$

		$U_t(x) \sim$					
		$ x ^{\frac{1}{2}}$	$ x ^{\frac{2}{3}}$	$ x $	x^2	x^4	x^∞
$\tau_0(kT) \sim$	$ x ^{\frac{1}{2}}$	$(kT)^3$	$(kT)^{\frac{5}{2}}$	$(kT)^2$	$(kT)^{\frac{3}{2}}$	$(kT)^{\frac{5}{4}}$	$(kT)^1$
	$ x ^{\frac{2}{3}}$	$(kT)^{\frac{5}{2}}$	$(kT)^2$	$(kT)^{\frac{3}{2}}$	$(kT)^1$	$(kT)^{\frac{3}{4}}$	$(kT)^{\frac{1}{2}}$
	$ x $	$(kT)^2$	$(kT)^{\frac{3}{2}}$	$(kT)^1$	$(kT)^{\frac{1}{2}}$	$(kT)^{\frac{1}{4}}$	$(kT)^0$
	x^2	$(kT)^{\frac{3}{2}}$	$(kT)^1$	$(kT)^{\frac{1}{2}}$	$(kT)^0$	$(kT)^{-\frac{1}{4}}$	$(kT)^{-\frac{1}{2}}$
	x^4	$(kT)^{\frac{5}{4}}$	$(kT)^{\frac{3}{4}}$	$(kT)^{\frac{1}{4}}$	$(kT)^{-\frac{1}{4}}$	$(kT)^{-\frac{1}{2}}$	$(kT)^{-\frac{3}{4}}$
	$ x ^\infty$	$(kT)^1$	$(kT)^{\frac{1}{2}}$	$(kT)^0$	$(kT)^{-\frac{1}{2}}$	$(kT)^{-\frac{3}{4}}$	$(kT)^{-1}$
$U_b(x) \sim$							

Laplace transform method

$$\frac{d^2 Y(x, s)}{dx^2} + \frac{d}{dx} \left[\frac{du(x)}{dx} Y(x, s) \right] - sBY(x, s) = -B\delta(x - x_0)$$

$$Y(x, s) = \int_0^{\infty} W(x, t) e^{-st} dt$$

$$G(x, s) = \int_0^{\infty} G(x, t) e^{-st} dt$$

$$\theta = \frac{\int_0^{\infty} [P(t) - P(\infty)] dt}{P(0) - P(\infty)}$$

$$\theta = \lim_{s \rightarrow 0} \frac{s\hat{P}(s) - P(\infty)}{s[P(0) - P(\infty)]}$$

$$s\hat{P}(s) - P(\infty) = G(c, s) - G(d, s)$$

$$H(x, s) = sG(x, s) = H_0(x) + sH_1(x) + s^2H_2(x) + \dots$$

$$\tau_1(c, x_0, d) = -(H_2(d) - H_2(c));$$

$$\tau_2(c, x_0, d) = 2(H_3(d) - H_3(c));$$

$$\tau_n(c, x_0, d) = (-1)^n n! (H_{n+1}(d) - H_{n+1}(c)).$$

$$\tau_1 = B \left\{ \int_{x_0}^d e^{u(x)} \int_c^x e^{-u(y)} dy dx + \int_c^d e^{-u(y)} dy \cdot \int_d^\infty e^{u(x)} dx \right\}$$

$$\tau_2 = 2\tau_1^2 + F, \quad \tau_1 = \frac{2\pi}{\omega_c \sqrt{1-i^2}} \exp(\Delta u), \quad \Delta u \gg 1$$

A.N. Malakhov, A.L. Pankratov, Physica C **269**, 46-54 (1996).

A.N. Malakhov, Chaos **7**, 488 (1997).

A.L. Pankratov, Physics Letters A **234**, 329-335 (1997).

A.L. Pankratov, B. Spagnolo, Physical Review Letters **93**, 177001 (2004).

A.N. Malakhov, A.L. Pankratov, Adv. Chem. Phys. 121, 357-438 (2002).

Kramers' formula

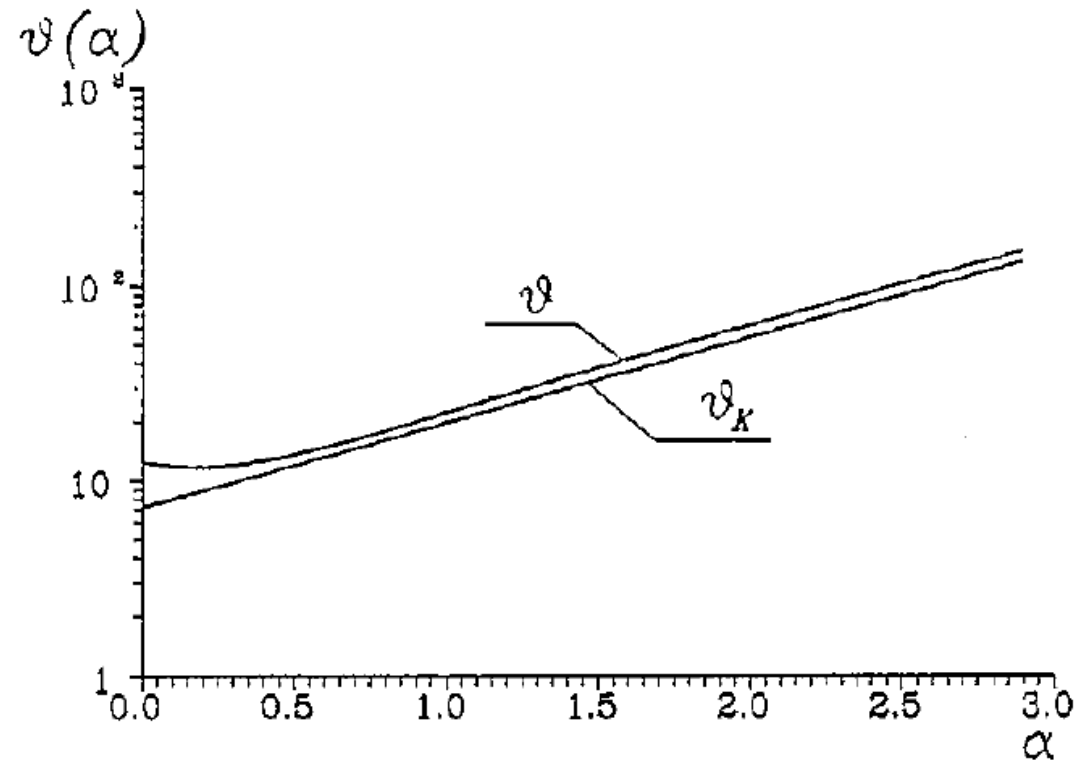
$$\tau = \frac{f(\alpha) \exp(\Delta u / \gamma)}{\sqrt{1 - i^2}}$$

$$\frac{d^2 \varphi}{dt^2} + \alpha \frac{d\varphi}{dt} = \eta - \sin \varphi + \xi(t)$$

$$\gamma = I_T / I_C \quad I_T [\mu\text{A}] = 0.042 T [\text{K}]$$

M. Büttiker, E. P. Harris, R. Landauer,
Phys. Rev. B 28, 1268 (1983).

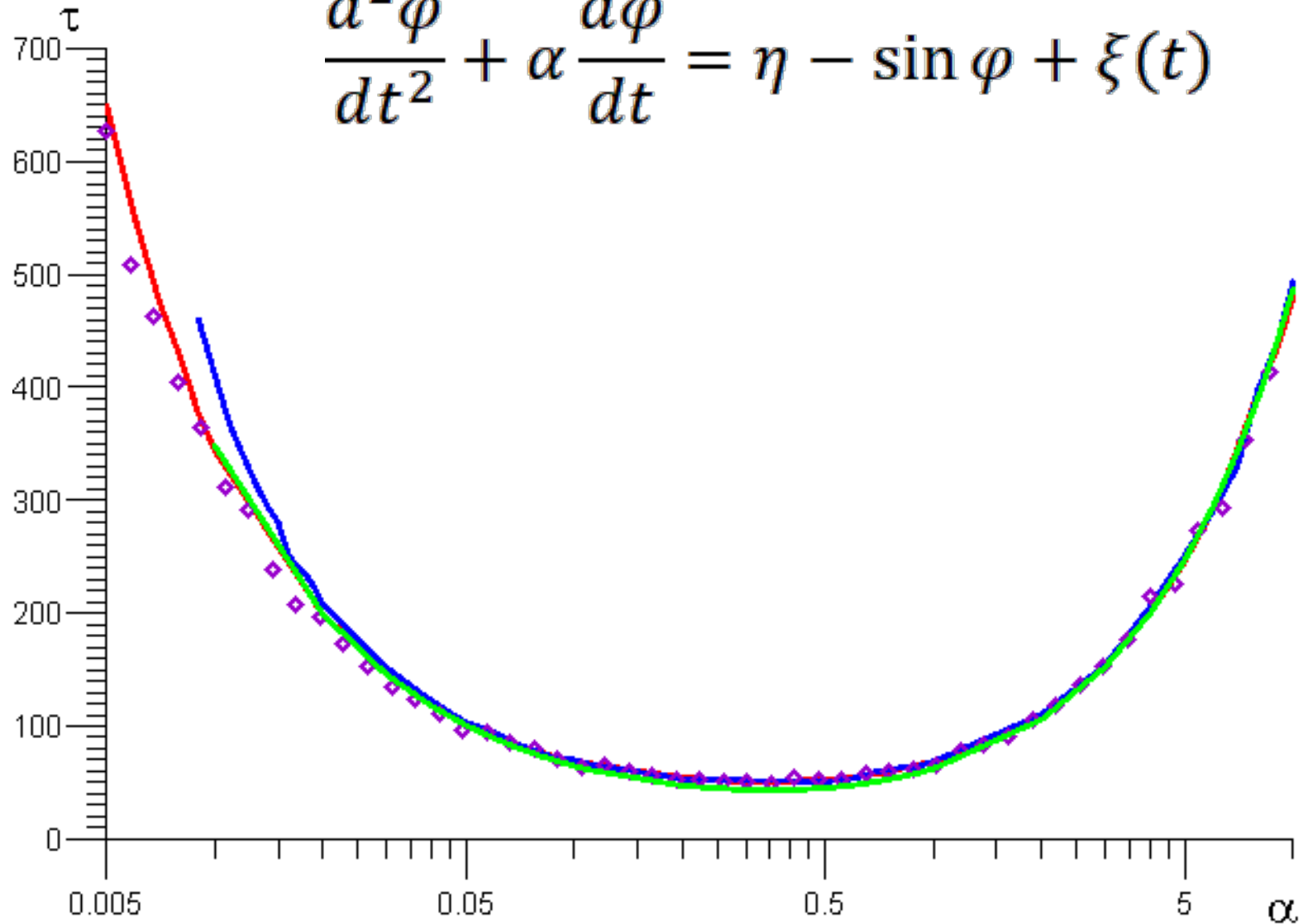
$$\tau_K = \frac{2\pi}{\omega_c \sqrt{1 - i^2}} e^\alpha,$$



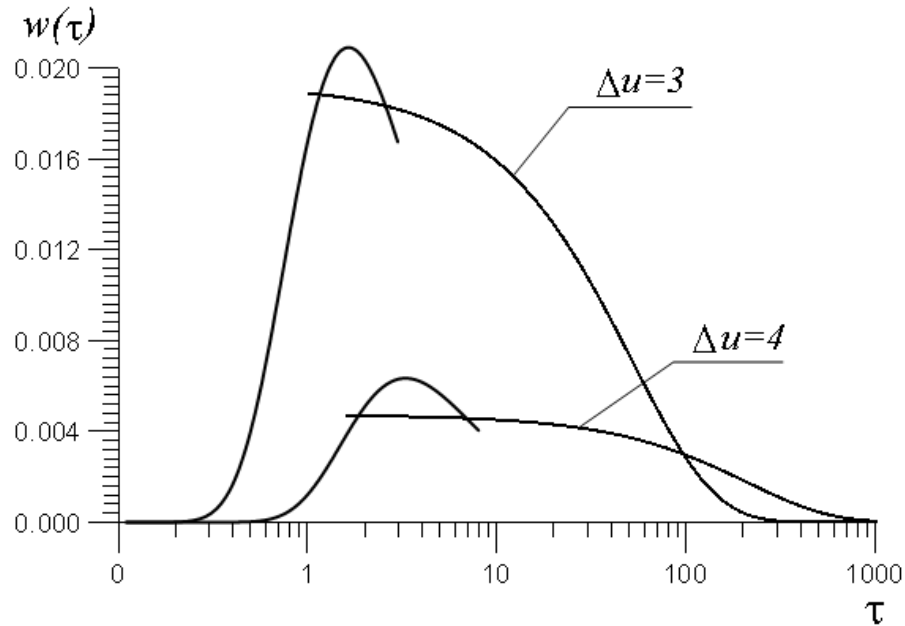
where $\alpha = \Delta u / \gamma = (2\sqrt{1 - i^2} + 2i(\arcsin i - \pi/2)) / \gamma$

Escape time for arbitrary damping α

$$\frac{d^2\varphi}{dt^2} + \alpha \frac{d\varphi}{dt} = \eta - \sin \varphi + \xi(t)$$

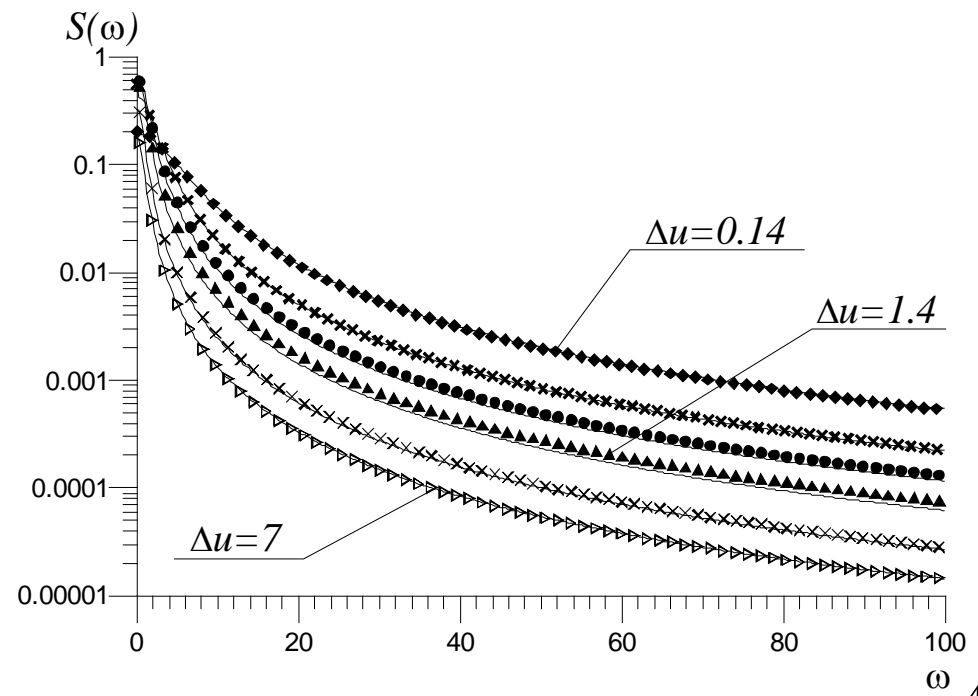
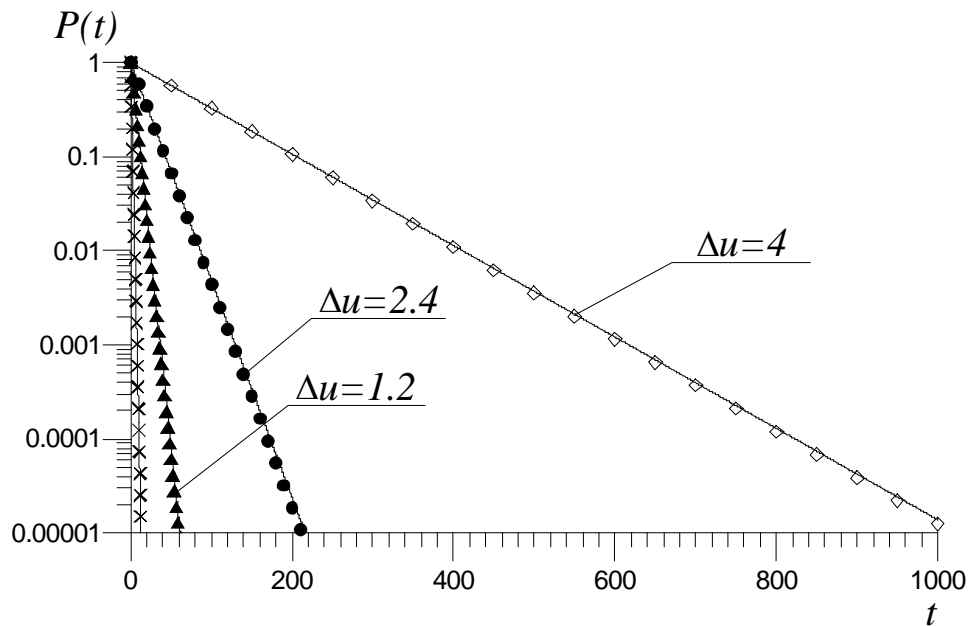


Time evolution of averages



$$\tau_n \approx n! \tau_1^n$$

$$F(t) = F_0 \exp(-t / \tau)$$

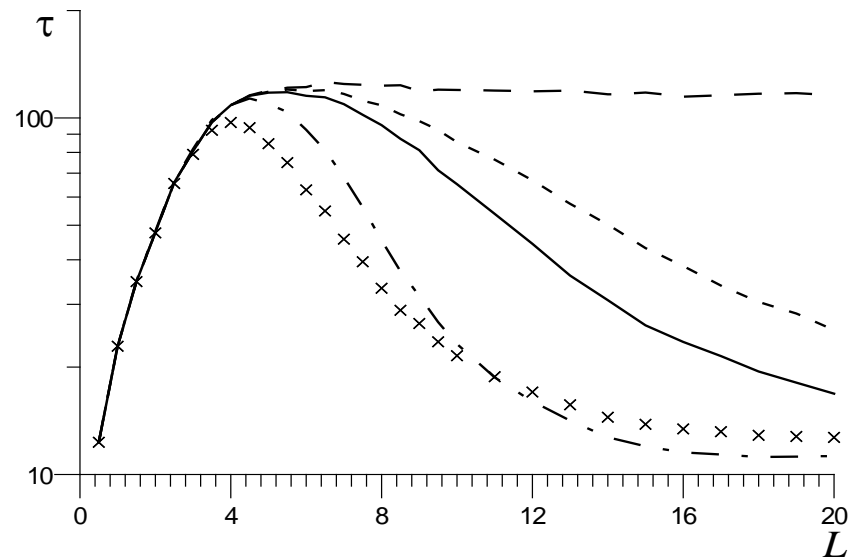
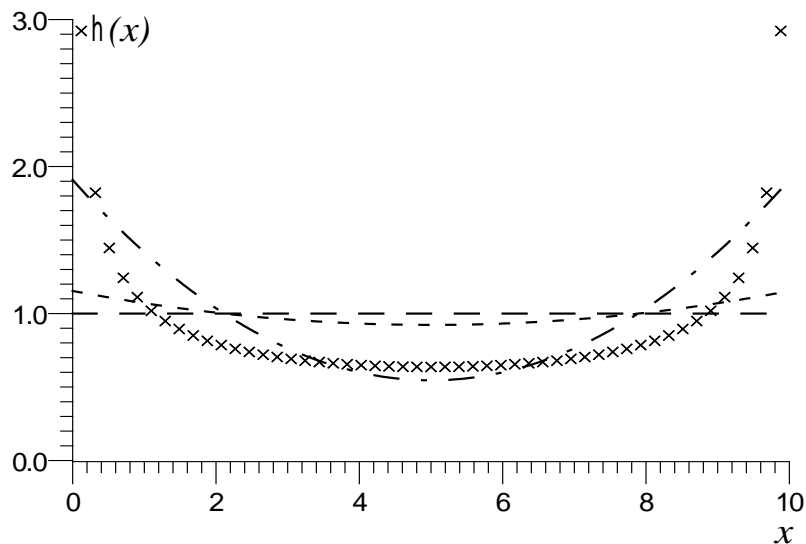
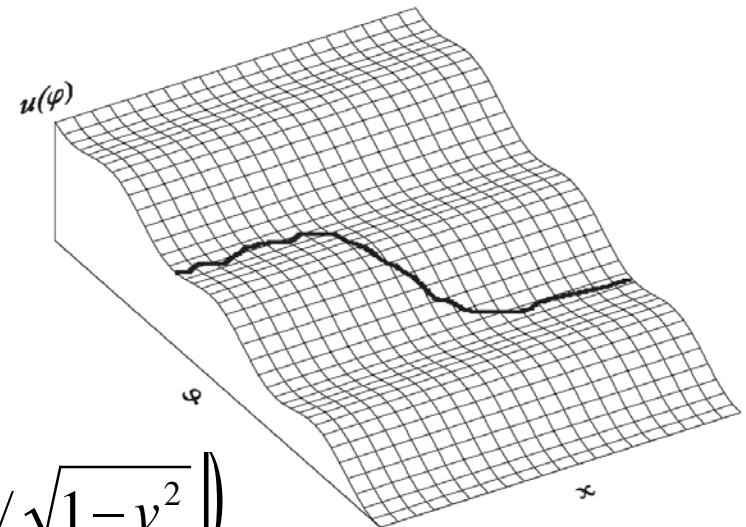


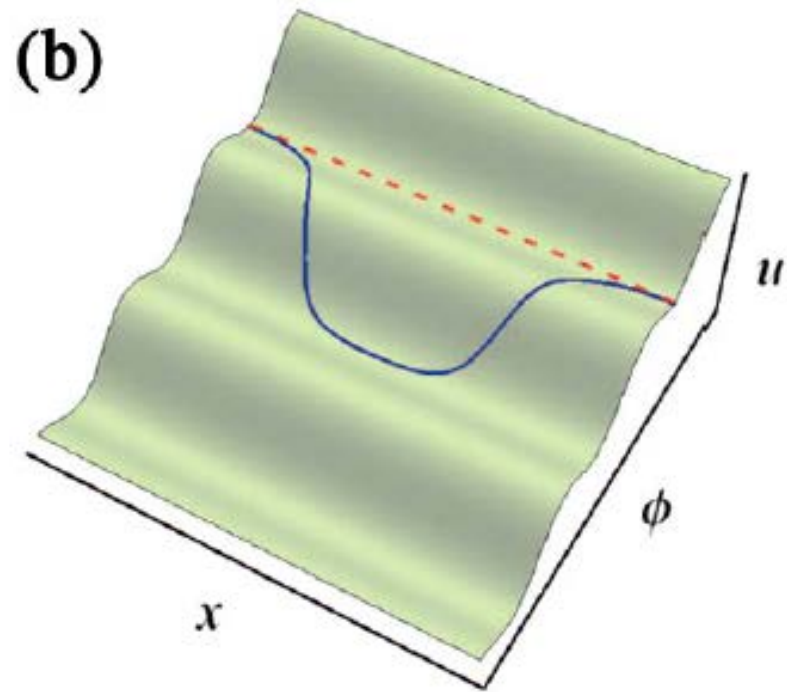
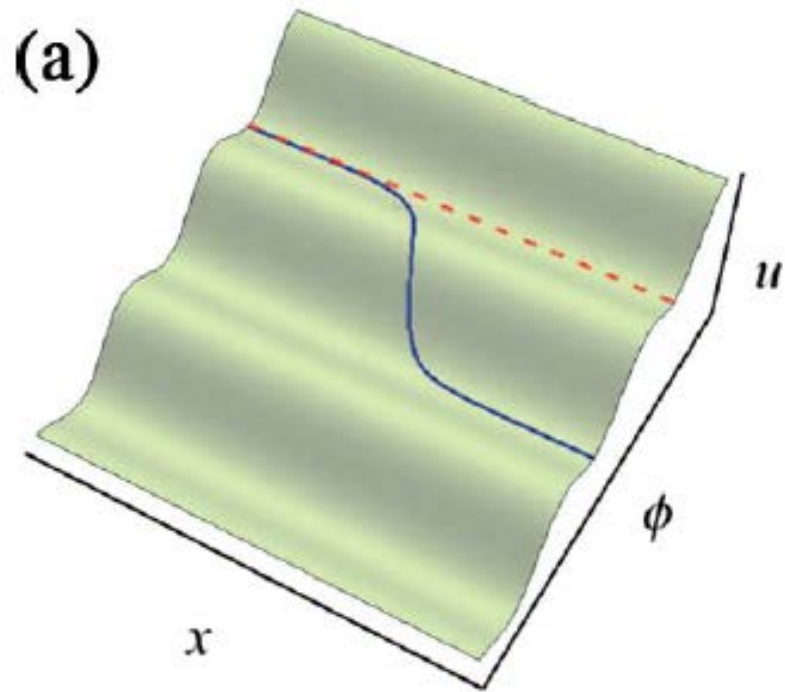
Lifetime in spatially extended systems

$$\frac{\partial^2 \varphi}{\partial t^2} + \alpha \frac{\partial \varphi}{\partial t} - \frac{\partial^2 \varphi}{\partial x^2} = \eta(x) - \sin(\varphi)$$

$$\frac{\partial \varphi(0,t)}{\partial x} = \frac{\partial \varphi(L,t)}{\partial x} = H$$

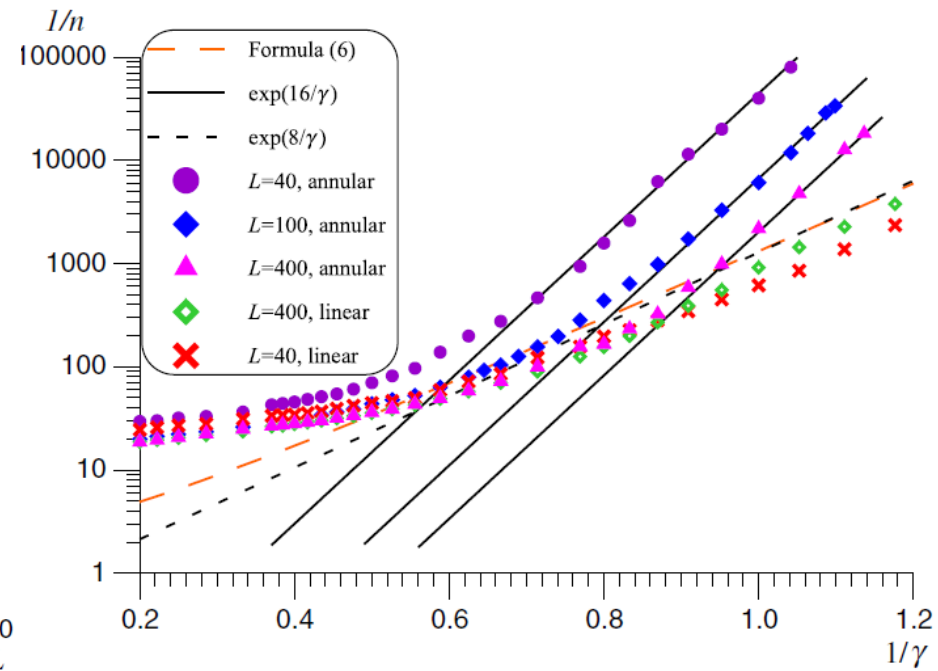
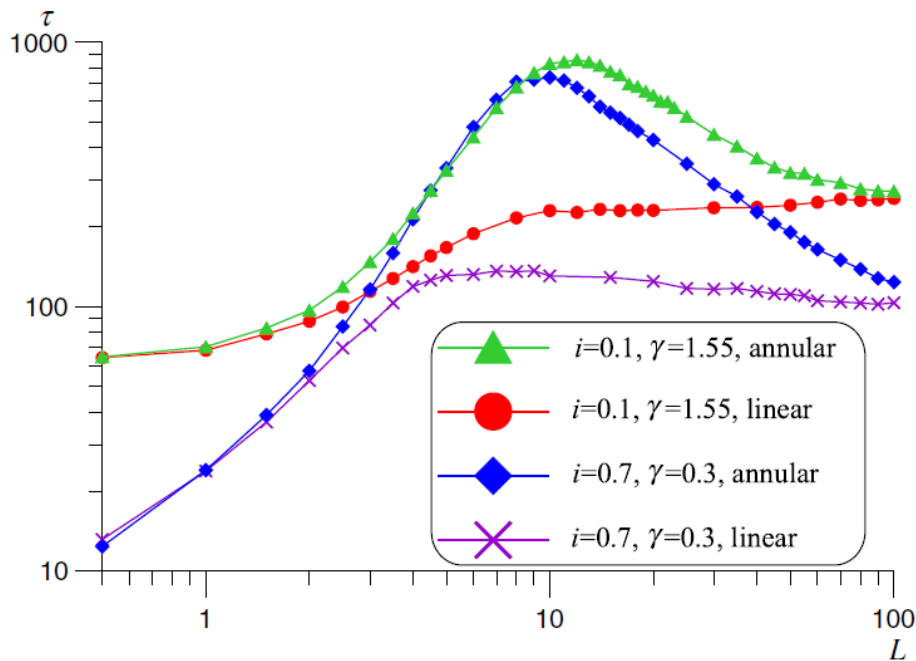
$$\varphi(x,t) = \arctg \left(\exp \left[(x - vt) / \sqrt{1 - v^2} \right] \right)$$





K.G. Fedorov, and A.L. Pankratov, Phys. Rev. Lett., 103, 260601 (2009).

Lifetime in spatially extended systems



$$n = \sqrt{2E_k / \pi \gamma} \exp(-E_k / \gamma), \quad (6)$$

M. Buttiker, and R. Landauer, Phys. Rev. A, 23, 1397 (1981).

M. Buttiker, and T. Christen, Phys. Rev. Lett. 75, 1895 (1995).

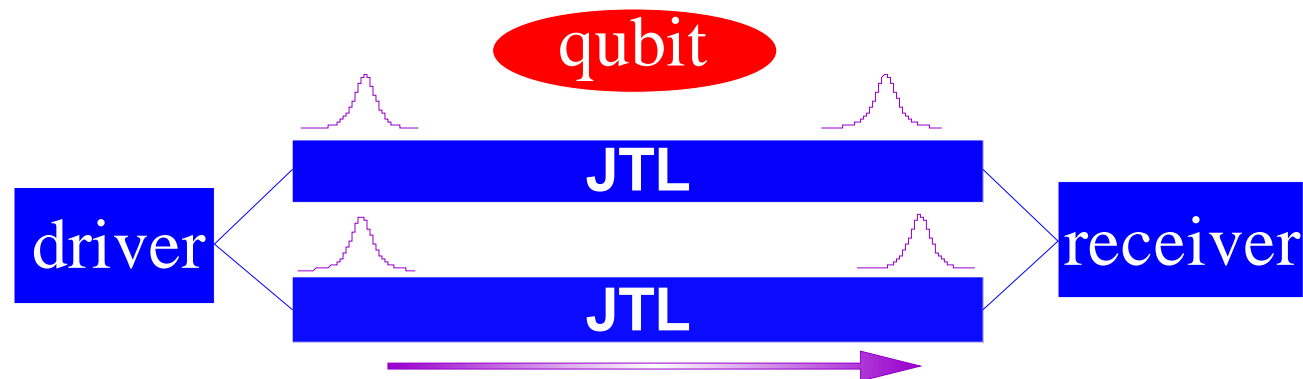
Sine-Gordon equation

$$\frac{\partial^2 \phi}{\partial t^2} + \alpha \frac{\partial \phi}{\partial t} - \frac{\partial^2 \phi}{\partial x^2} = i - \sin(\phi) + i_F(x, t)$$

$$\phi(0, t)_x + r_L c_L \phi(0, t)_{xt} - c_L \phi(0, t)_{tt} = \Gamma$$

$$\phi(L, t)_x + r_R c_R \phi(L, t)_{xt} + c_R \phi(L, t)_{tt} = \Gamma$$

and ballistic readout of qubits



Jitter in long Josephson junctions



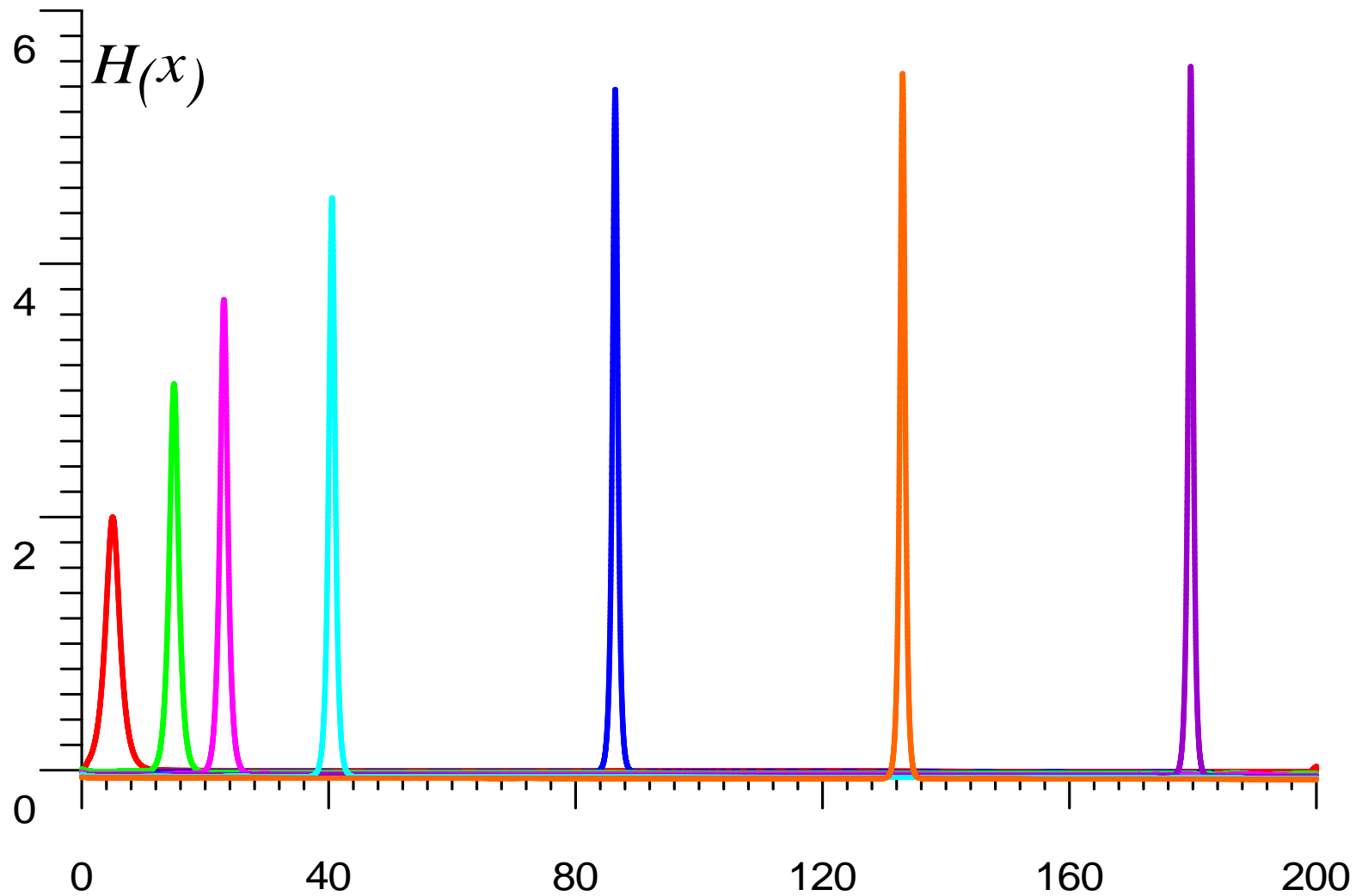
$\sigma \sim \sqrt{L}$ for a long junction, $\alpha \ll 1$

Arkady Fedorov, Alexander Shnirman, Gerd Schön and Anna Kidiyarova-Shevchenko,
Phys. Rev. B, 75, 224504 (2007).

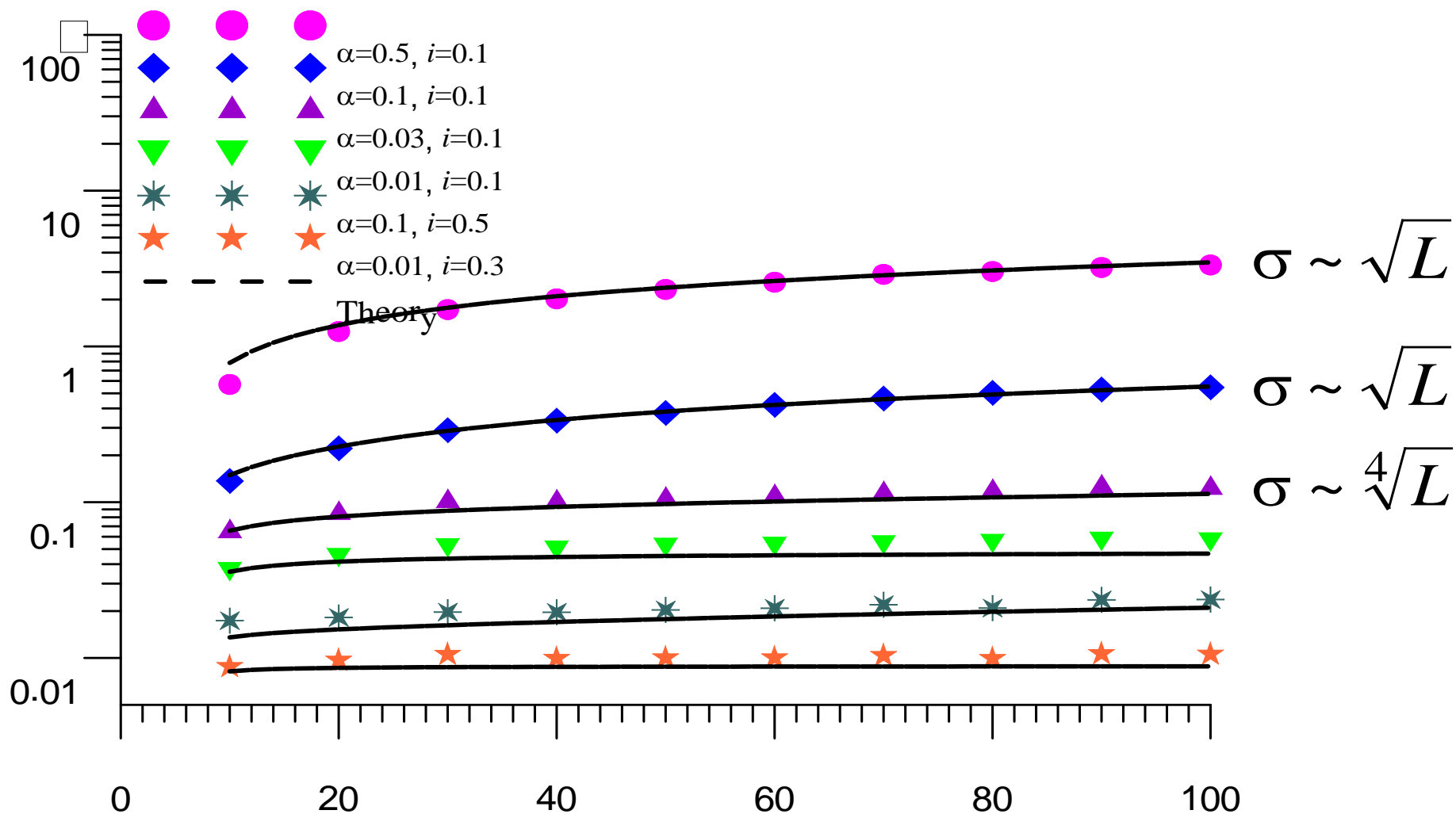
$\sigma \sim \sqrt{N}$ for a chain of N junctions, $\alpha > 1$

1. H. Terai, Z. Wang, Y. Hishimoto, S. Yorozu, A. Fujimaki, and N. Yoshikawa,
Appl. Phys. Lett. 84, 2133 (2004).
2. H. Terai et al. IEEE Trans. Appl. Supercond., 15, 364 (2005).

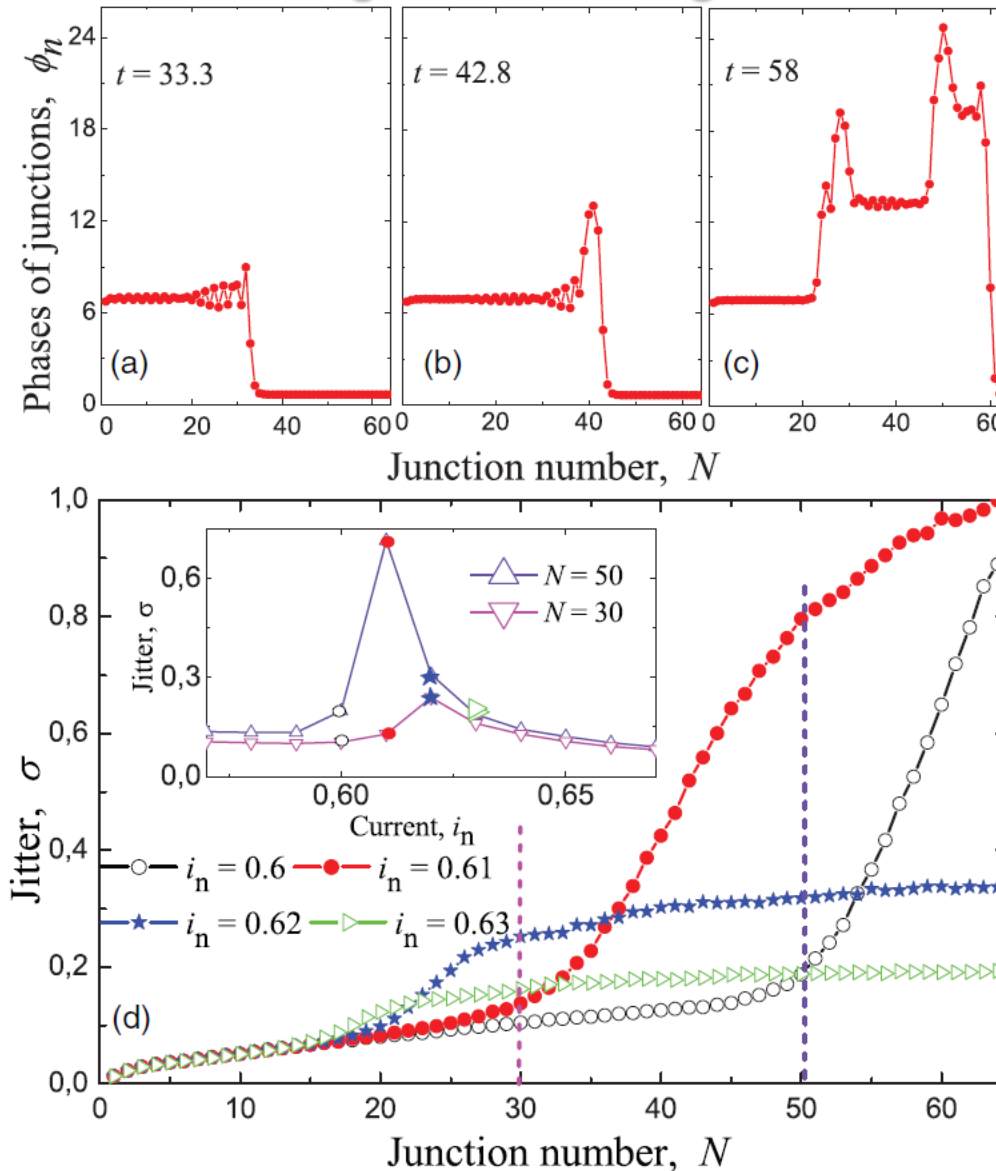
Soliton dynamics, $\alpha=0.03$



Dependence of jitter vs junction length



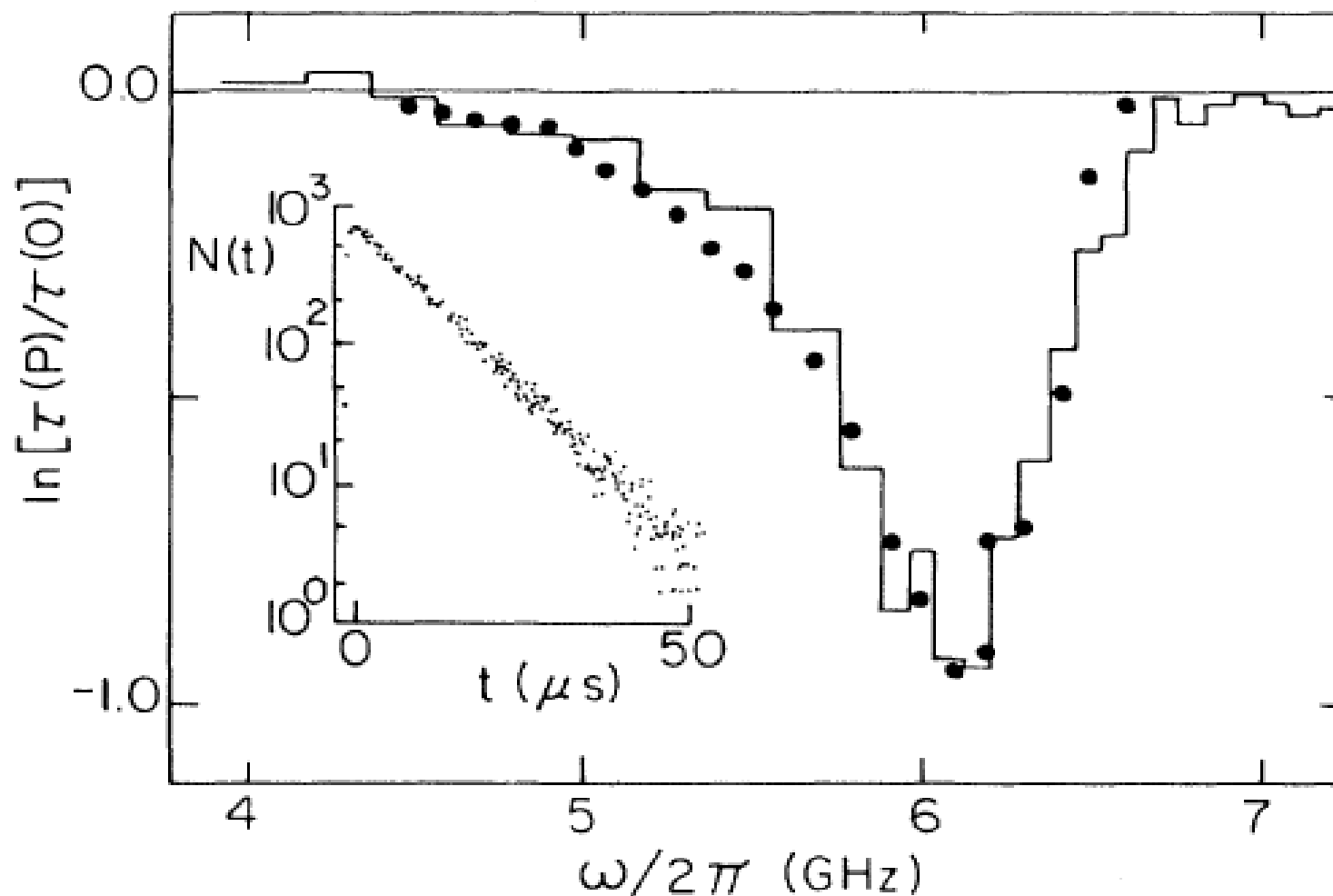
Dependence of jitter vs junction length



Resonant Activation from the Zero-Voltage State of a Current-Biased Josephson Junction

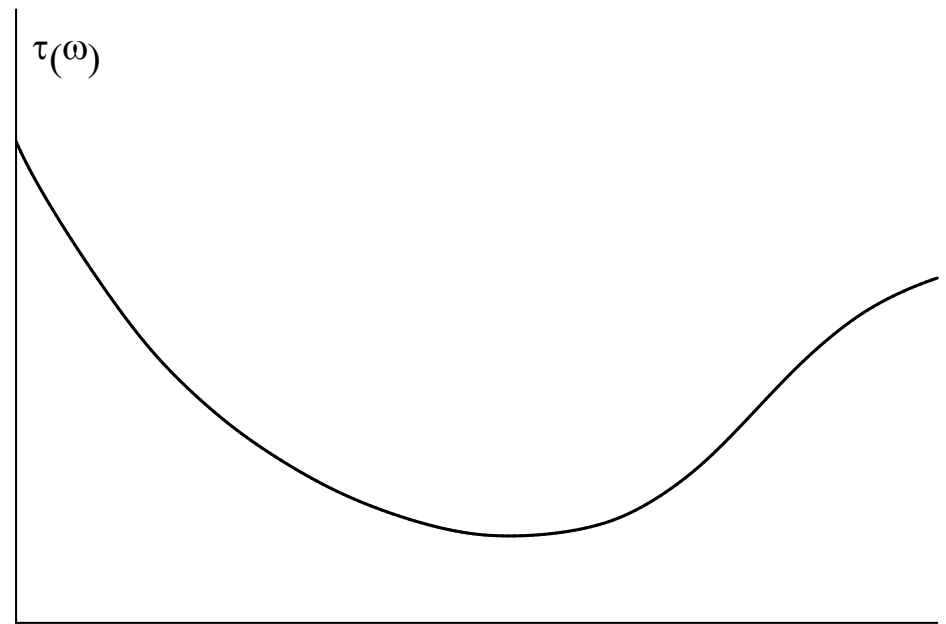
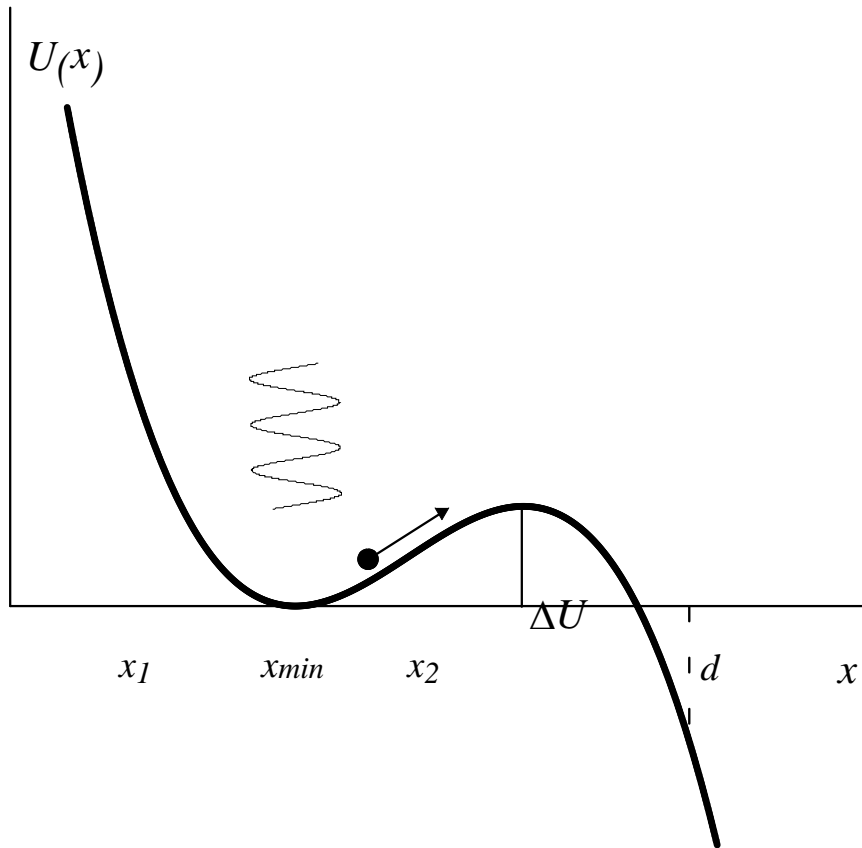
Michel H. Devoret,^(a) John M. Martinis, Daniel Esteve,^(a) and John Clarke

Department of Physics, University of California, Berkeley, California 94720, and Materials and Molecular Research Division, Lawrence Berkeley Laboratory, Berkeley, California 94720



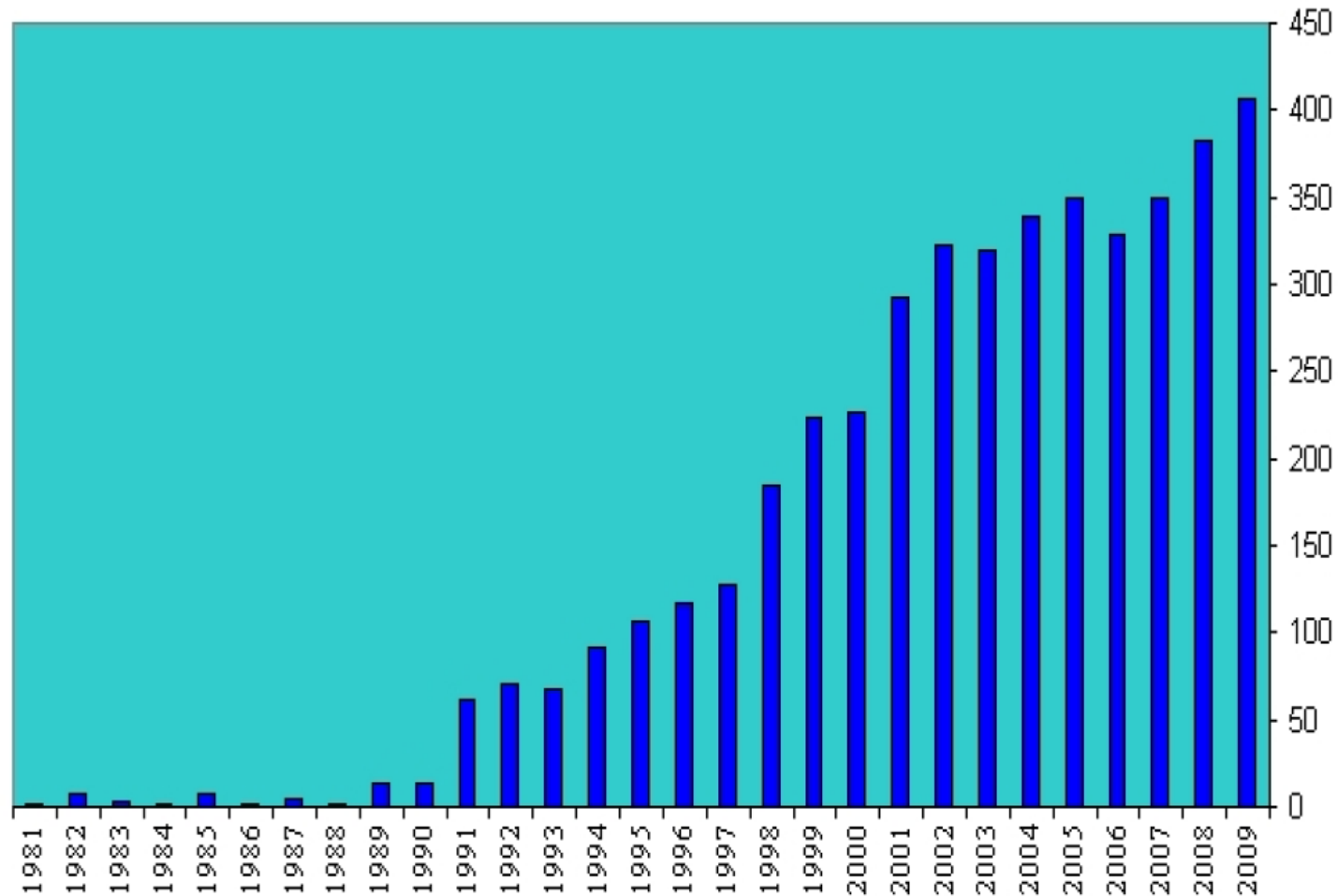
Resonant activation

$$\frac{m}{h} \frac{d^2 x(t)}{dt^2} + \frac{dx(t)}{dt} = -\frac{1}{h} \left(\frac{dU(x)}{dx} + A \sin(\omega t) \right) + \xi(t)$$



P. Jung, Physics Reports **234**, 175-295 (1993).

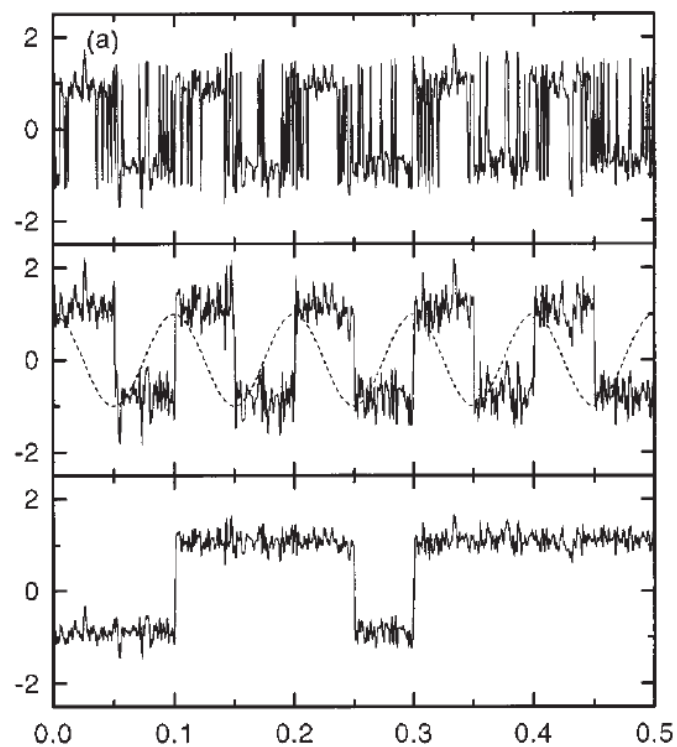
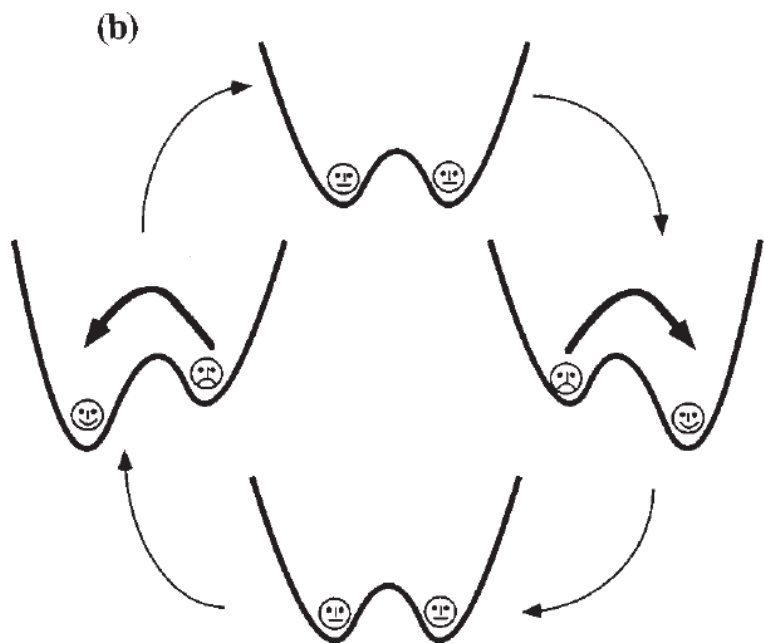
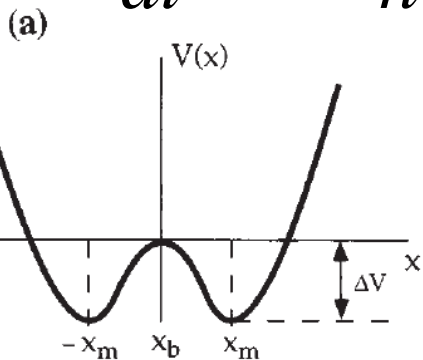
Stochastic resonance



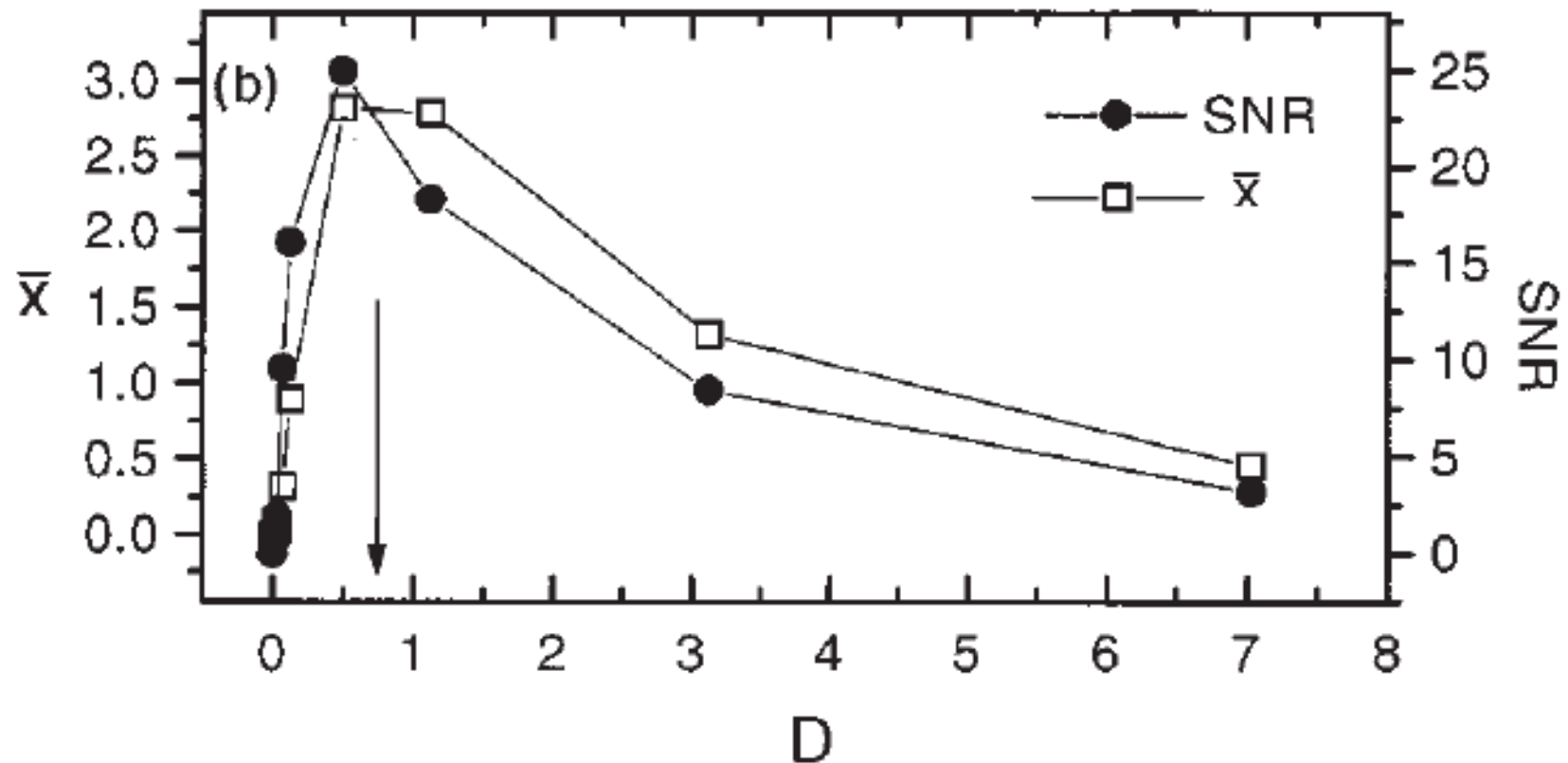
L. Gammaitoni, P. Hänggi, P. Jung and F. Marchesoni, Rev. Mod. Phys. 70, 223-287 (1998).
В.С. Анищенко, А.Б. Нейман, Ф. Мосс, Л. Шиманский-Гайер, УФН, 169, №1, 7 (1999).
Th. Wellens, Y. Shatokhin and A. Buchleitner, Rep. Progr. Phys. 67, 45-105 (2004).

Stochastic resonance

$$\frac{dx(t)}{dt} = -\frac{1}{h} \left(\frac{dU(x)}{dx} + A \sin(\omega t) \right) + \xi(t)$$



Stochastic resonance



It is important to note that the variation of the angular frequency ω at a fixed value of the noise intensity D does not yield a resonance-like behavior of the response amplitude. This behavior is immediately evident from Eq. (2.7a) and also from numerical studies (for those who don't trust the theory).

L. Gammaitoni, P. Hänggi, P. Jung and F. Marchesoni, [Rev. Mod. Phys.](#) 70, 223-287 (1998).

Adiabatic approximation

$$P(x_0, t) = \exp \left\{ - \int_0^t \frac{1}{\tau_K(t')} dt' \right\} \quad P(x_0, t) = \frac{\exp \left\{ - \int_0^t [1/\tau_p(t')] dt' \right\} + 1}{2}$$

Standard adiabatic approximation

$$\tau_K = \tau_0 (kT) e^{\Delta U/kT}$$

Modified adiabatic approximation

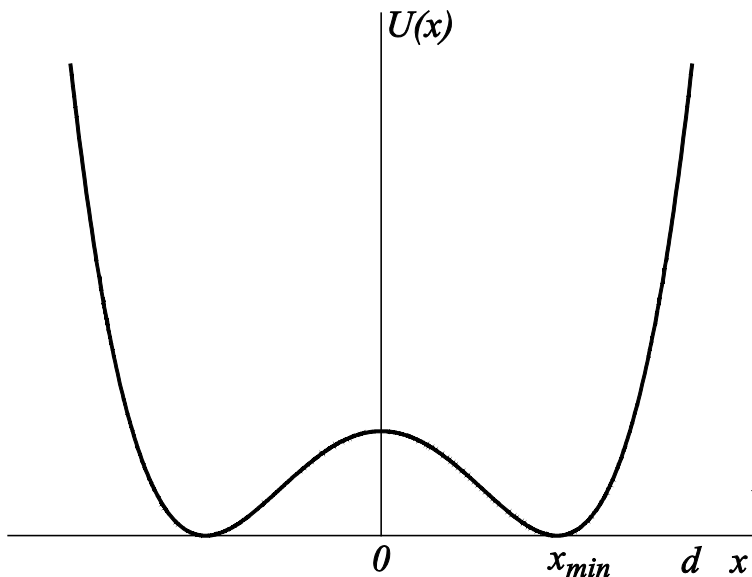
$$\tau_p(x_0) = T(x_0, 0) = B \int_{x_0}^0 e^{\varphi(y)} \int_{-\infty}^y e^{-\varphi(x)} dx dy$$

A.L. Pankratov, [Physics Letters A](#) **234**, 329 (1997).

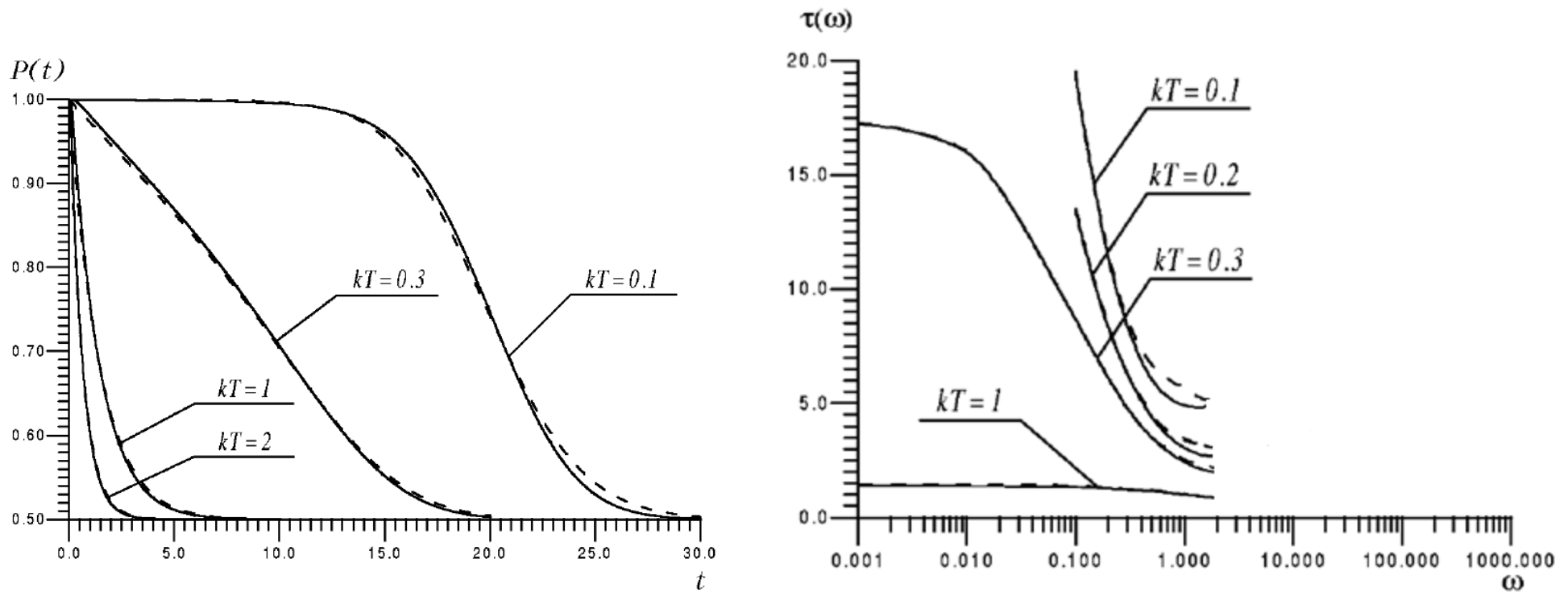
$$\tau_p = B \left\{ \int_{x_0}^d e^{u(x)} \int_c^x e^{-u(y)} dy dx + \int_c^d e^{-u(y)} dy \cdot \int_d^{\infty} e^{u(x)} dx \right\}$$

$$U(x) = bx^4 - a(t)x^2, \quad a(t) = 1 + \cos(\omega t)$$

A.L. Pankratov, M. Salerno, [Phys. Rev. E](#) **61**, 1206 (2000).



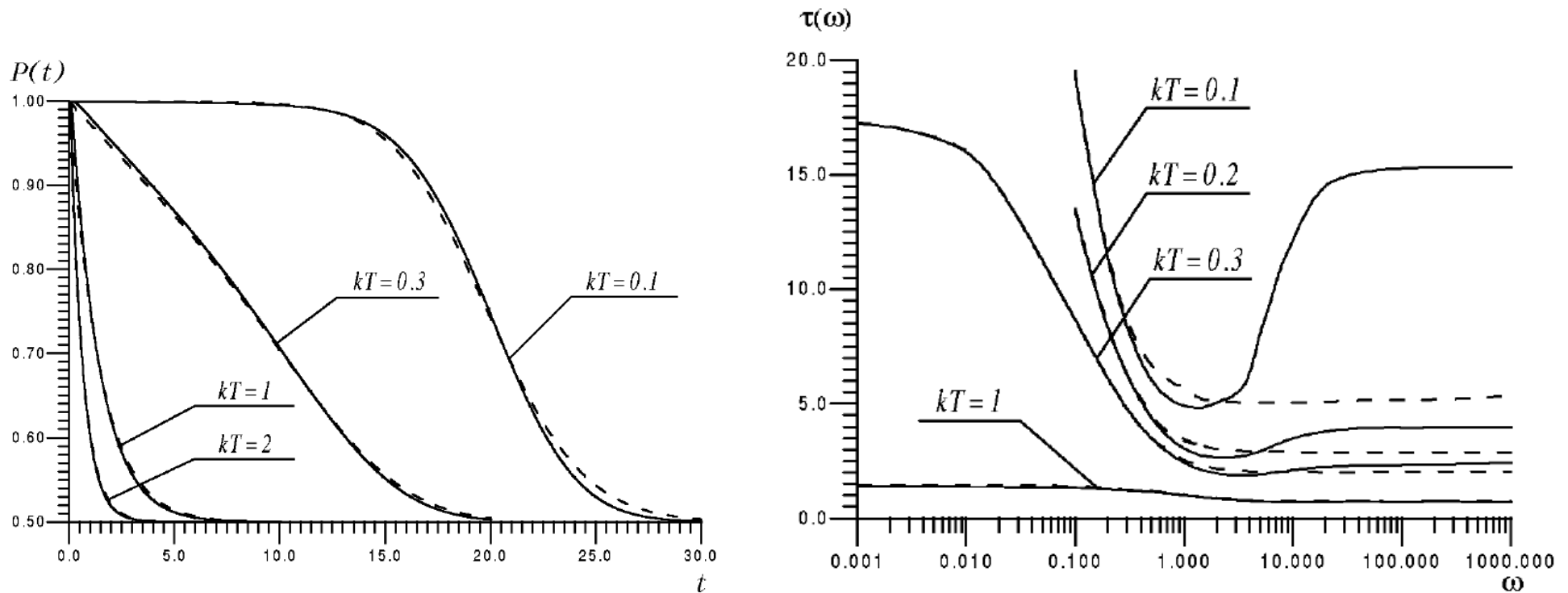
Parametric stochastic resonance



It is important to note that the variation of the angular frequency ω at a fixed value of the noise intensity D does not yield a resonance-like behavior of the response amplitude. This behavior is immediately evident from Eq. (2.7a) and also from numerical studies (for those who don't trust the theory).

L. Gammaitoni, P. Hänggi, P. Jung and F. Marchesoni, [Rev. Mod. Phys.](#) 70, 223-287 (1998).

Parametric stochastic resonance

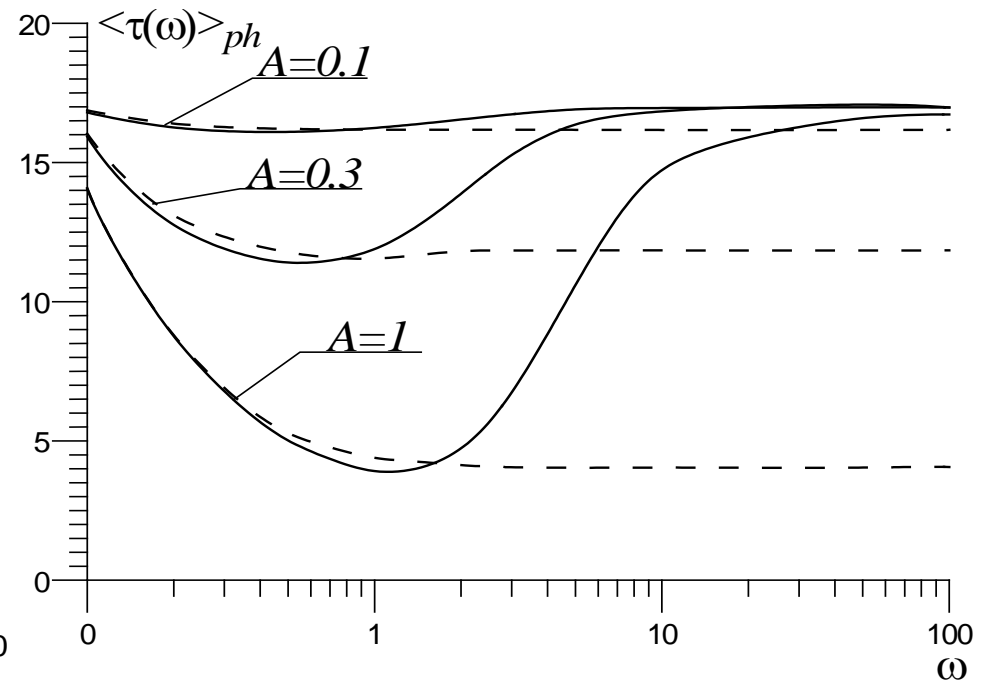
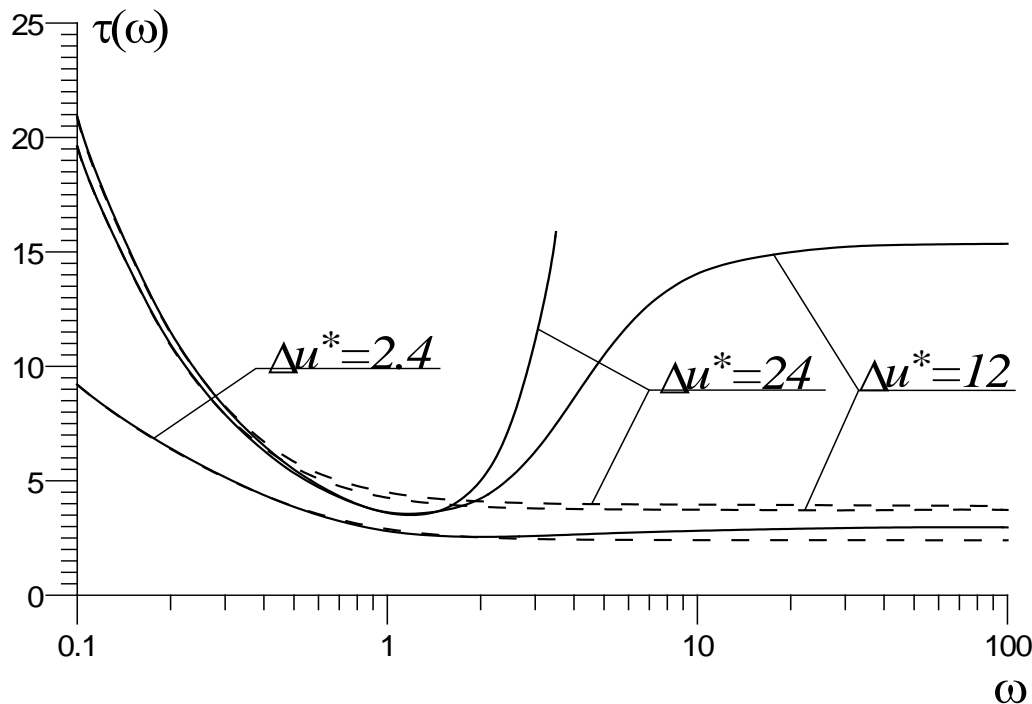


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A.L. Pankratov, M. Salerno, [Phys. Rev. E](#) **61**, 1206 (2000).

Resonant activation?

$$\frac{dx(t)}{dt} = -\frac{1}{h} \left(\frac{dU(x)}{dx} + A \sin(\omega t) \right) + \xi(t)$$

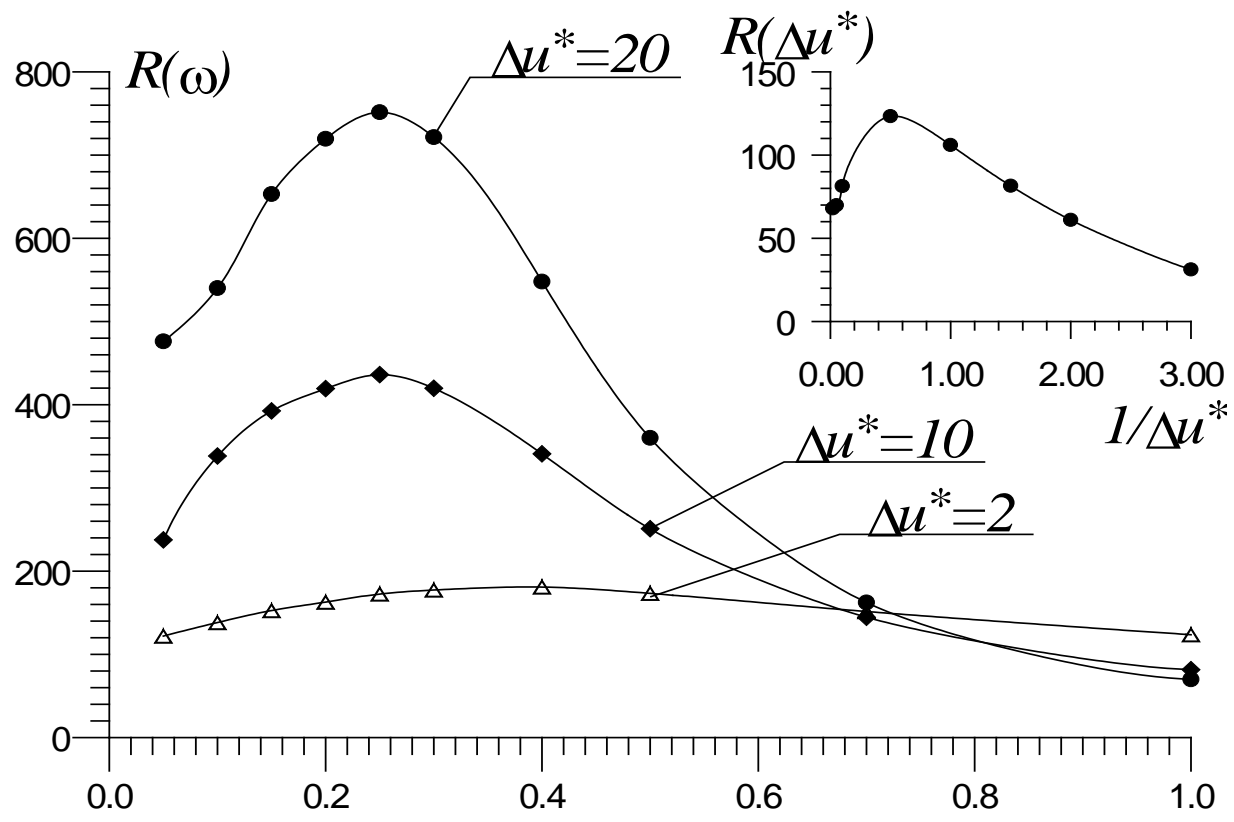


A.L. Pankratov, M. Salerno, Physics Letters A **273**, 162-166 (2000).

Suppression of noise by driving

$$\ddot{x} = x - x^3 + A \sin(\omega t + \psi) + \xi(t)$$

$$R(\omega) = \frac{1}{S_N(\omega)} \lim_{\Delta\Omega \rightarrow 0} \int_{\omega - \Delta\Omega}^{\omega + \Delta\Omega} S(\omega) d\omega$$



Suppression of noise by driving

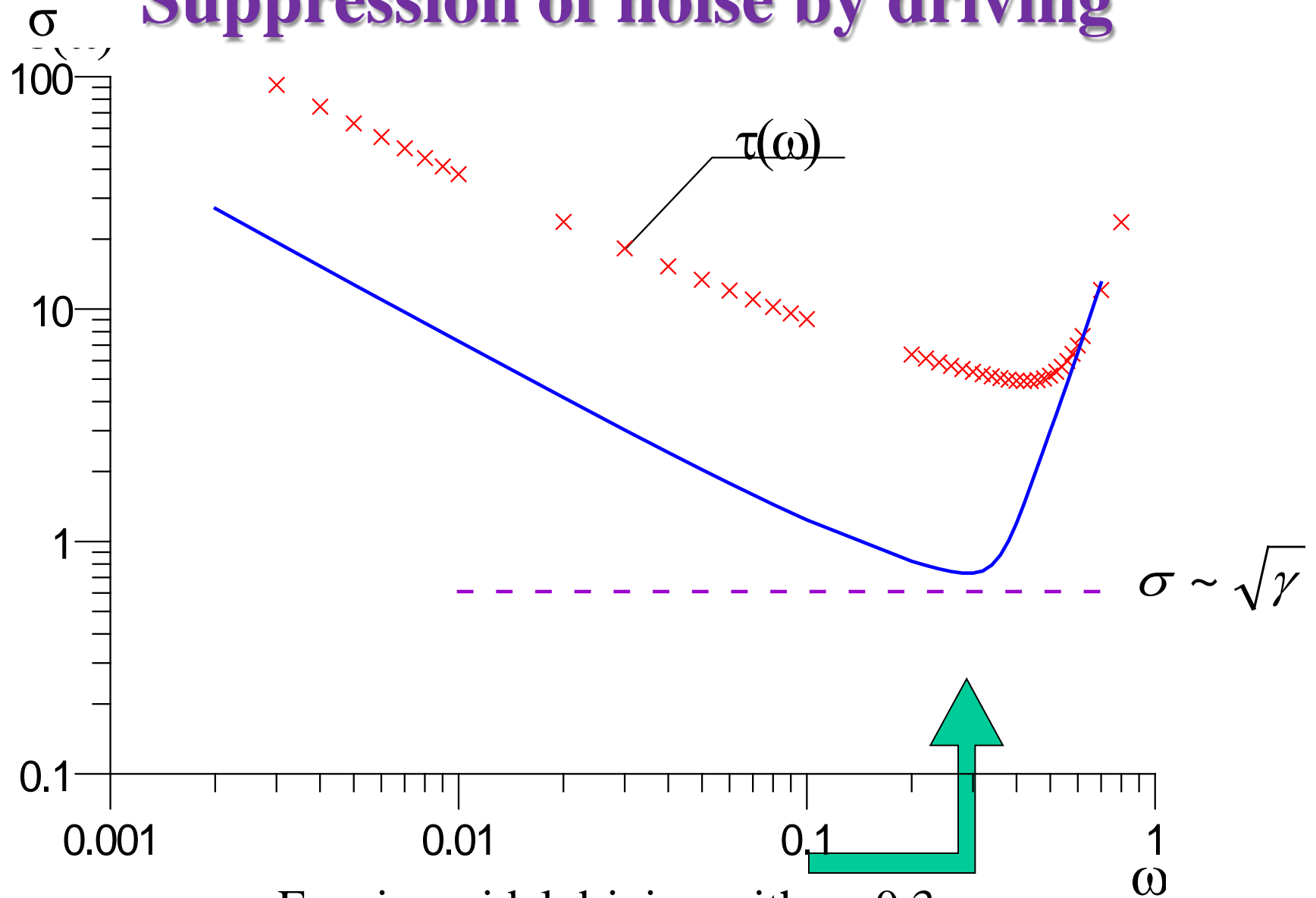
A.L. Pankratov, B. Spagnolo, Physical Review Letters **93**, 177001 (2004).

$$\frac{d\varphi}{dt} = \sin(\varphi) - i(t) + i_F(t)$$

$$\tau = \langle t \rangle = \int_0^{\infty} t w(t) dt, \quad \sigma = \sqrt{\langle t^2 \rangle - \langle t \rangle^2}$$

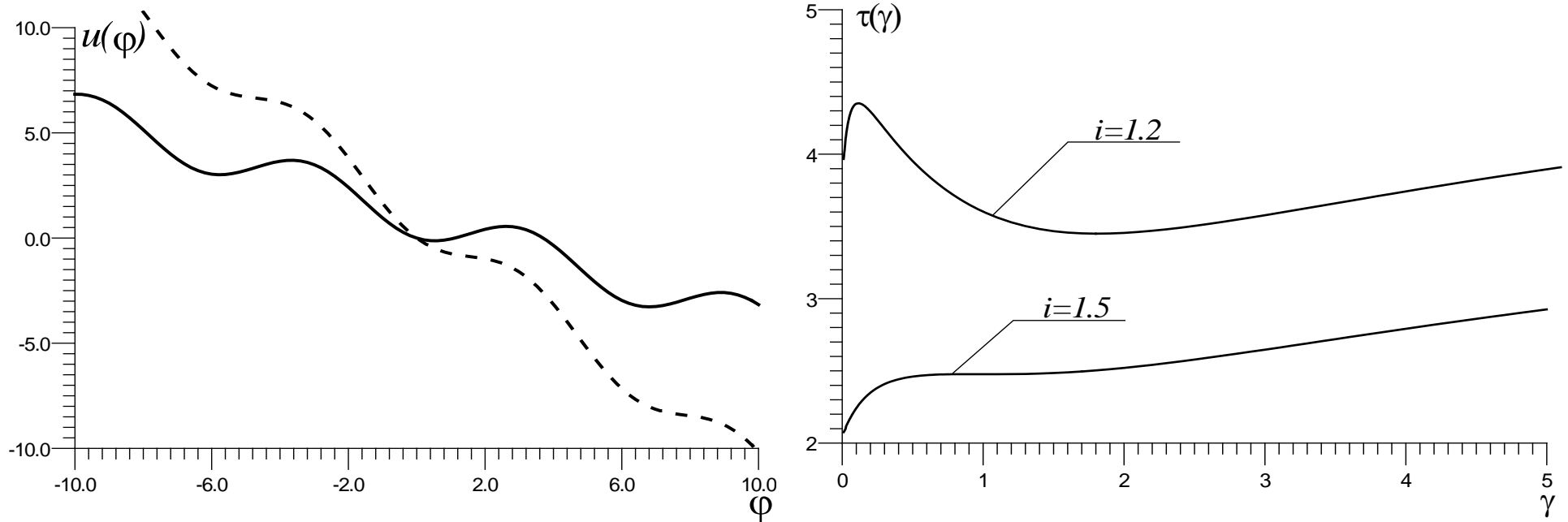
$$\begin{aligned} \tau = \frac{1}{\omega_c} & \left\{ \frac{2}{\sqrt{i^2 - 1}} \arctan \left(\frac{i \tan(y/2) - 1}{\sqrt{i^2 - 1}} \right) \right|_{y=x_0}^{y=d} + \\ & + \gamma \left[\frac{1}{2(i - \sin d)^2} + \frac{1}{2(i - \sin x_0)^2} \right] + \\ & + \gamma^2 \int_{x_0}^d \left[\frac{3 \cos^2 y}{(i - \sin y)^5} - \frac{\sin y}{(i - \sin y)^4} \right] dy + \dots \Bigg\} \end{aligned}$$

Suppression of noise by driving



For sinusoidal driving with $\omega \sim 0.3$
SD for meander driving is nearly reached

Noise delayed switching



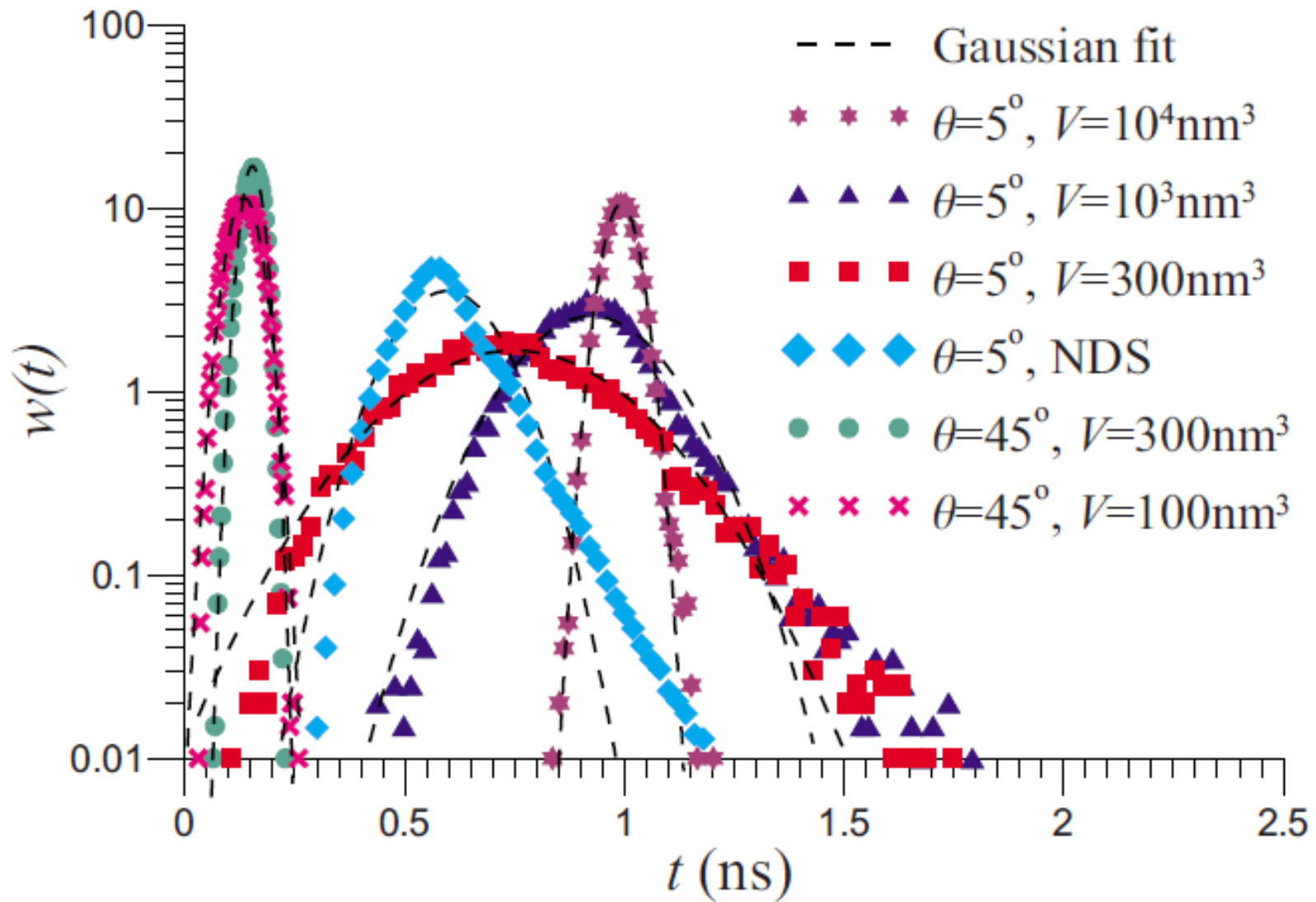
Rylyakov A.V., Likharev K.K., **Pulse jitter and timing errors in RSFQ circuits**, IEEE Trans. Appl. Supercond. Vol. 9, 2 - P. 3539-3544 (1999).

A.N. Malakhov, and A.L. Pankratov, Physica C, 269, 46 (1996).

A.L. Pankratov and B. Spagnolo, Phys. Rev. Lett., 93, 177001 (2004).

V.K. Semenov and A. Inamdar, IEEE Trans. Appl. Supercond., 15, 435 (2005).

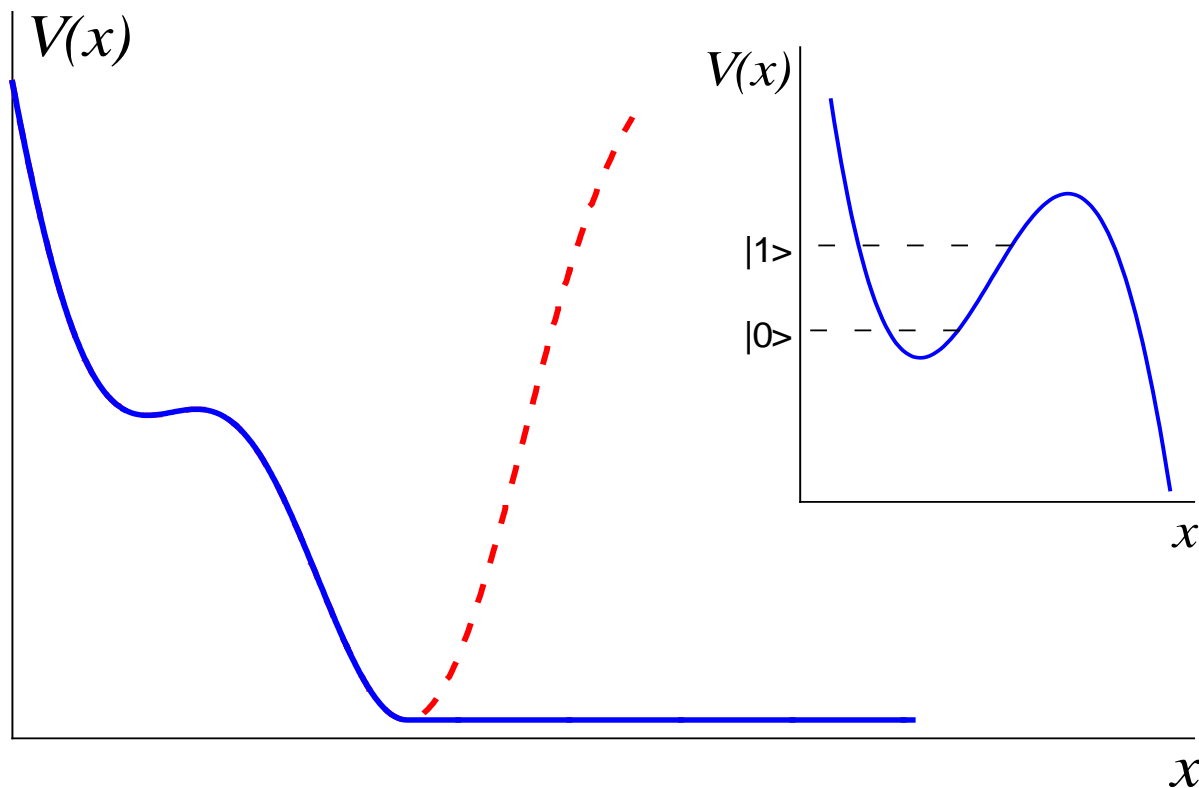
A.V. Gordeeva and A.L. Pankratov, Appl. Phys. Lett., 88, 022505 (2006).



A.L. Pankratov, S.N. Vdovichev, I.M. Nefedov, Physical Review B, 78, 052401 (2008).
 A.A. Smirnov, A.L. Pankratov, Physical Review B, 82, 132405 (2010).
 A.L. Pankratov, S.N. Vdovichev, I.M. Nefedov, I.R. Karetnikova, Journal of Applied Physics, 109, 033906 (2011).

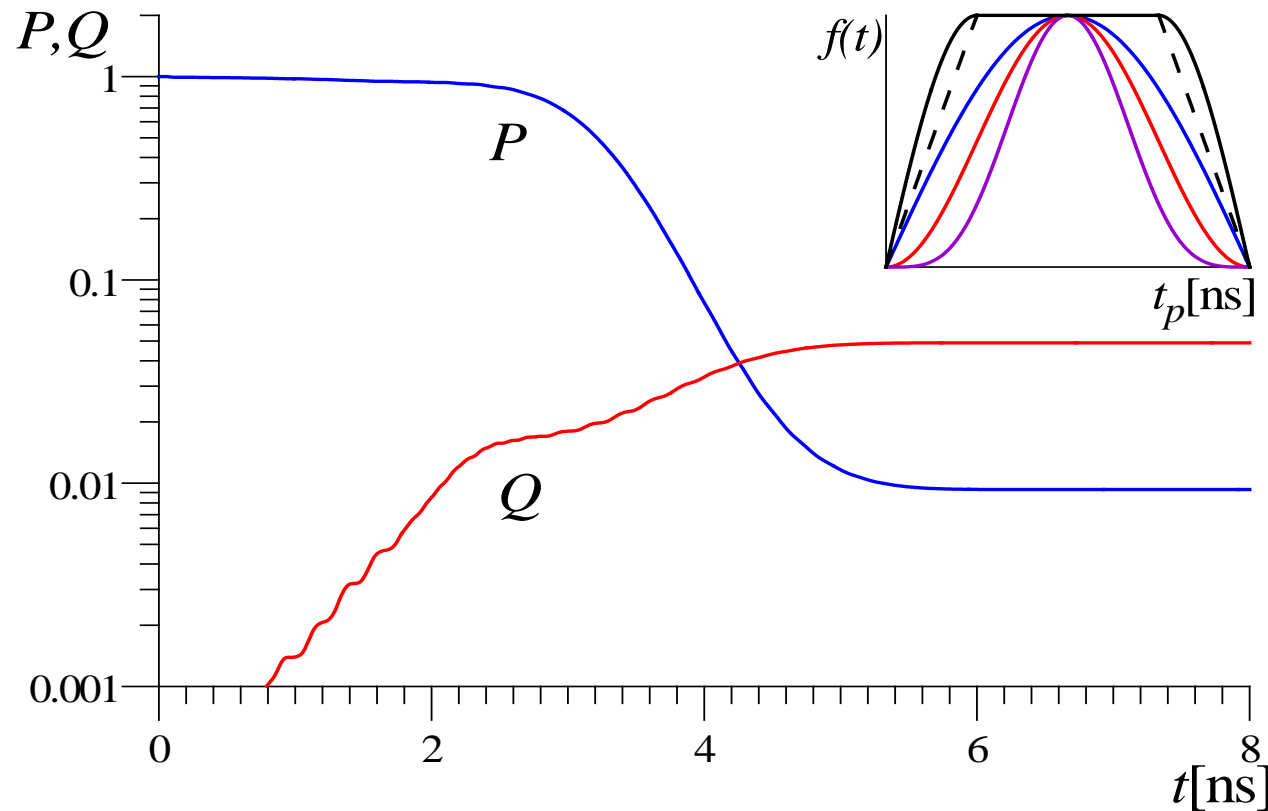
Optimal fast single pulse readout of qubits

$$i\hbar \frac{\partial \Psi(x,t)}{\partial t} = -\frac{\hbar^2}{2m} \frac{\partial^2 \Psi(x,t)}{\partial x^2} + V(x,t) \Psi(x,t)$$



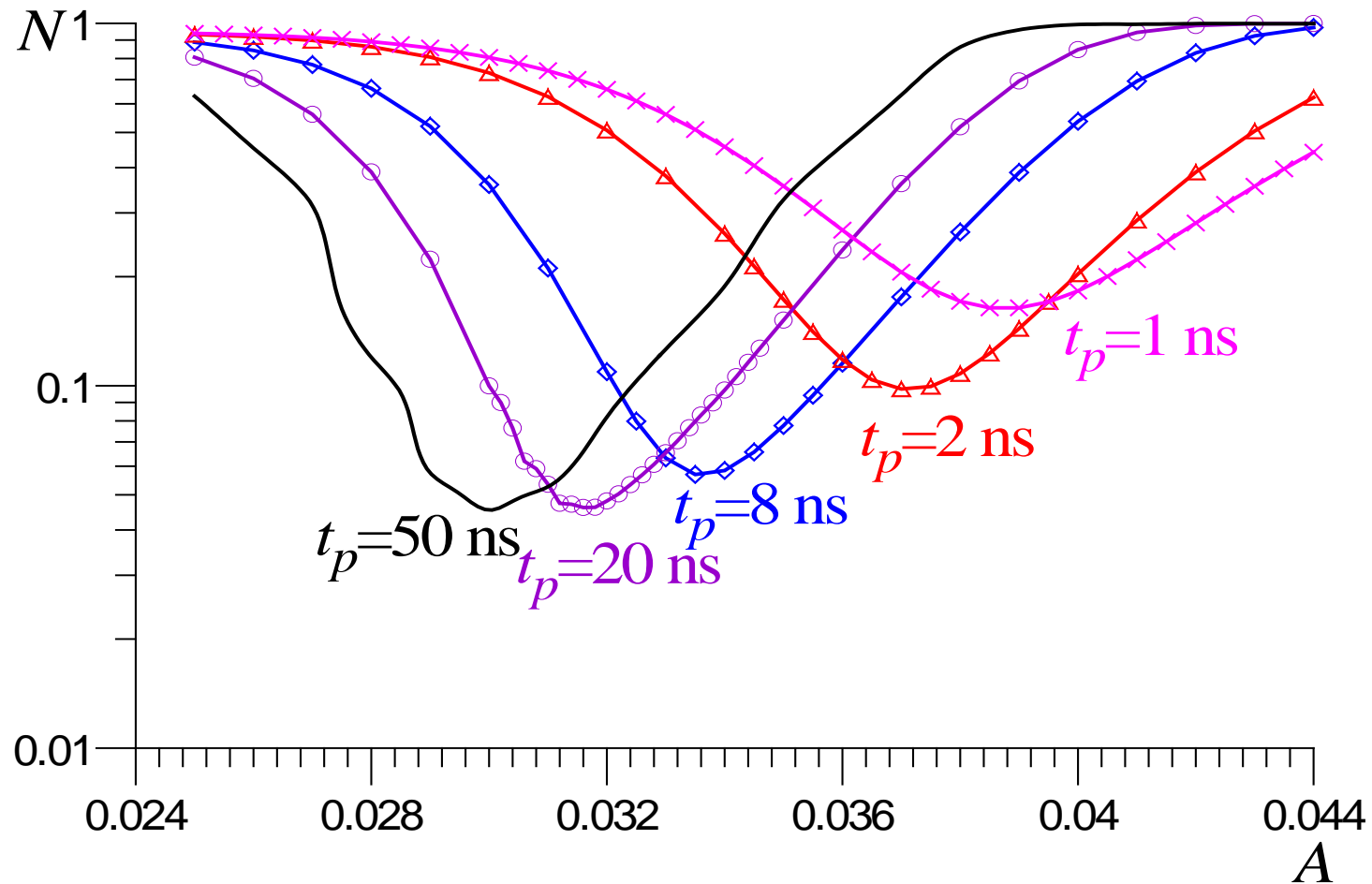
Probability evolution

$$N = P(t_p) + Q(t_p) = P_{10} + P_{01}, \quad F = 1 - N$$

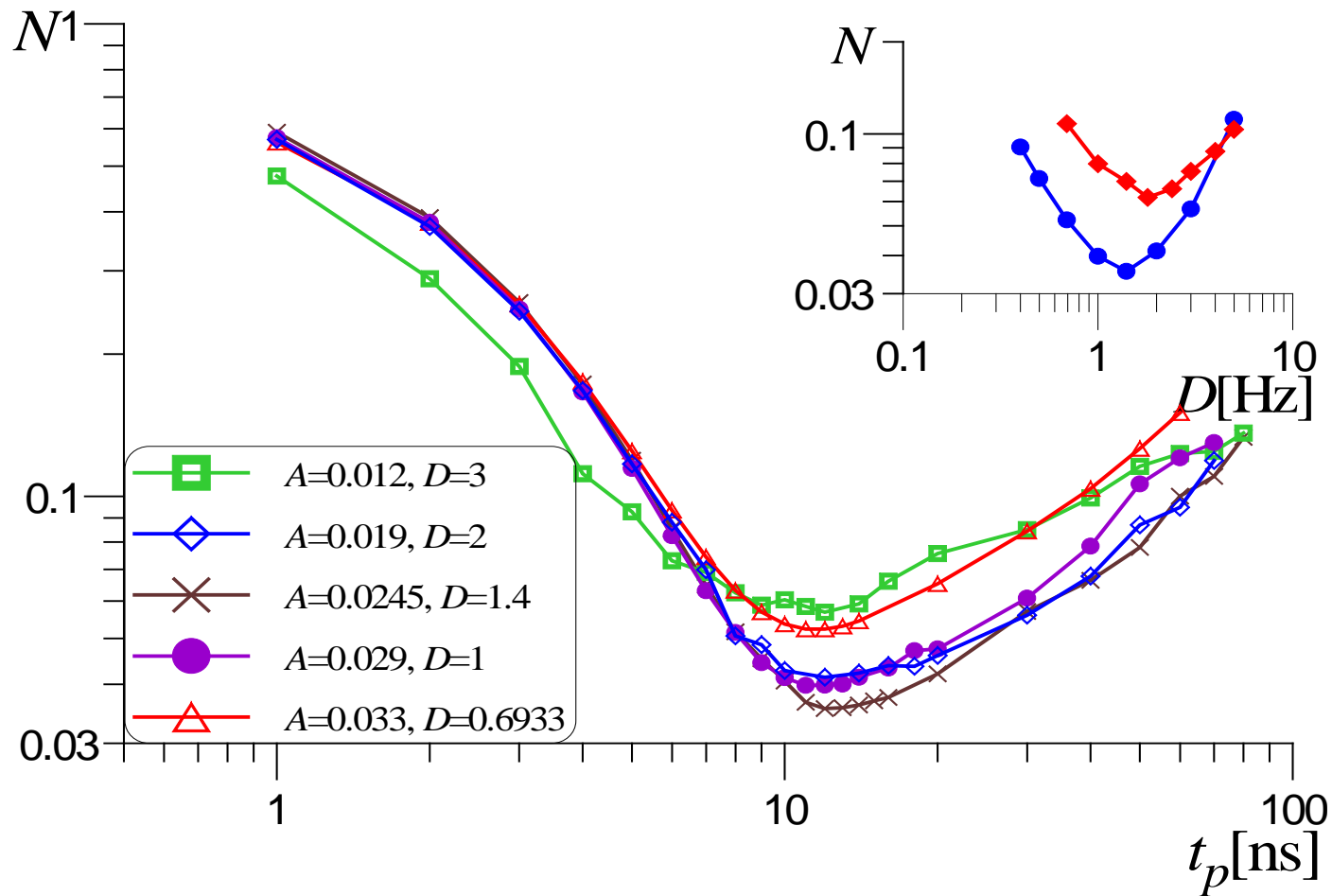


Q. Zhang, A. G. Kofman, J. M. Martinis, and A. N. Korotkov,
Phys. Rev. B **74**, 214518 (2006).

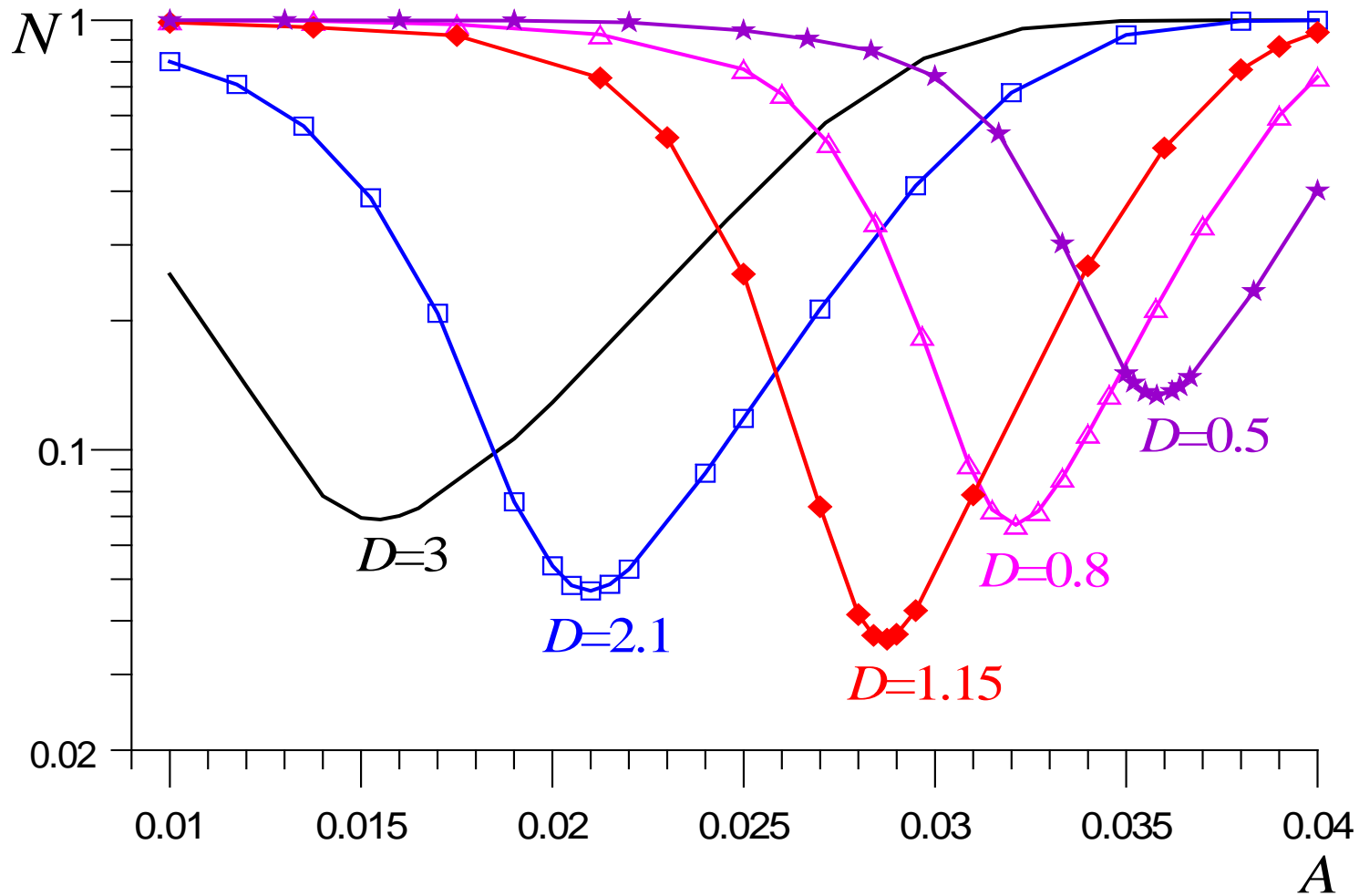
Readout error vs pulse amplitude



Readout error vs pulse duration



Readout error vs well depth

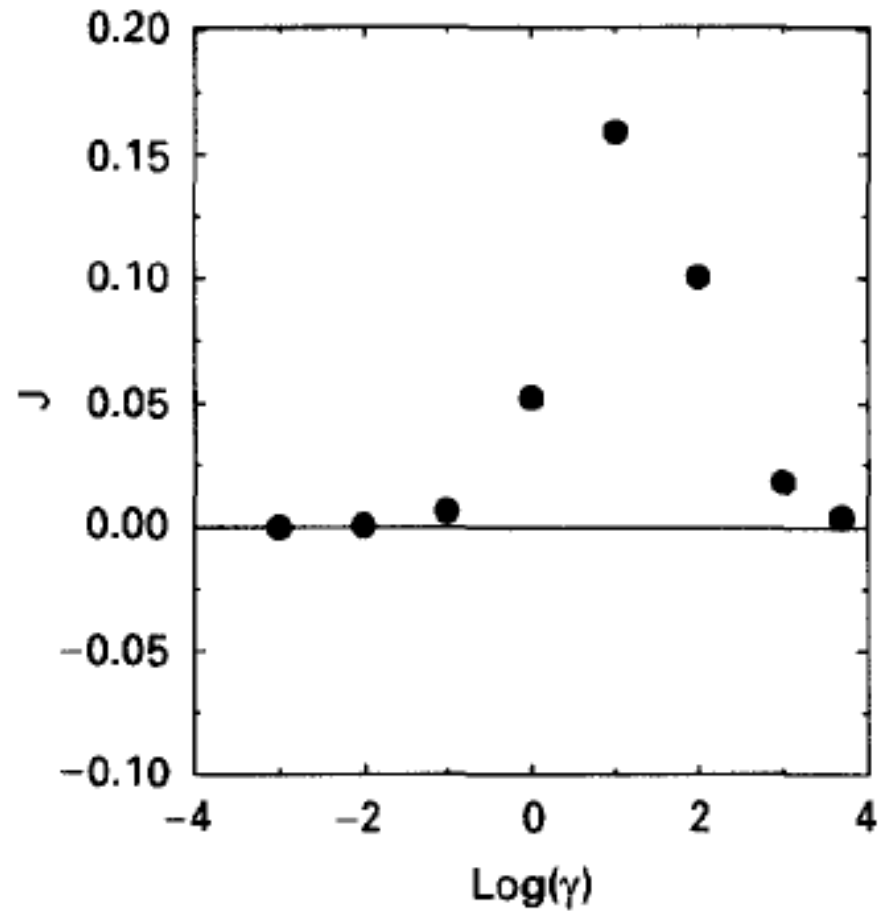
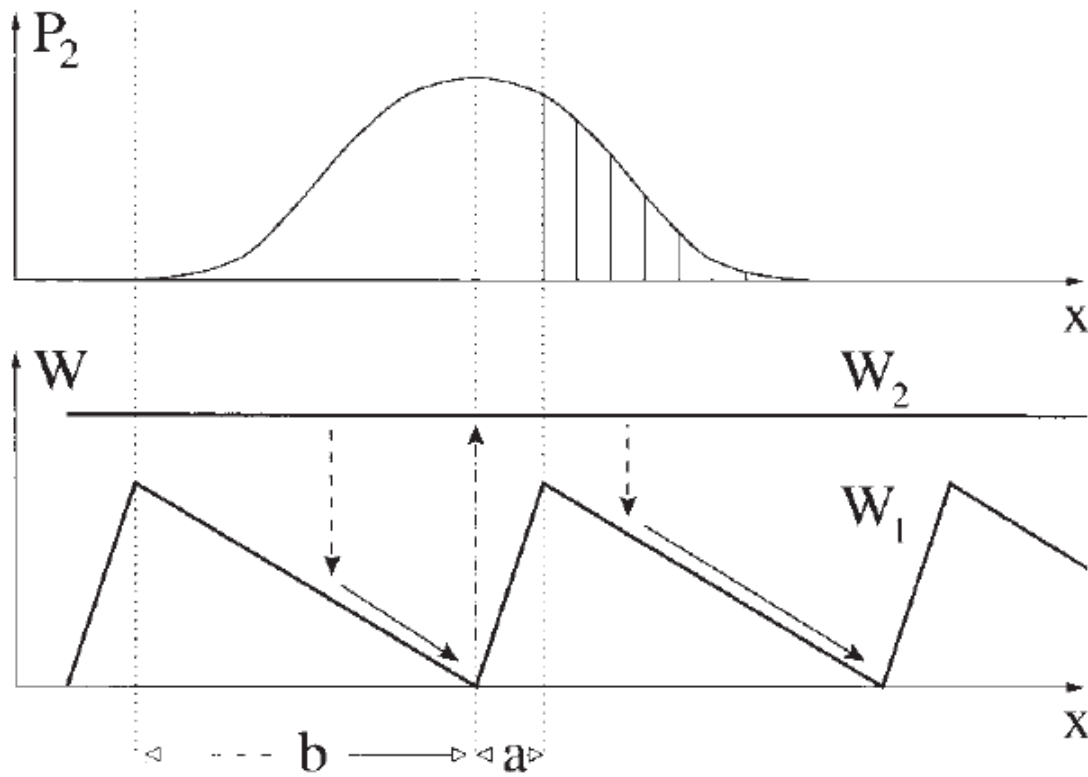


A.L. Pankratov and A.S. Gavrilov, Phys. Rev. B, 81, 052501 (2010).

L.S. Revin and A.L. Pankratov, Appl. Phys. Lett., 98, 162501 (2011).

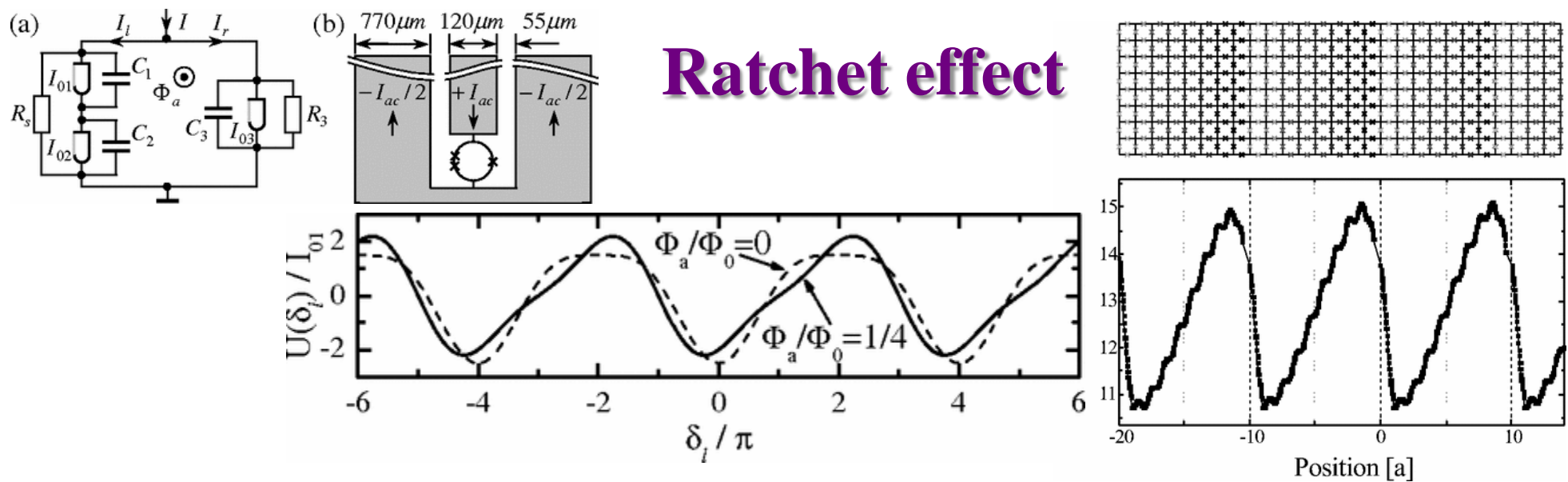


Ratchet effect



F. Julicher, A. Ajdari, J. Prost, Rev. Mod. Phys., 69, 1269 (1997).

C. Doering, Physica A, 254, 1 (1998).



Ratchet effect in dc SQUIDs, S. Weiss, D. Koelle, J. Müller, R. Gross and K. Barthel, Europhys. Lett. **51**, 499 (2000)

Three-Junction SQUID Rocking Ratchet, A. Sterck, R. Kleiner, and D. Koelle, Phys. Rev. Lett. **95**, 177006 (2005)

High-efficiency deterministic Josephson vortex ratchet, M Beck, E Goldobin, M Neuhaus, M Siegel, R Kleiner, D Koelle, Phys. Rev. Lett. **95**, 090603 (2005)

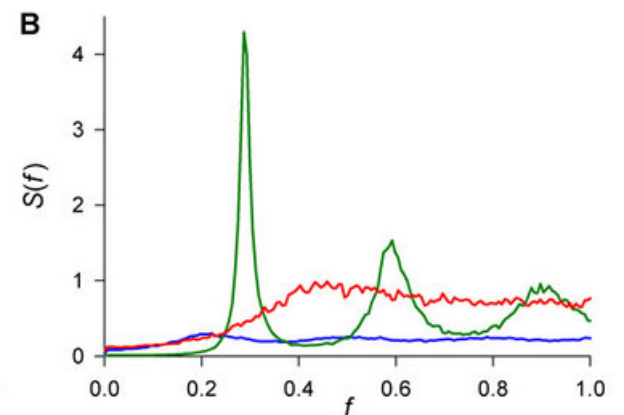
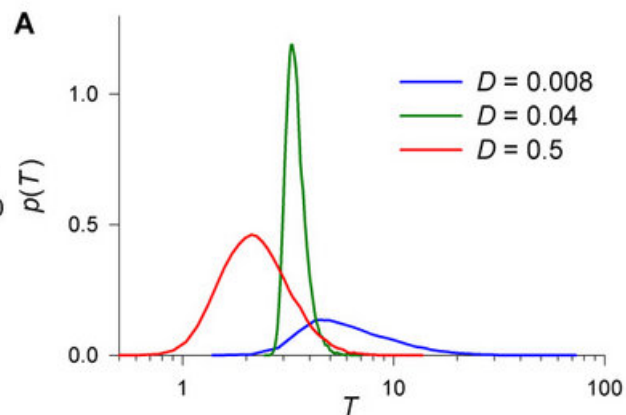
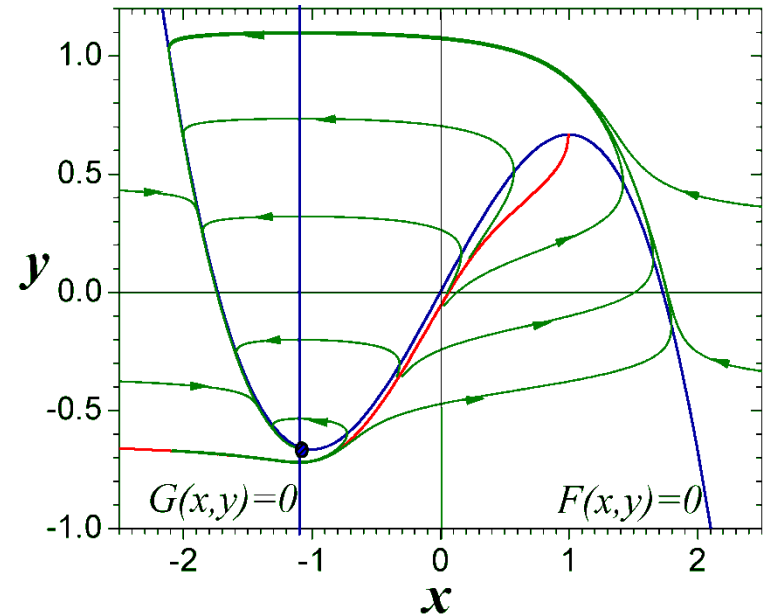
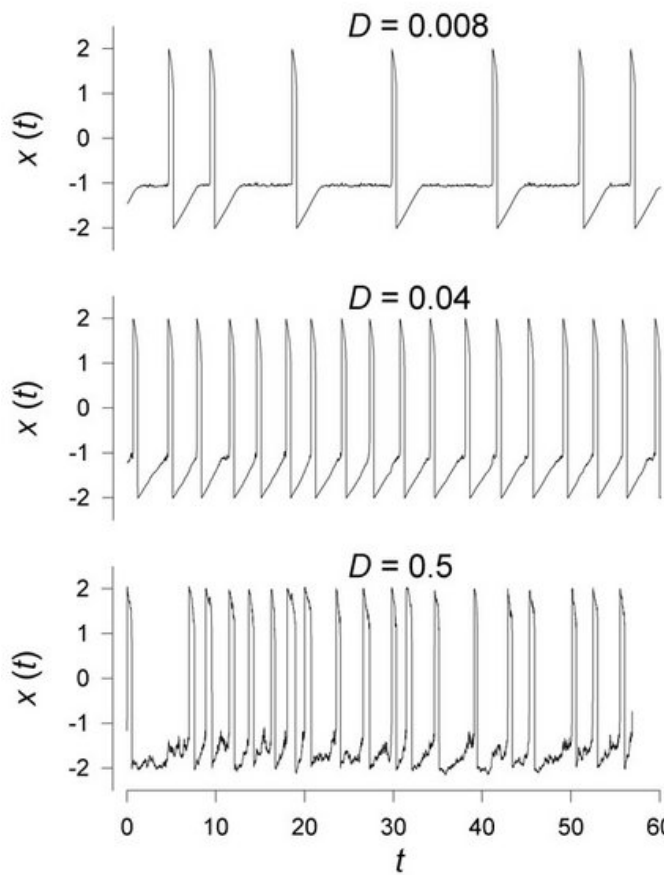
Vortex Motion Rectification in Josephson Junction Arrays with a Ratchet Potential, D. E. Shalóm and H. Pastoriza, Phys. Rev. Lett. **94**, 177001 (2005)

Tunable ϕ Josephson junction ratchet, R. Menditto, H. Sickinger, M. Weides, H. Kohlstedt, D. Koelle, R. Kleiner, and E. Goldobin, Phys. Rev. E **94**, 042202 (2016).

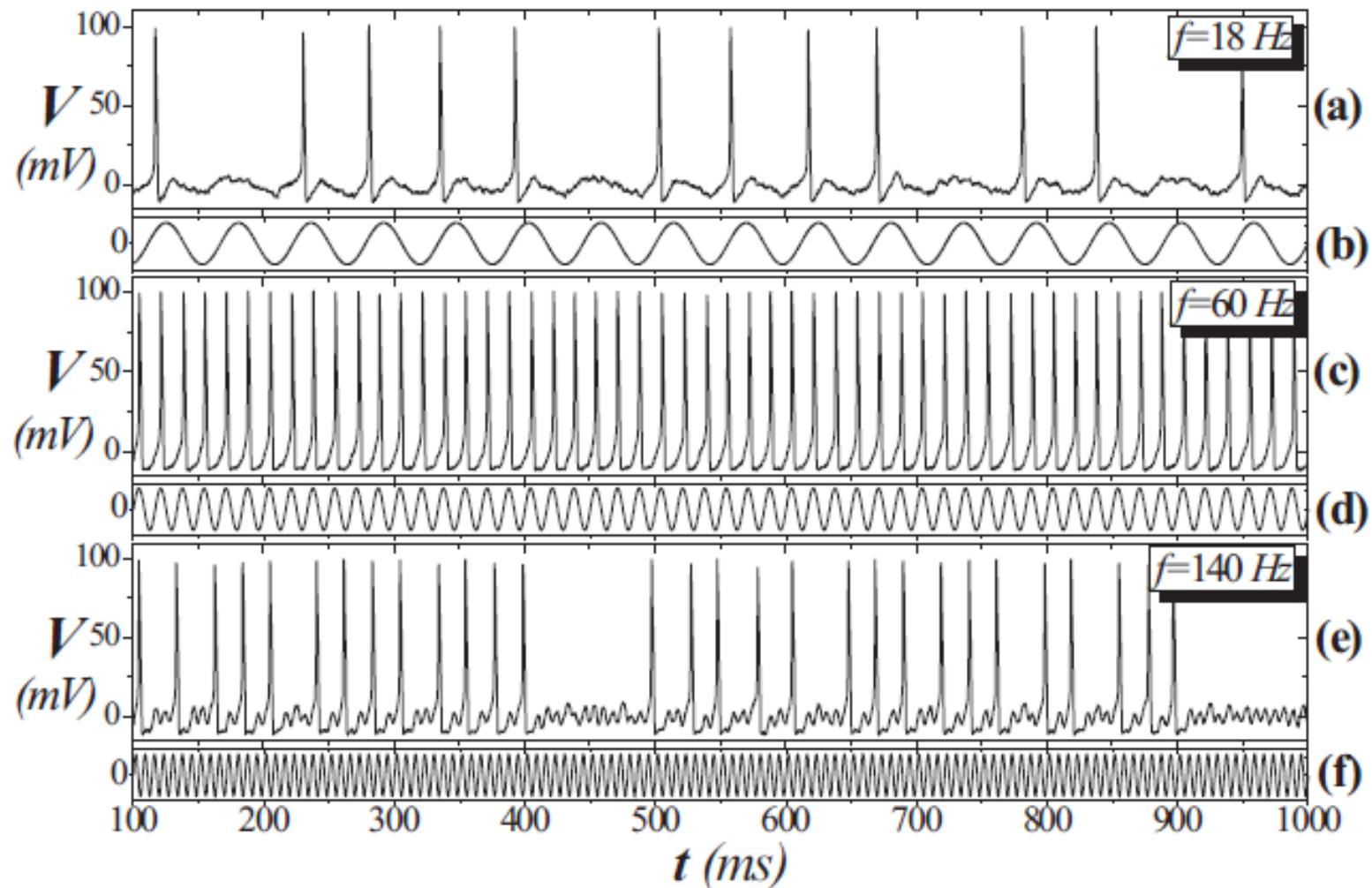
The current-phase relation in Josephson junctions, A. A. Golubov, M. Yu. Kupriyanov, E. Il'ichev, Rev. Mod. Phys. **76**, 411 (2004)

Coherence resonance

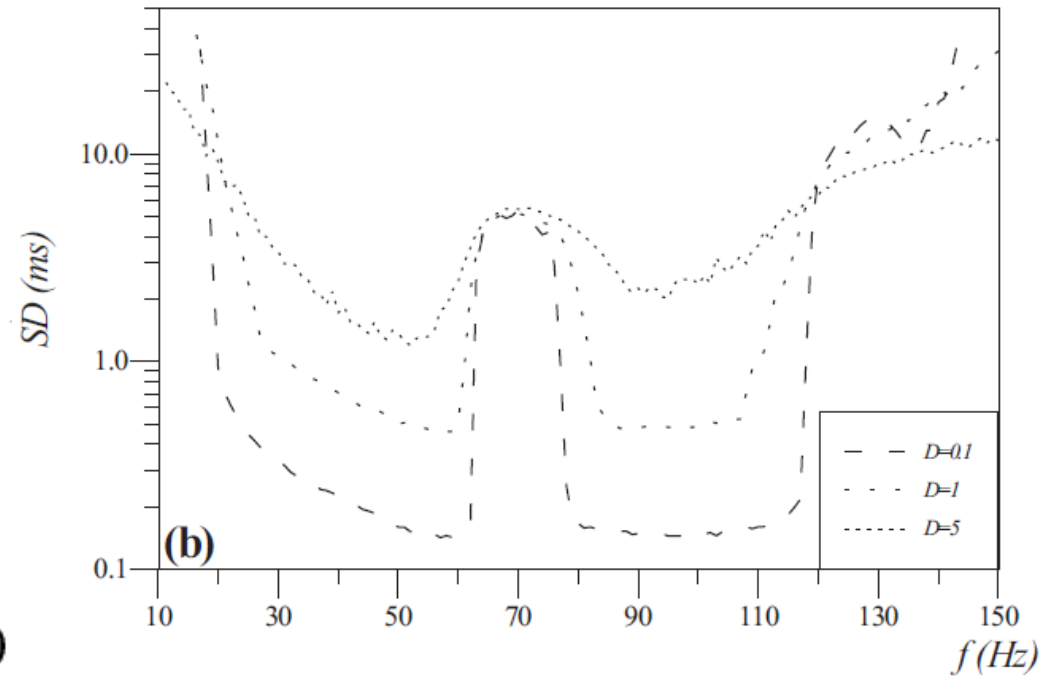
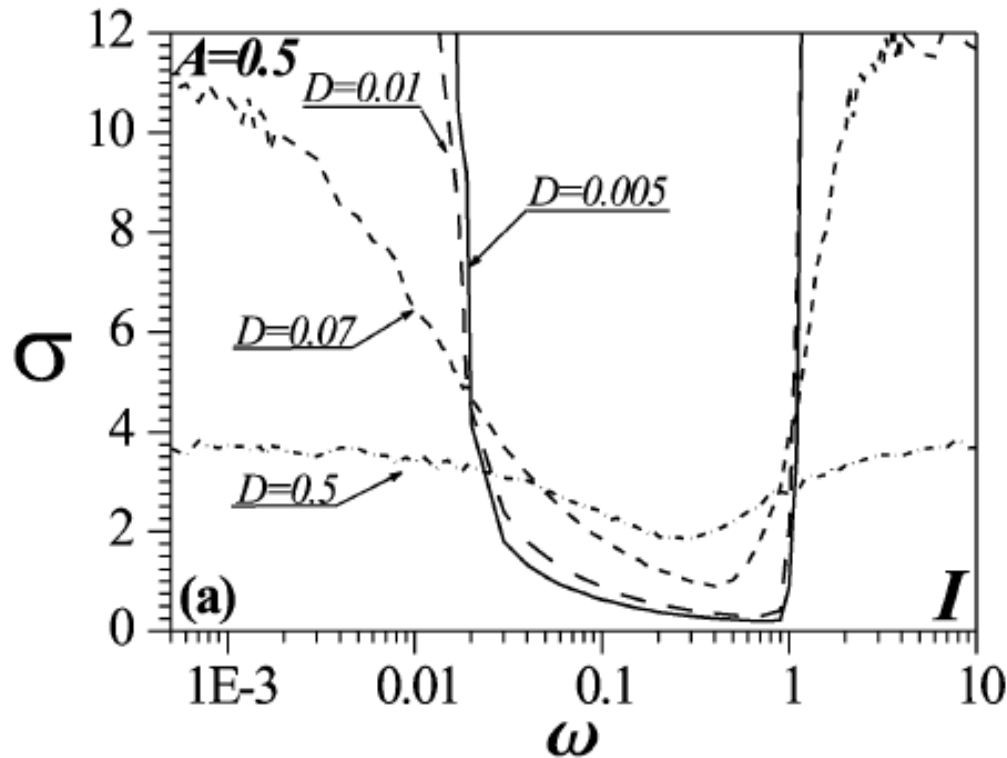
Pikovsky AS, Kurths J, Coherence resonance in a noise-driven excitable system. Physical Review Letters 78:775-778 (1997).



Suppression of noise in neuronal models

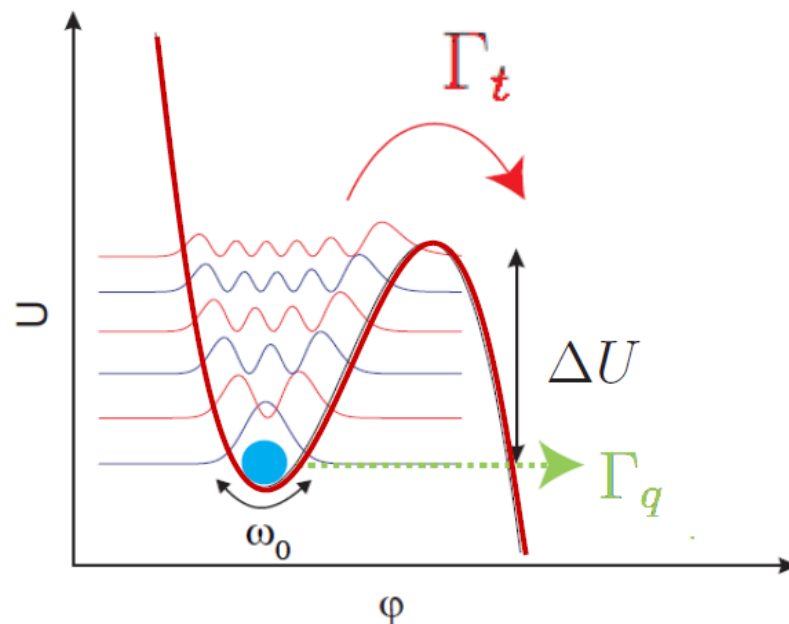
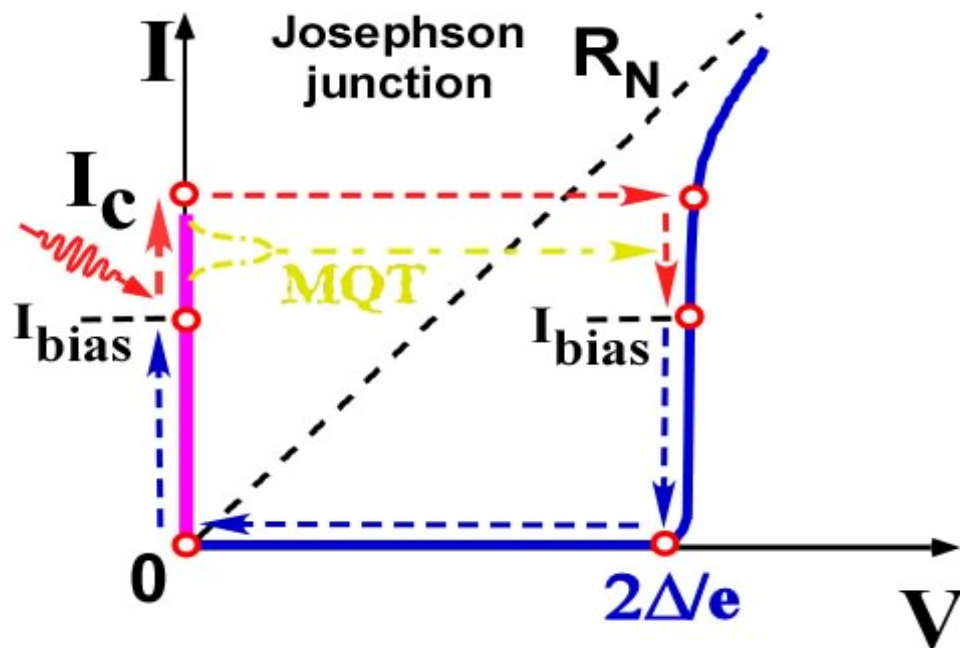


Suppression of noise in neuronal models



- E.V. Pankratova, V.N. Belykh and E. Mosekilde, Eur. Phys. Journal B, 00401 (2006).
E.V. Pankratova, A.V. Polovinkin and B. Spagnolo, Phys. Lett. A, 344, 43 (2005).
E.V. Pankratova, A.V. Polovinkin and E. Mosekilde, Eur. Phys. Journ. B, 45, 391 (2005).

Al SIS junction as single photon counter for 14 GHz



A. Wallraff, T. Duty, A. Lukashenko, A.V. Ustinov, [Phys. Rev. Lett.](#) 90, 037003 (2003).
G. Oelsner, L.S. Revin, E. Il'ichev, A.L. Pankratov, H.-G. Meyer, L. Gronberg, J. Hassel, L.S. Kuzmin, [Appl. Phys. Lett.](#) 103, 142605 (2013).
L. Kuzmin, A. Sobolev, C. Gatti, D. Gioacchino, N. Crescini, A. Gordeeva, E. Il'ichev, [IEEE Trans. Appl. Supercond.](#), 8, 2400505 (2018).

Search for axions – dark matter particles

Giovanni Carugno

Frank Wilczek

Yannis Semertzidis

Searching for galactic axions through magnetized media: The QUAX proposal

R.Barbieri a,b) C.Braggio c, **G.Carugno** c, C.S.Gallo c, A.Lombardi d, A.Ortolan d, R.Pengo d, G.Ruoso d,*, C.C.Speake e

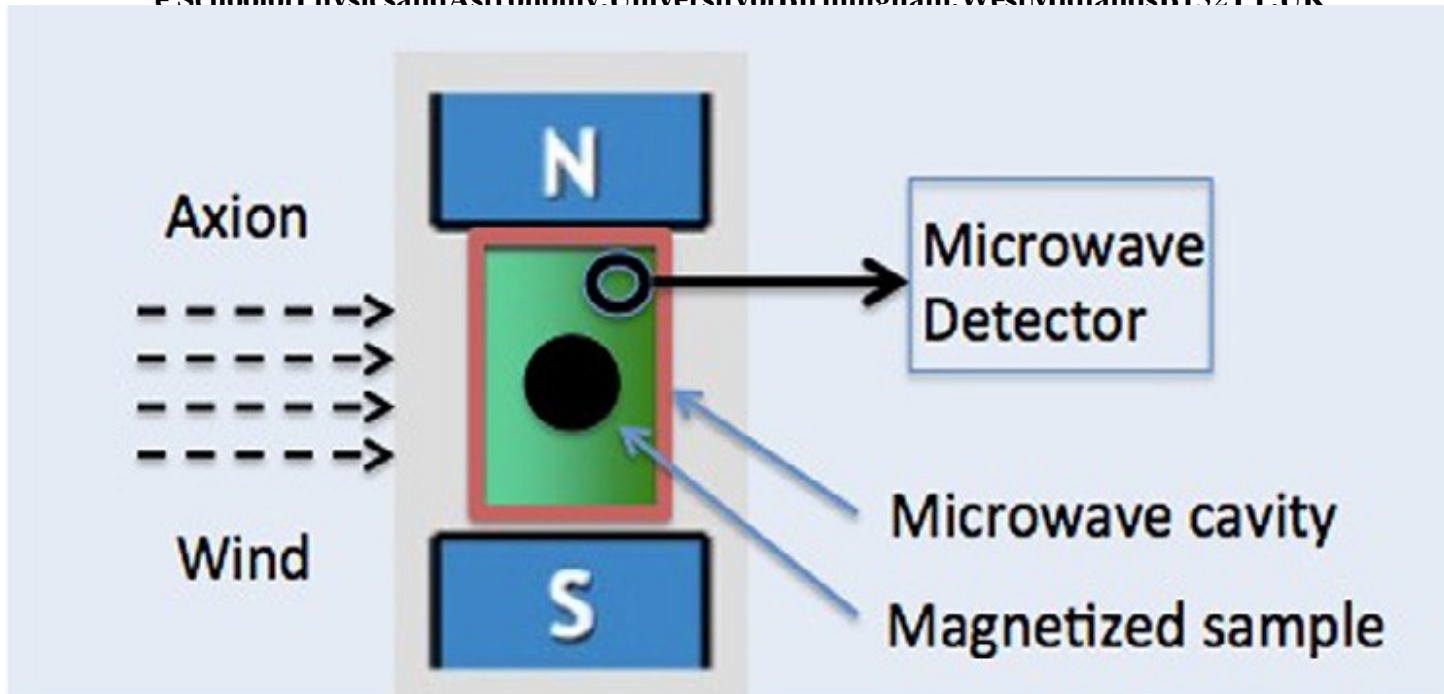
a Institute of Theoretical Studies, ETH, CH-8092 Zurich, Switzerland

b Scuola Normale Superiore, 56100 Pisa, Italy

c INFN, Sezione di Padova and Dipartimento di Fisica e Astronomia, Via Marzolo 8, **Padova, Italy**

d INFN, Laboratori Nazionali di Legnaro, Via dell'Università 2, 35020 Legnaro, Italy

e School of Physics and Astronomy, University of Birmingham, West Midlands B15 2TT, UK



Principle scheme of the axion haloscope

Cavity



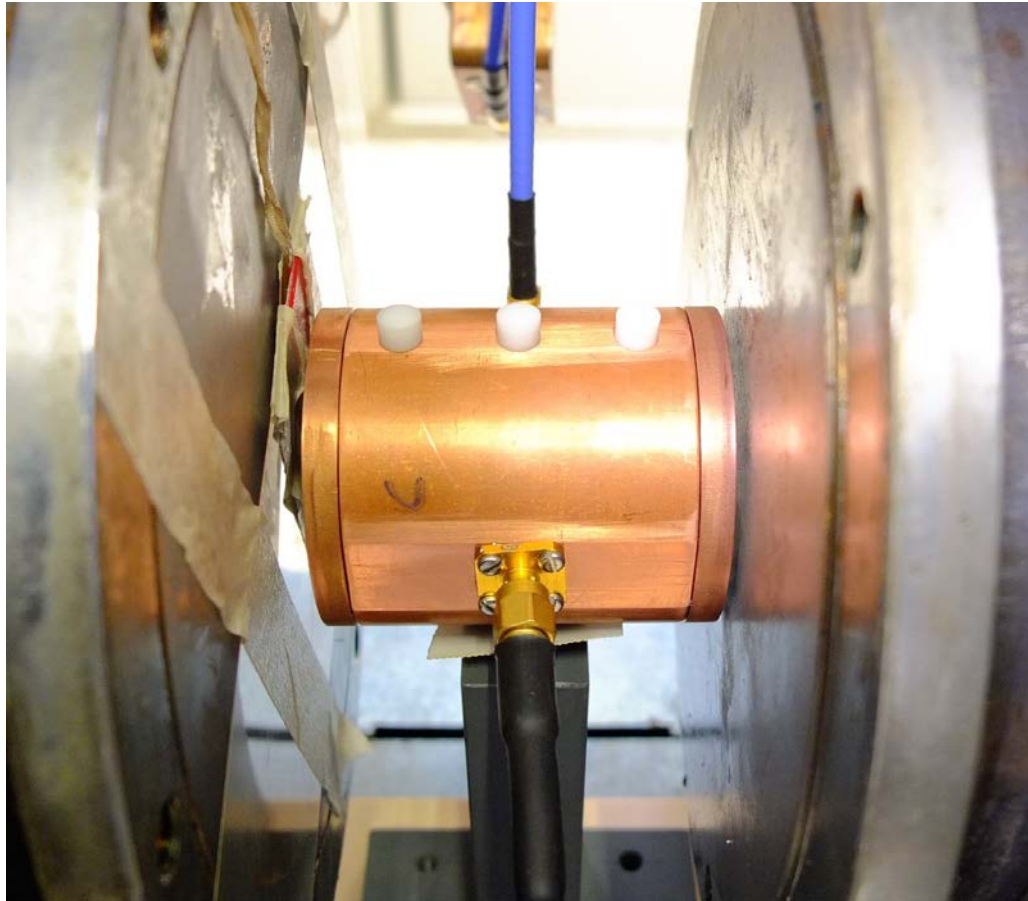
Half of a 14 GHz resonant cavity with conical endcaps used for the Quax R&D.

A cylindrical cavity with magnetized samples inserted from the top side during a test for the Quax R&D in magnetic field at room temperature.

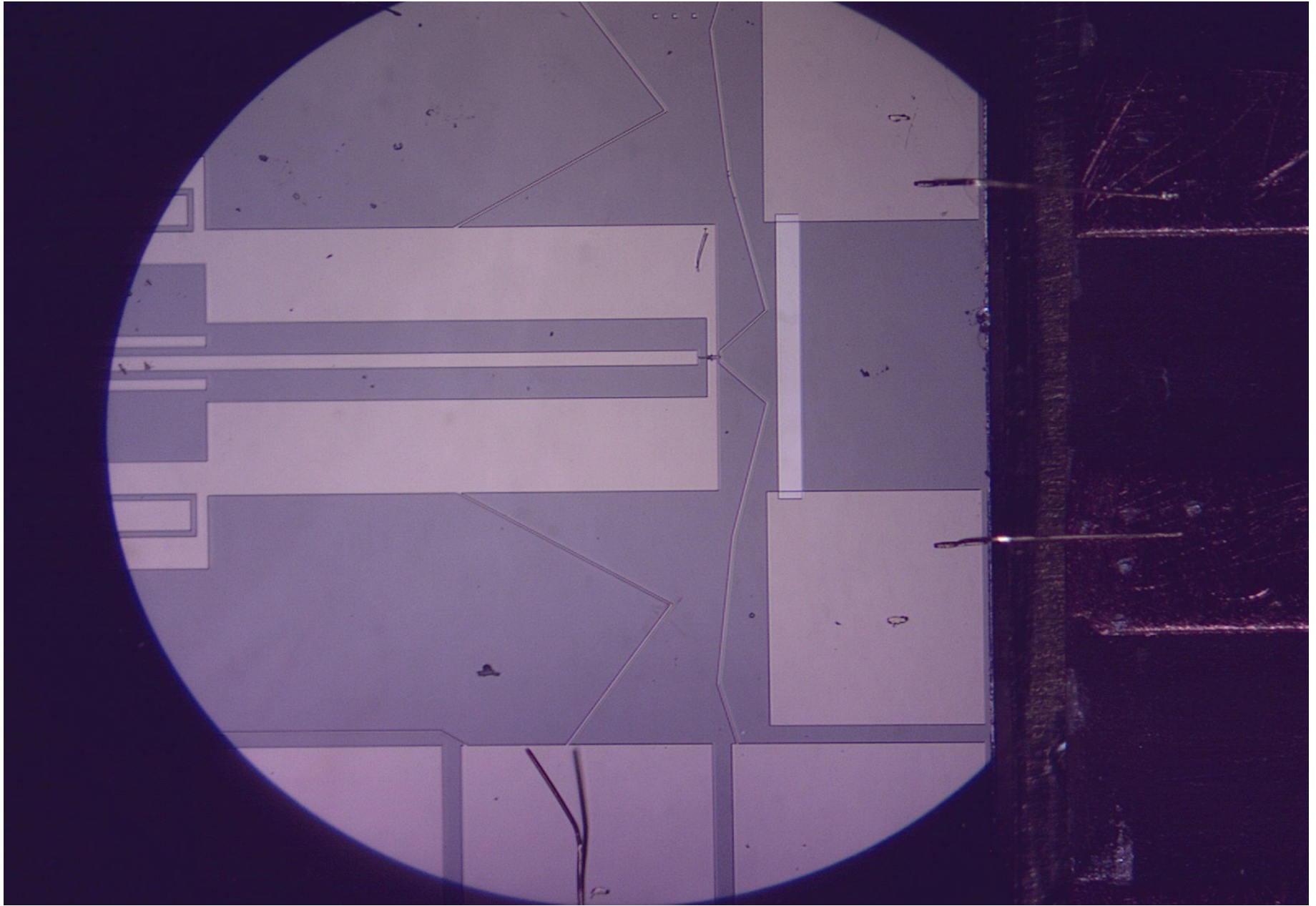
Q quality factor = 50 000

Resonant search of axions is performed tuning the cavity frequency by means of metallic tuning rods.

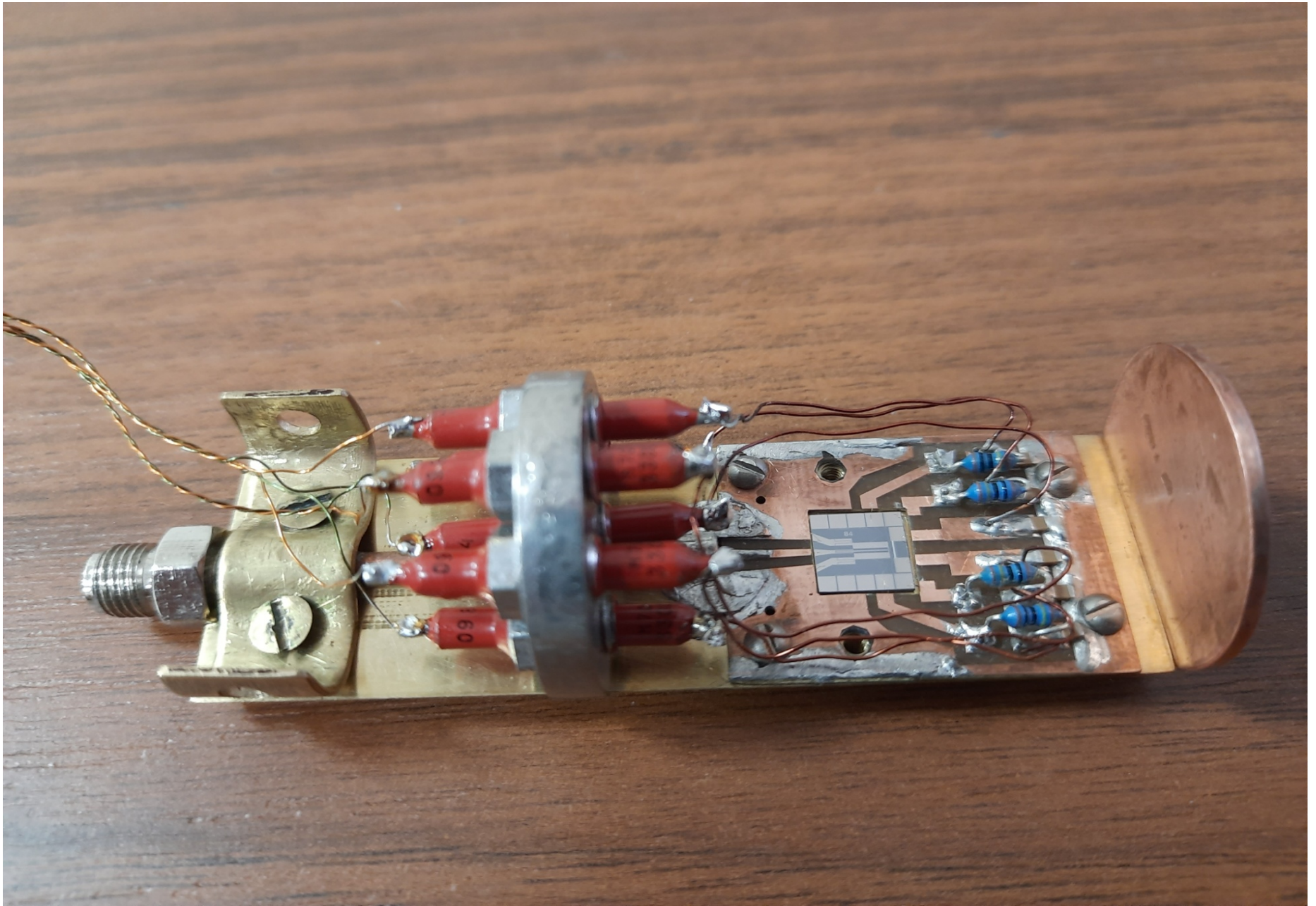
The frequency is shifted in a range $\pm 10\%$ corresponding to ± 1.4 GHz.



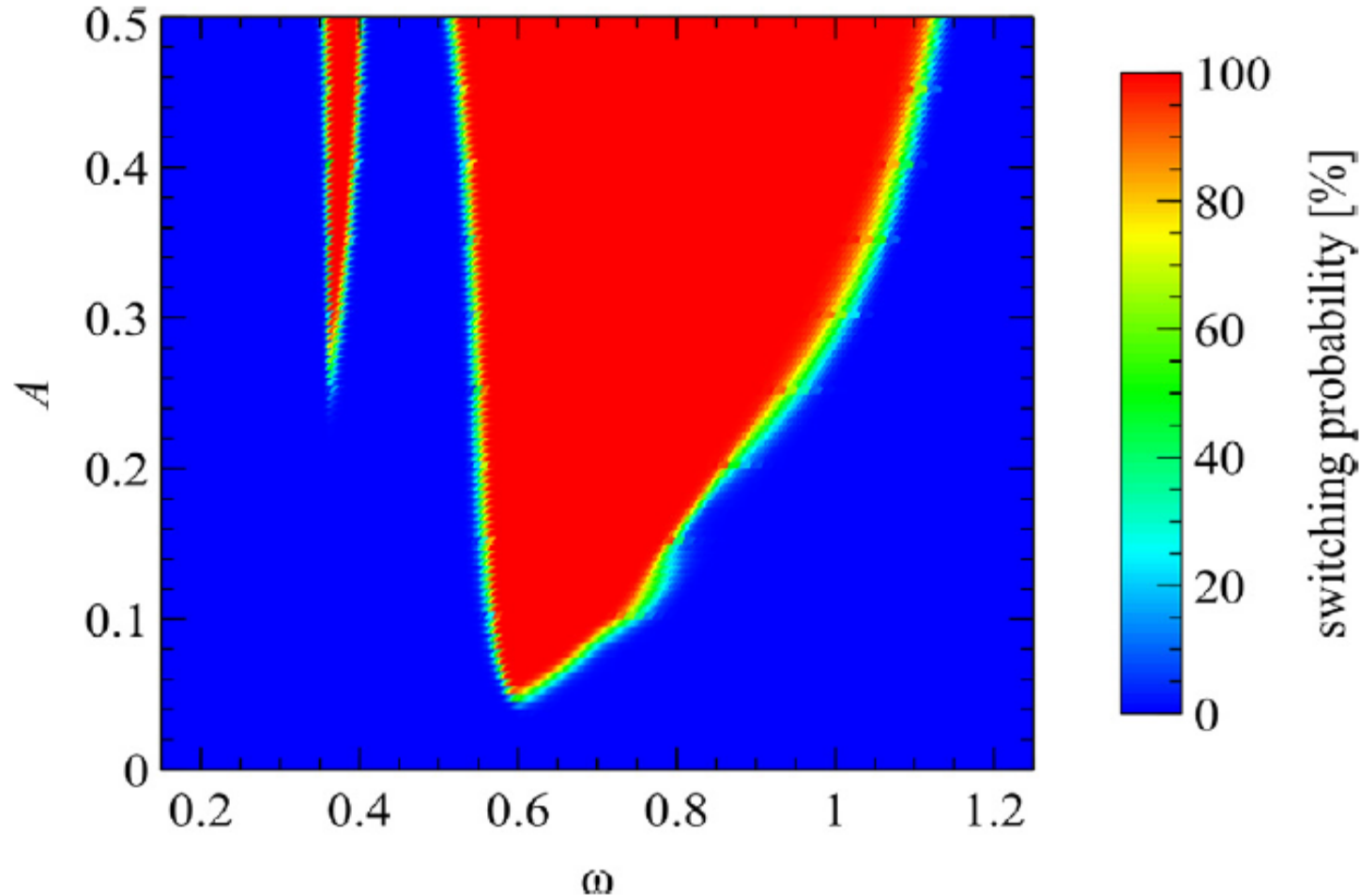
Sample photo



Sample photo



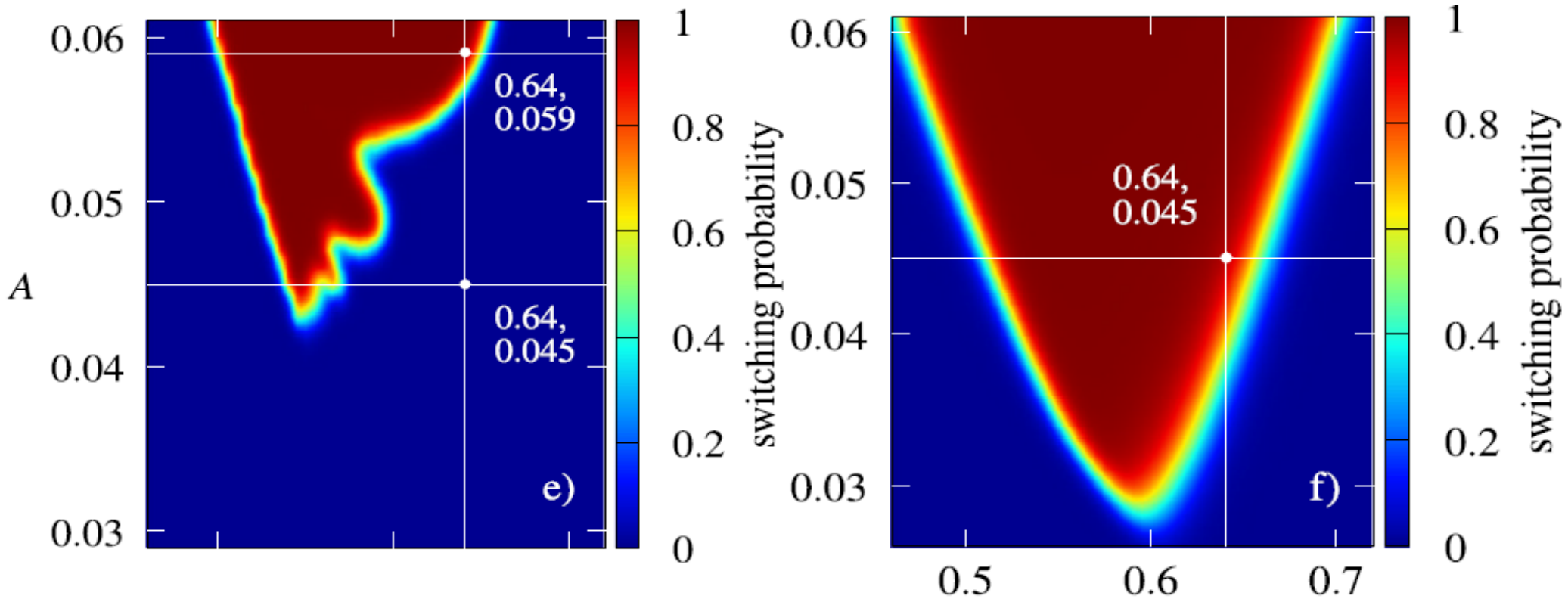
Resonant response drives sensitivity



Resonant response drives sensitivity of Josephson Escape Detector

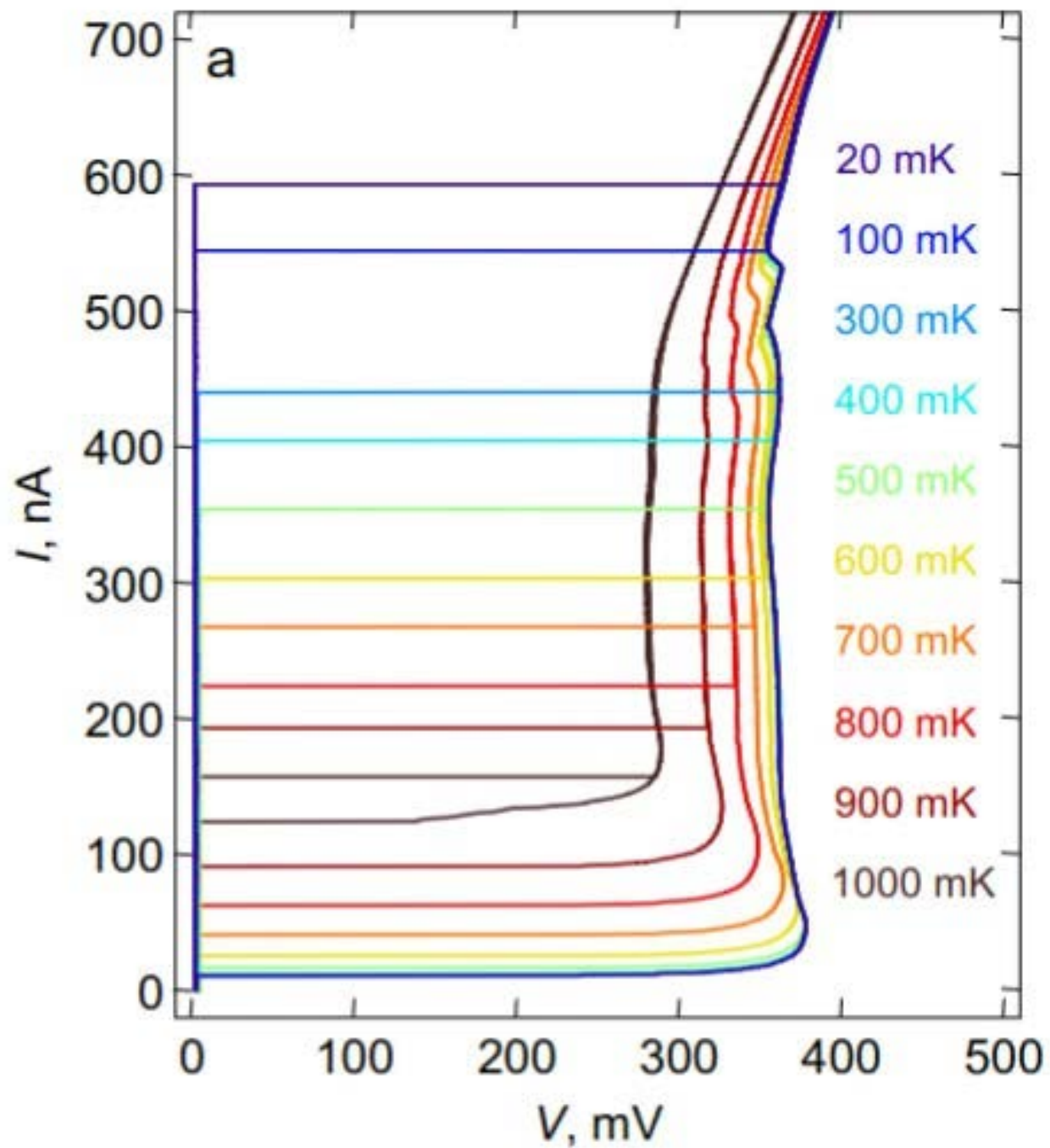
A.A. Yablokov, E.I. Glushkov, A.L. Pankratov, A.V. Gordeeva, L.S. Kuzmin, E.V. Il'ichev, [Chaos, Solitons & Fractals](#) 148, 111058 (2021)

Weak heating drives sensitivity



Stochastic versus dynamic resonant activation to enhance threshold detector sensitivity

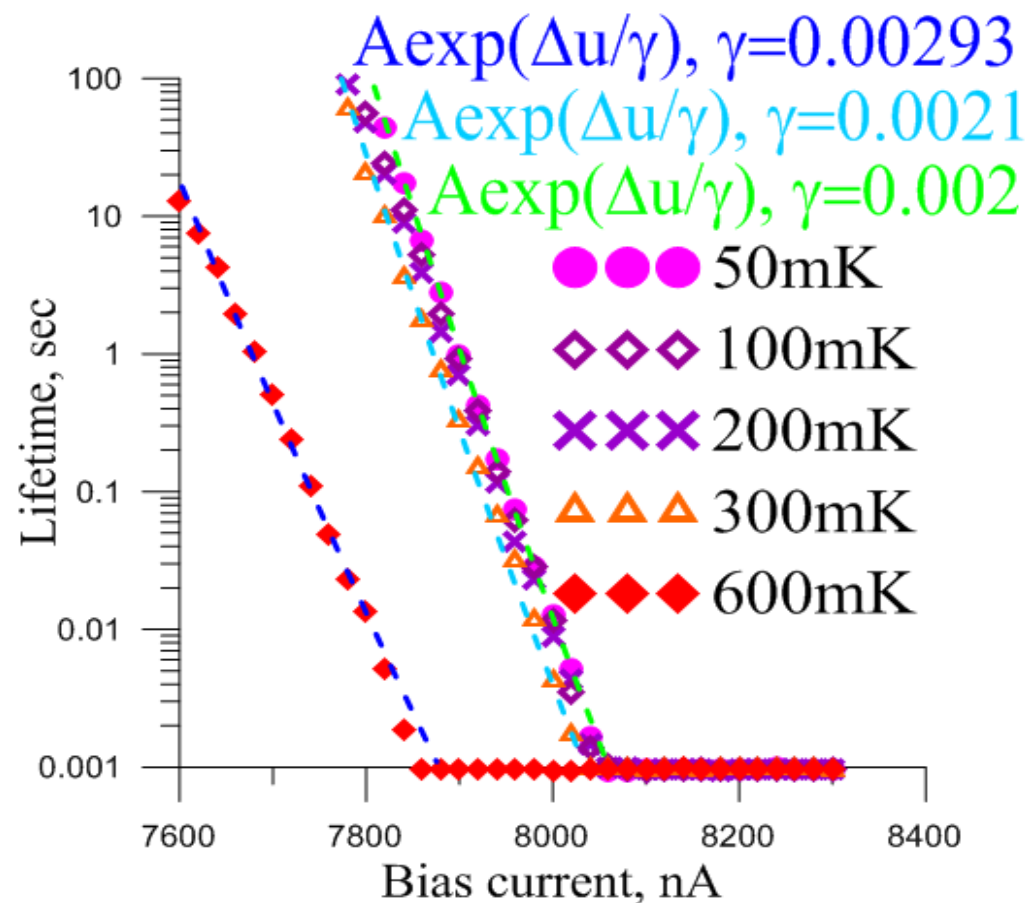
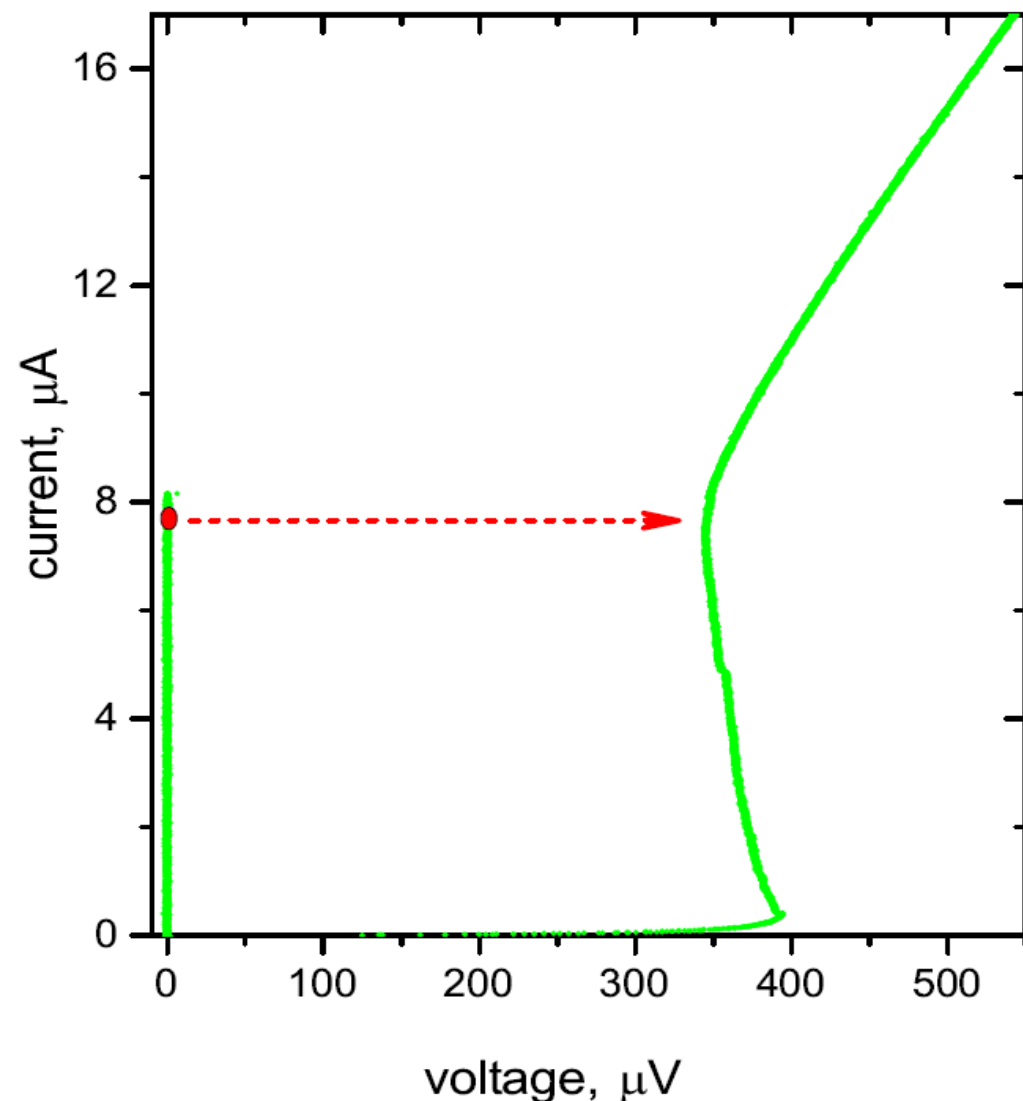
D.A. Ladeynov, E.G. Egorov, A.L. Pankratov, *Chaos, Solitons & Fractals* 171, 113506 (2023)



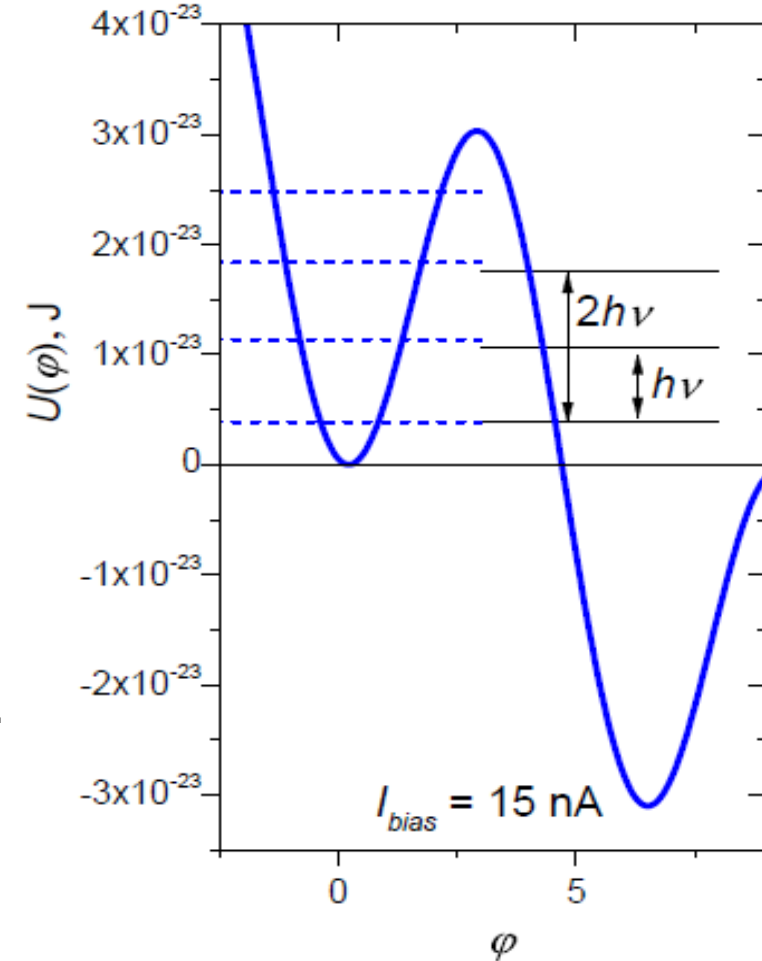
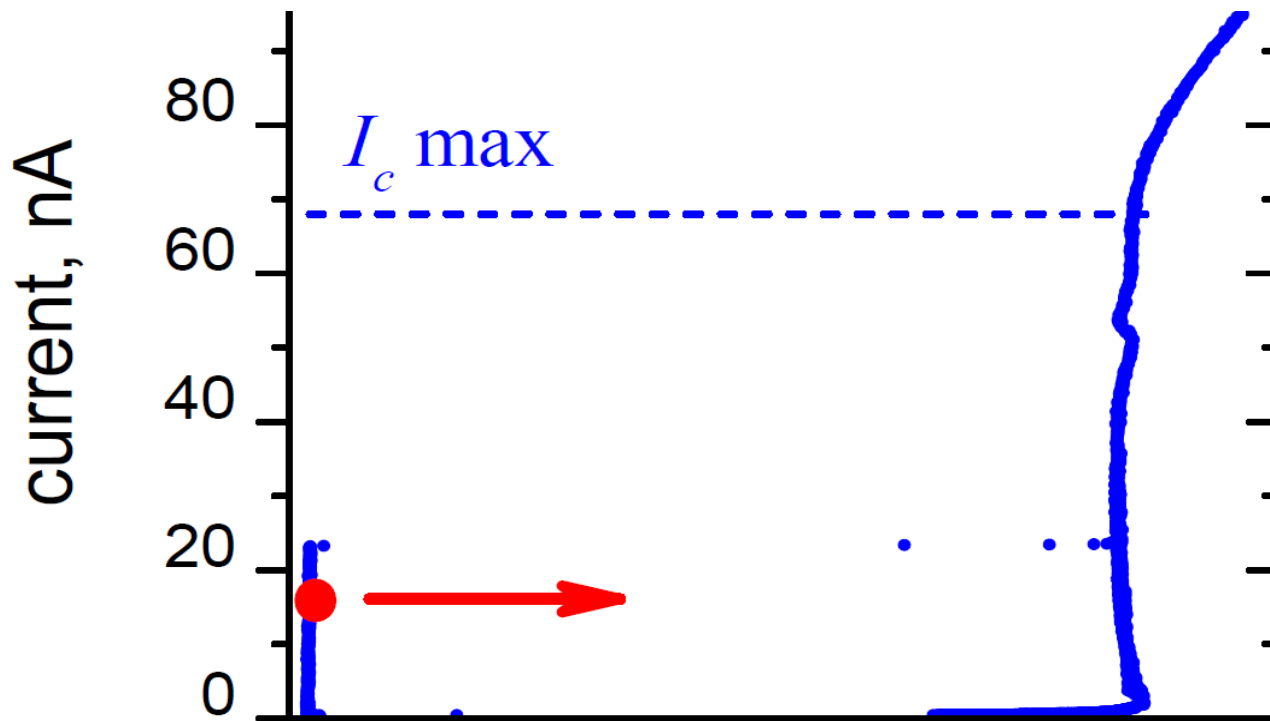
Lifetime of a large SIS junction

$$\gamma = I_T/I_C \quad I_T [\mu\text{A}] = 0.042T [\text{K}]$$

$$\tau = \frac{f(\alpha) \exp(\Delta u / \gamma)}{\sqrt{1 - i^2}}$$



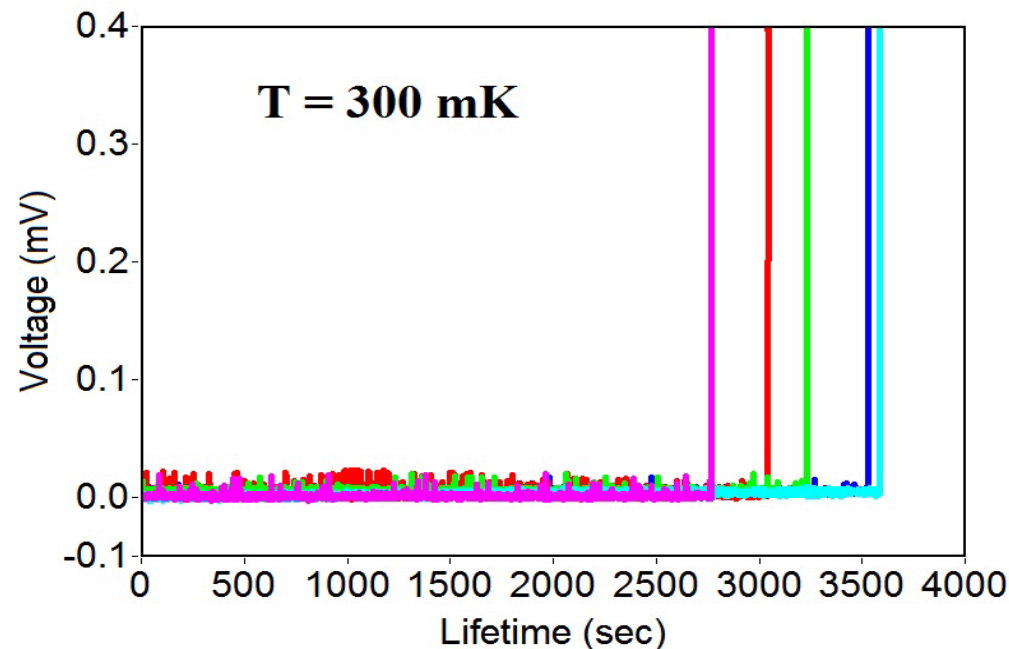
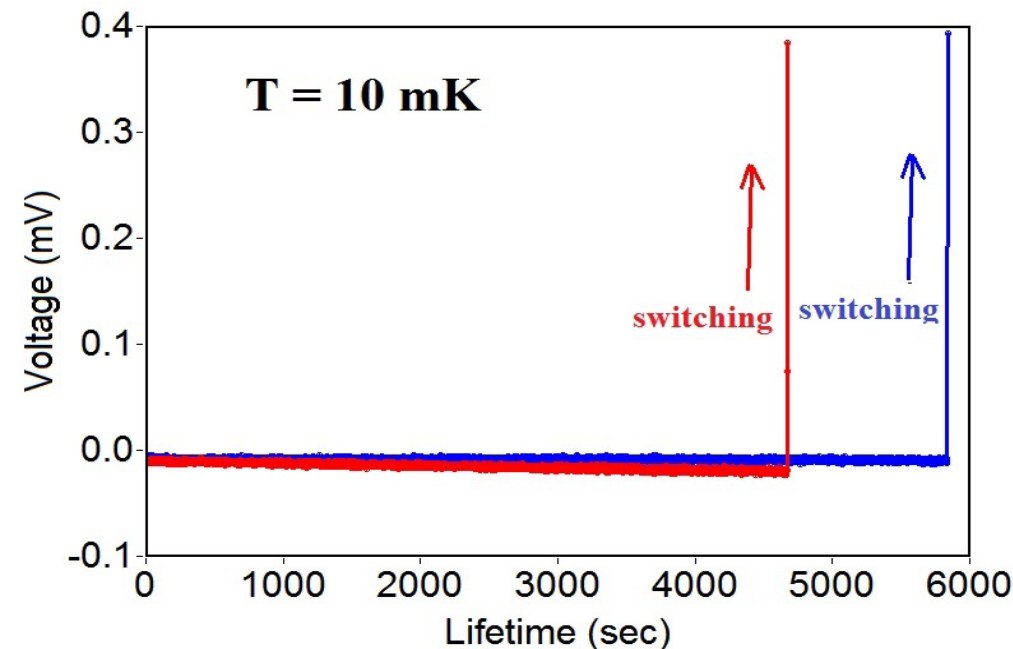
Lifetime of a small SIS junction



For small junctions the critical current is suppressed due to MQT.

D.S. Golubev, E.V. Il'ichev, & L.S. Kuzmin, *Phys. Rev. Appl.*, 16, 014025 (2021).

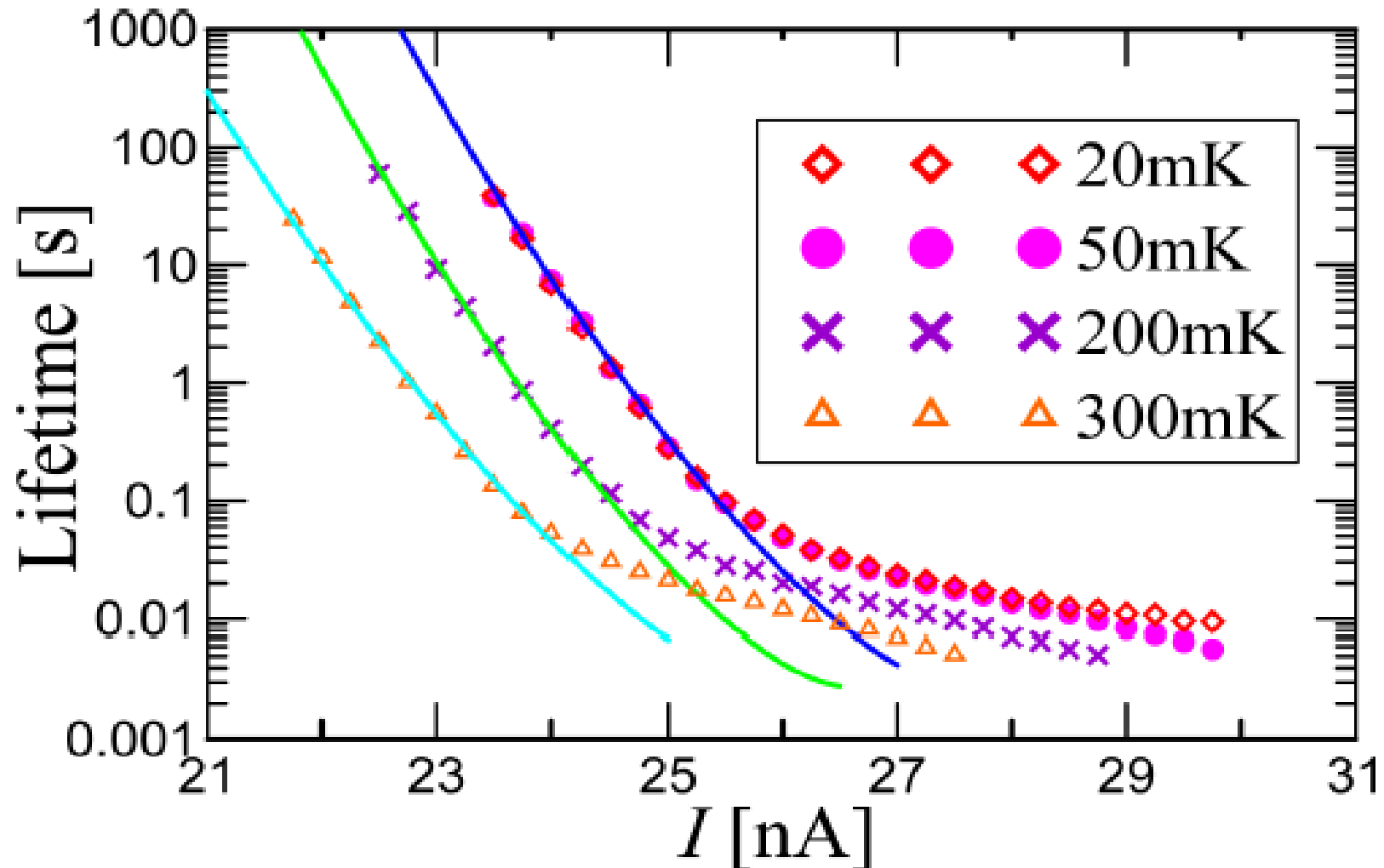
Lifetime of a small SIS junction



Does Kramers' formula $\tau \sim \exp(\Delta u / \gamma)$ still work ???
Lifetime can be increased by orders of magnitude
due to the phase diffusion regime

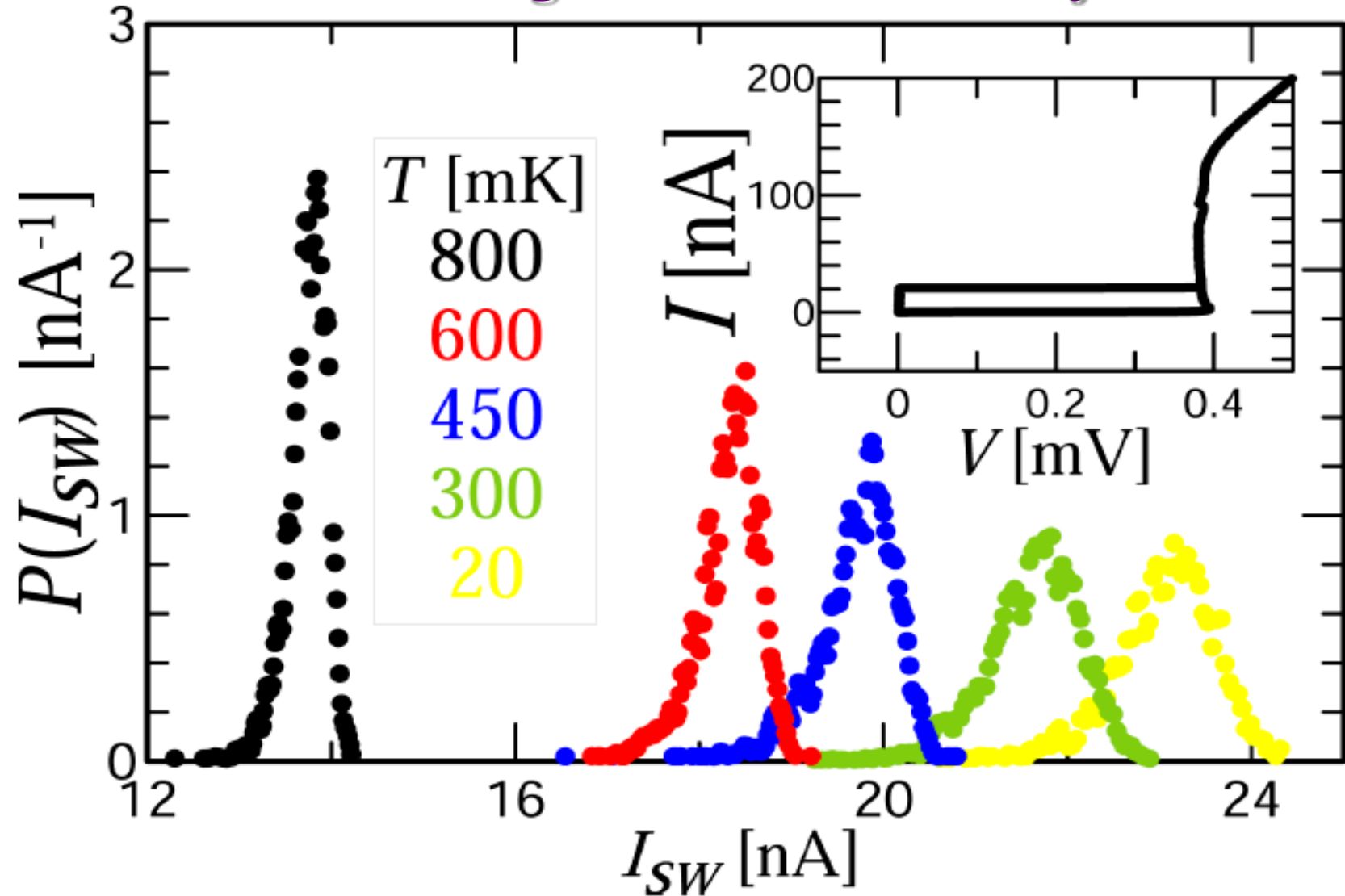
L.S. Revin, A.L. Pankratov, A.V. Gordeeva, A.A. Yablokov, I.V. Rakut, V.O. Zbrozhek, L.S. Kuzmin, [Beilstein J. Nanotechnol.](#) **11**, 960 (2020).

Lifetime of a small SIS junction



Kramers' formula $\tau \sim \exp(\Delta u / \gamma_{\text{eff}})$, but $\gamma_{\text{eff}} \ll \gamma$
Lifetime can be increased by orders of magnitude
due to the phase diffusion regime

Phase diffusion regime in a small SIS junction



L.S. Revin, A.L. Pankratov, A.V. Gordeeva, A.A. Yablokov, I.V. Rakut, V.O. Zbrozhek, L.S. Kuzmin, [Beilstein J. Nanotechnol.](#) **11**, 960 (2020).

Phase diffusion regime

J. M. Martinis, R. L. Kautz, Phys. Rev. Lett. 63, 1507 (1989).

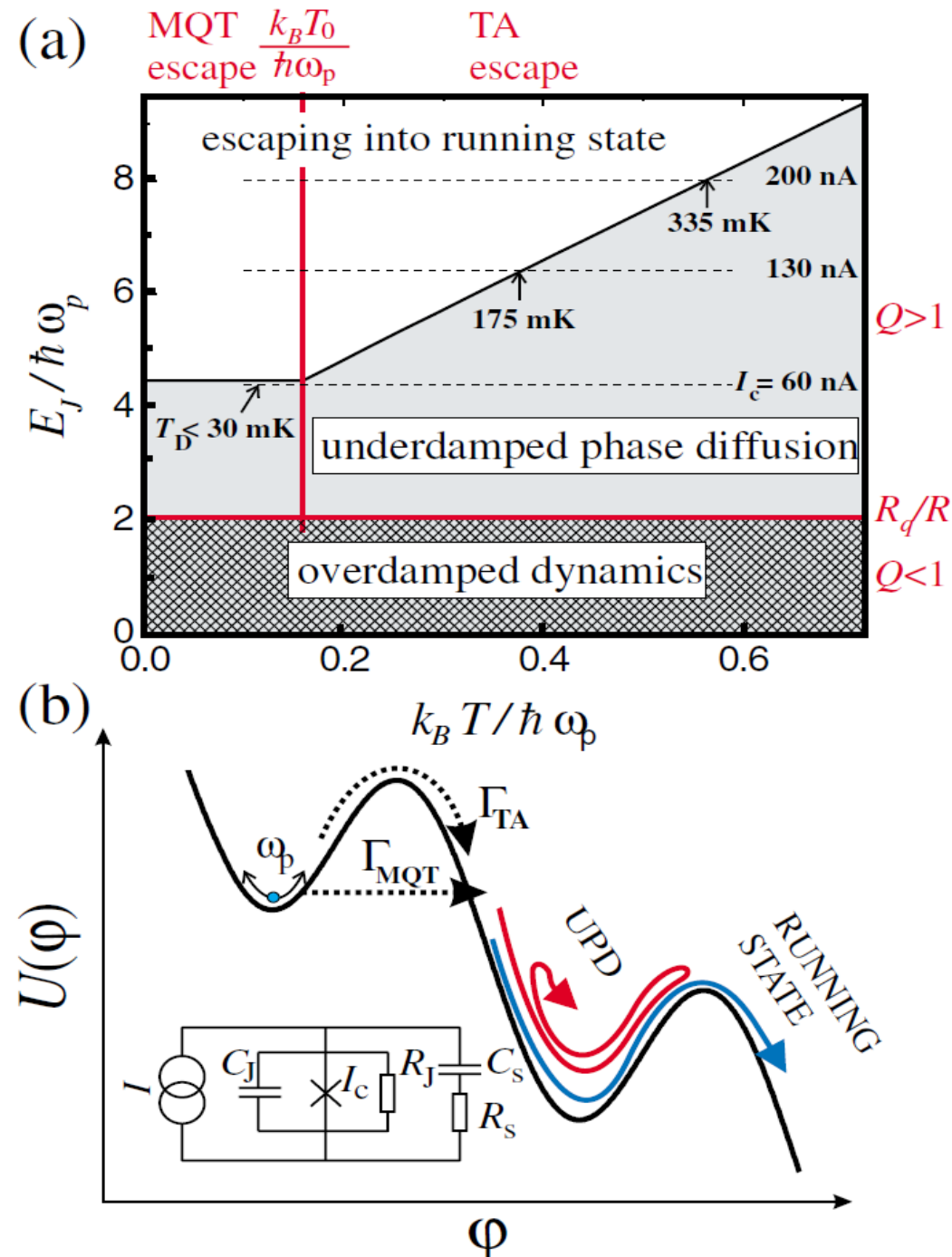
Y. Koval, M. V. Fistul, A. V. Ustinov, Phys. Rev. Lett. 93, 087004 (2004).

J. M. Kivioja, et al., Phys. Rev. Lett. 94, 247002 (2005).

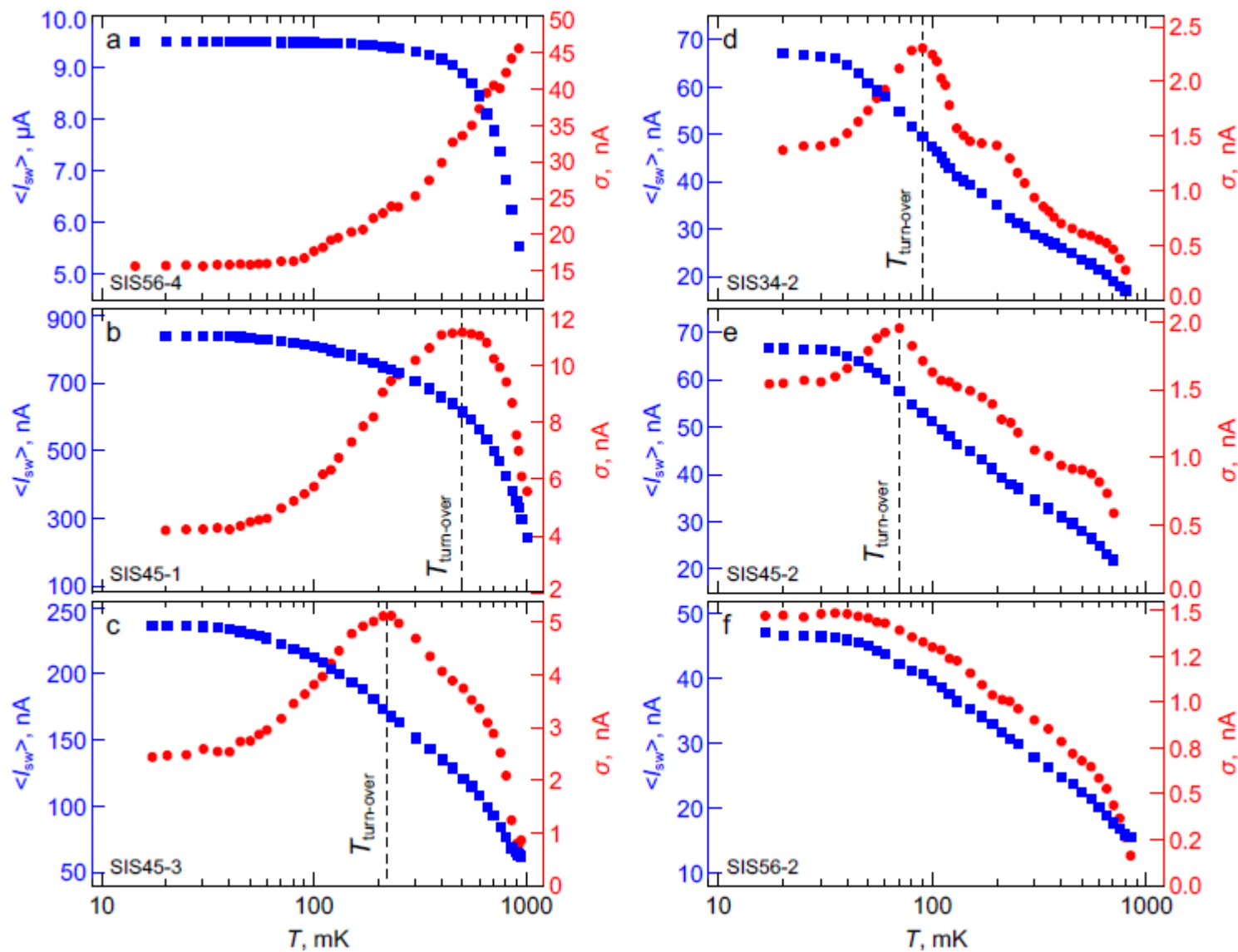
H. F. Yu, et al., Phys. Rev. Lett. 107, 067004 (2011).

L. Longobardi, et al., Phys. Rev. Lett. 109, 050601 (2012).

M. Lisitskiy, et. al., Journ. Appl. Phys. 116, 043905 (2014).

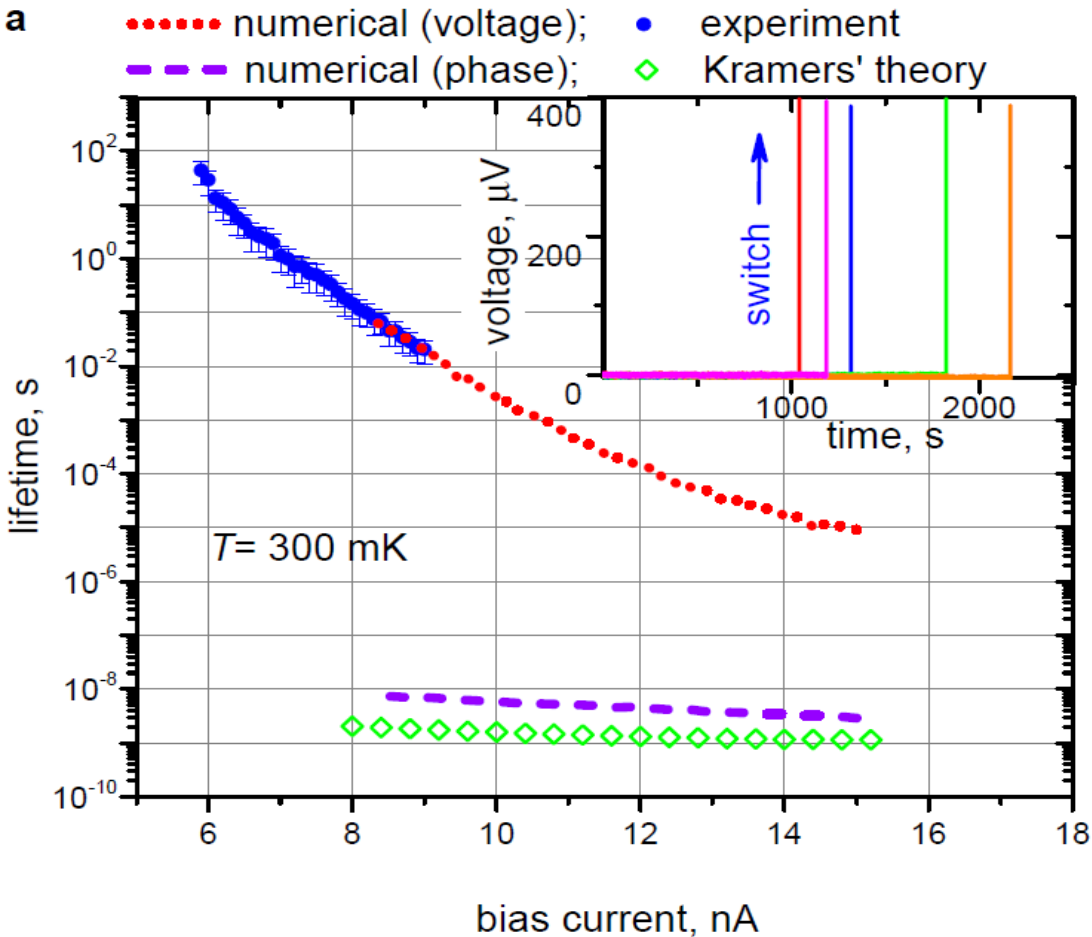


Switching current distributions

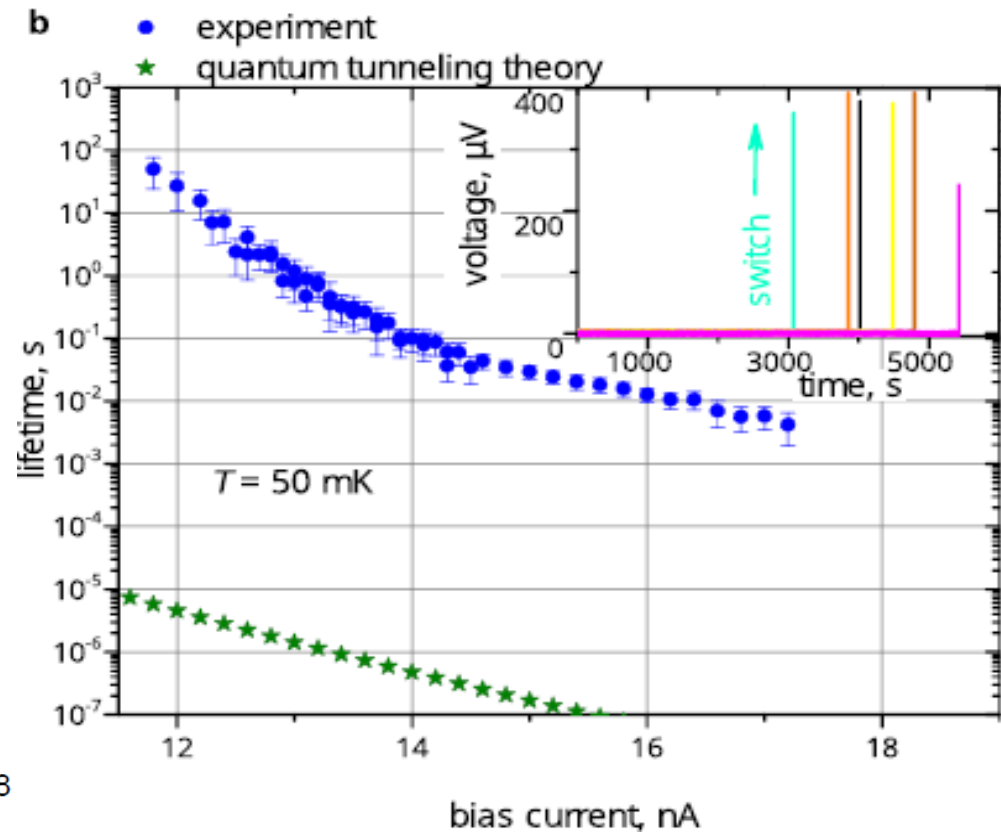


Lifetime of a small SIS junction

a



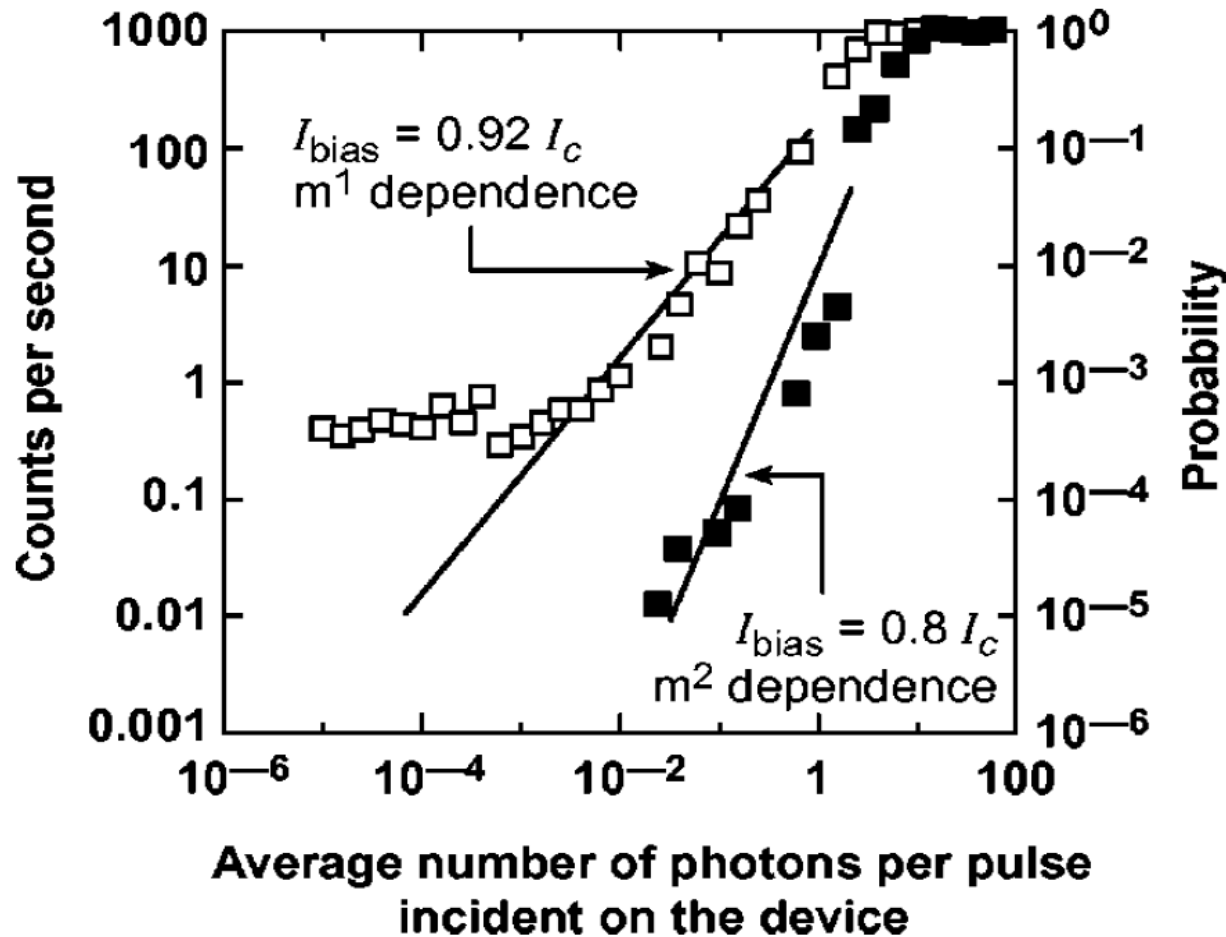
b



A. L. Pankratov, L. S. Revin, A. V. Gordeeva, A. A. Yablokov, L. S. Kuzmin & E. Il'ichev
Towards a microwave single-photon counter for searching axions,
[npj Quantum Information](https://www.nature.com/articles/s41534-022-00569-5), 8, 61 (2022)

<https://www.nature.com/articles/s41534-022-00569-5>

Counting of IR photons by statistics

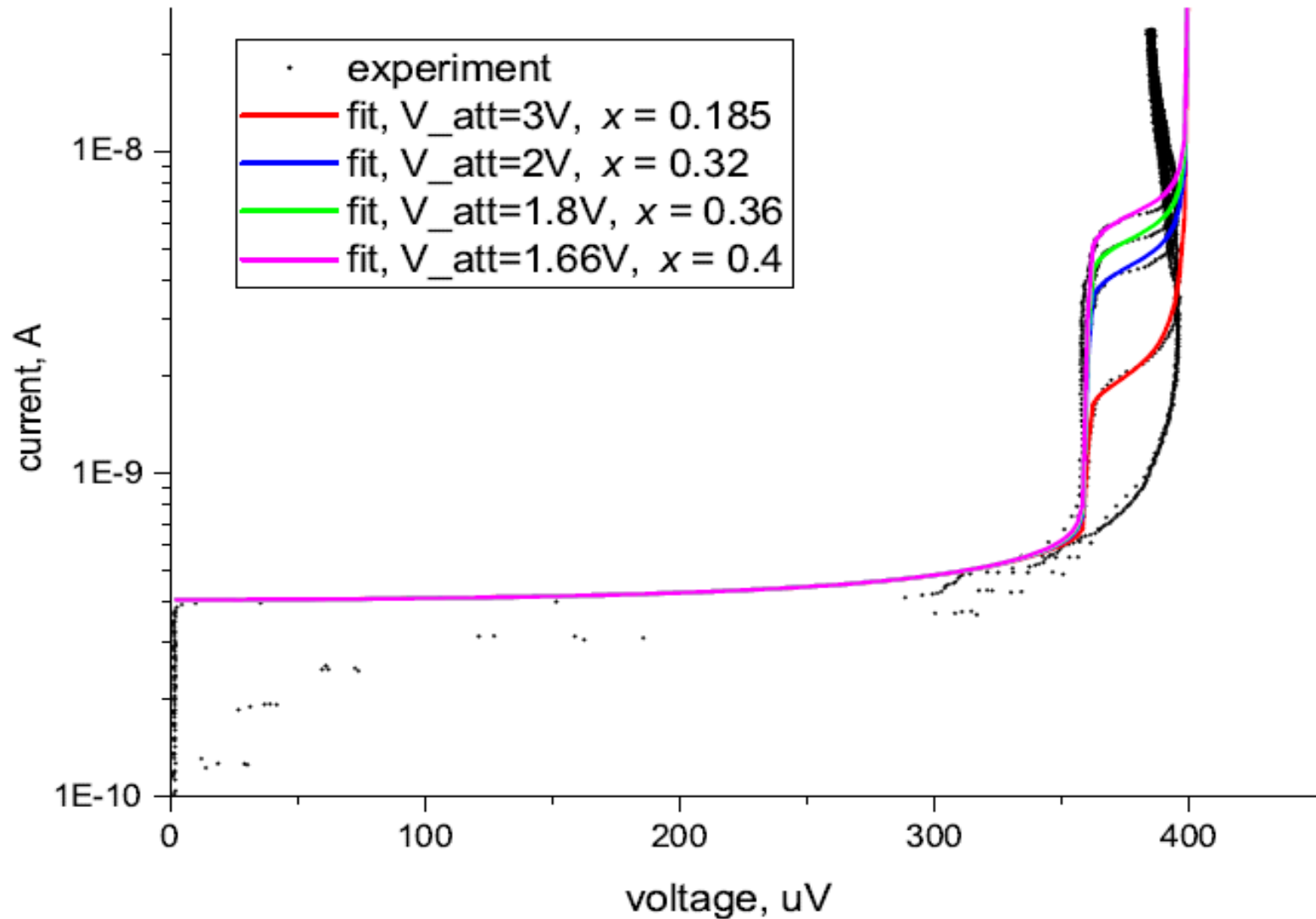


Detection of IR photons at 4K

G. N. Gol'tsman, O. Okunev, G. Chulkova, A. Lipatov, A. Semenov, K. Smirnov, B. Voronov, and A. Dzardanov, [Appl. Phys. Lett.](#), **79**, 705 (2001).



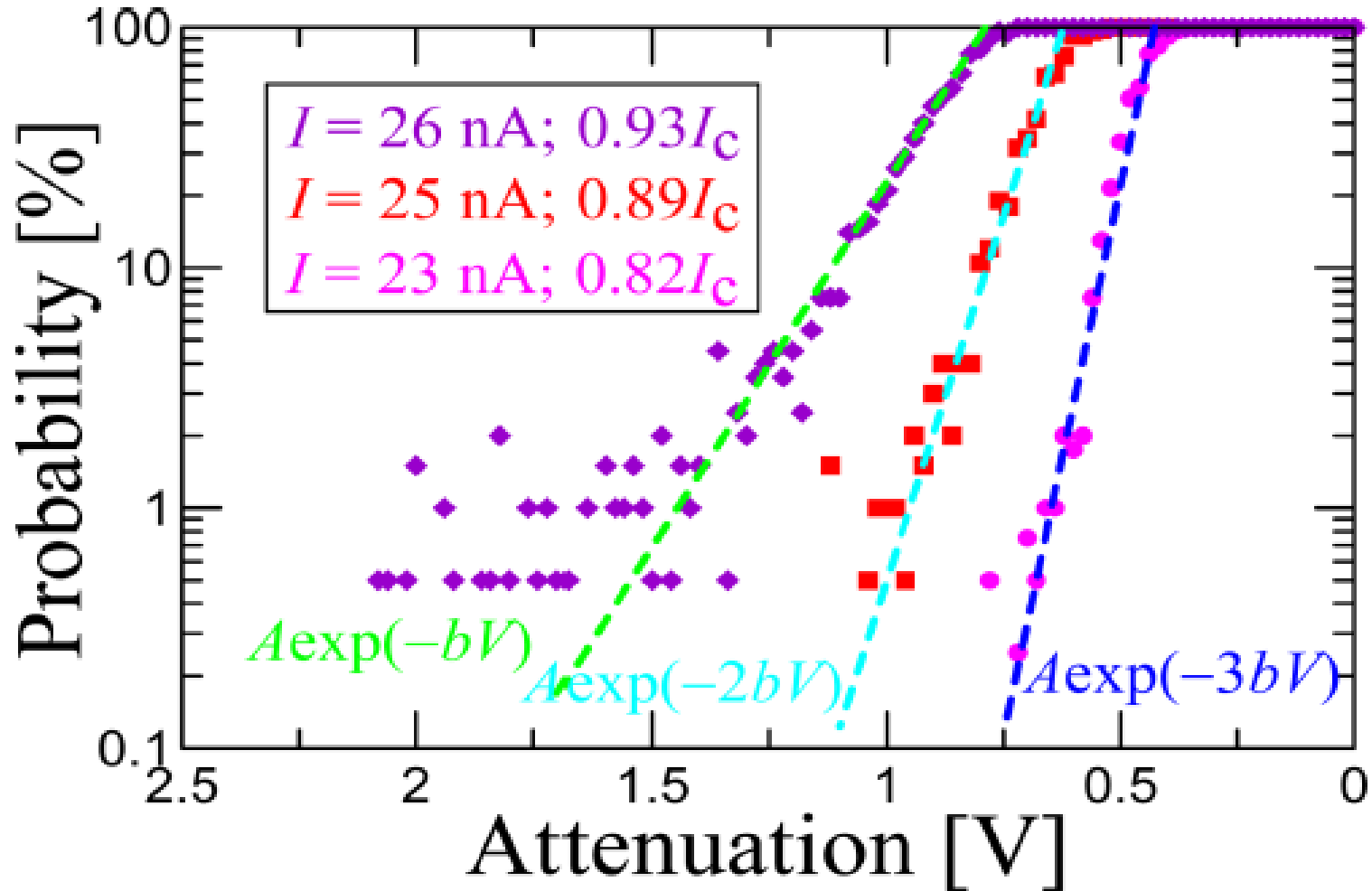
Signal power calibration by PAT steps



John R. Tucker and Marc J. Feldman, [Rev. Mod. Phys.](#) 57, 1055 (1985).

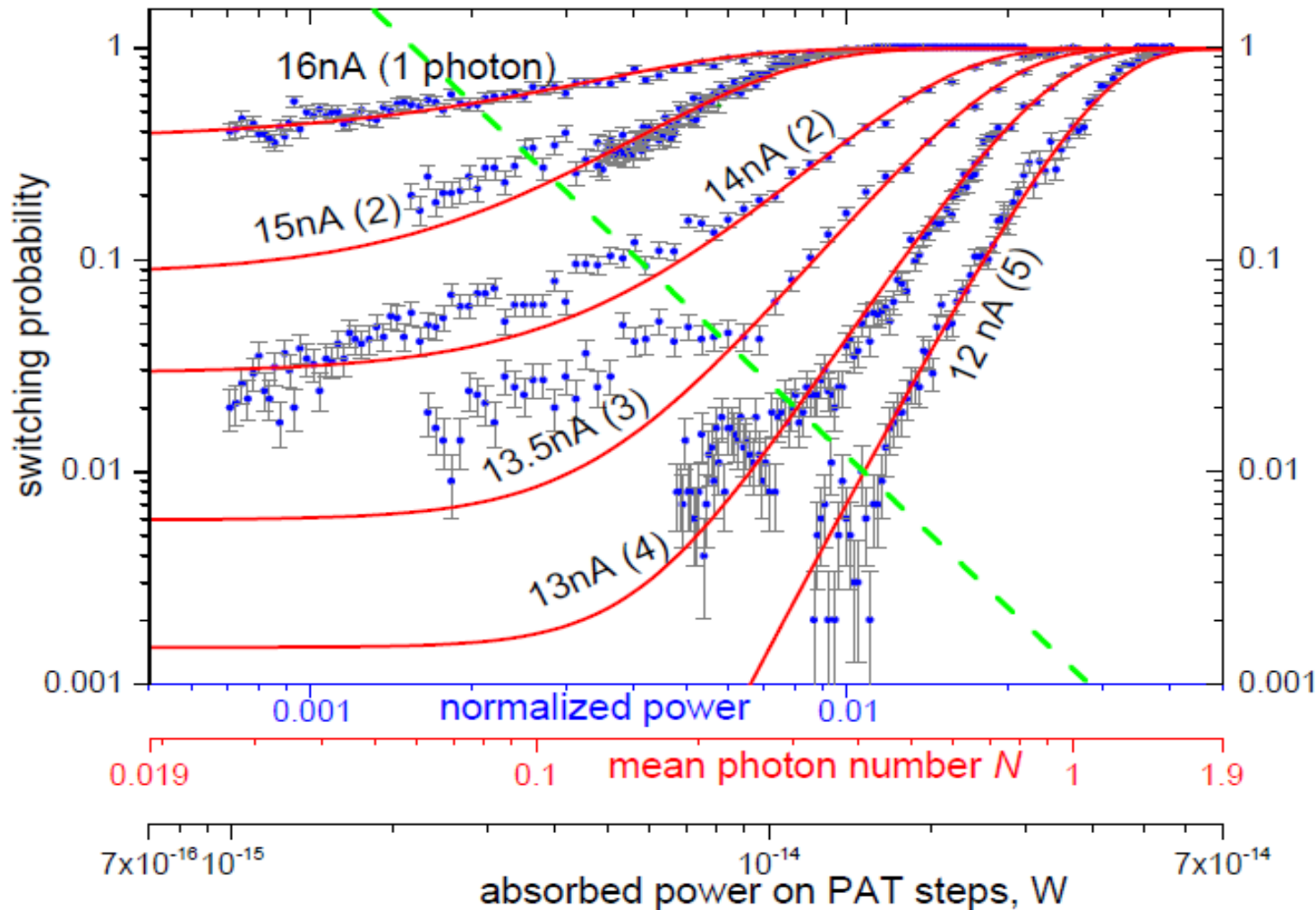
N-photon response for 9 GHz signal at 50 mK

Supply of a significantly attenuated harmonic signal, which decays into a stream of photons with a Poissonian distribution.



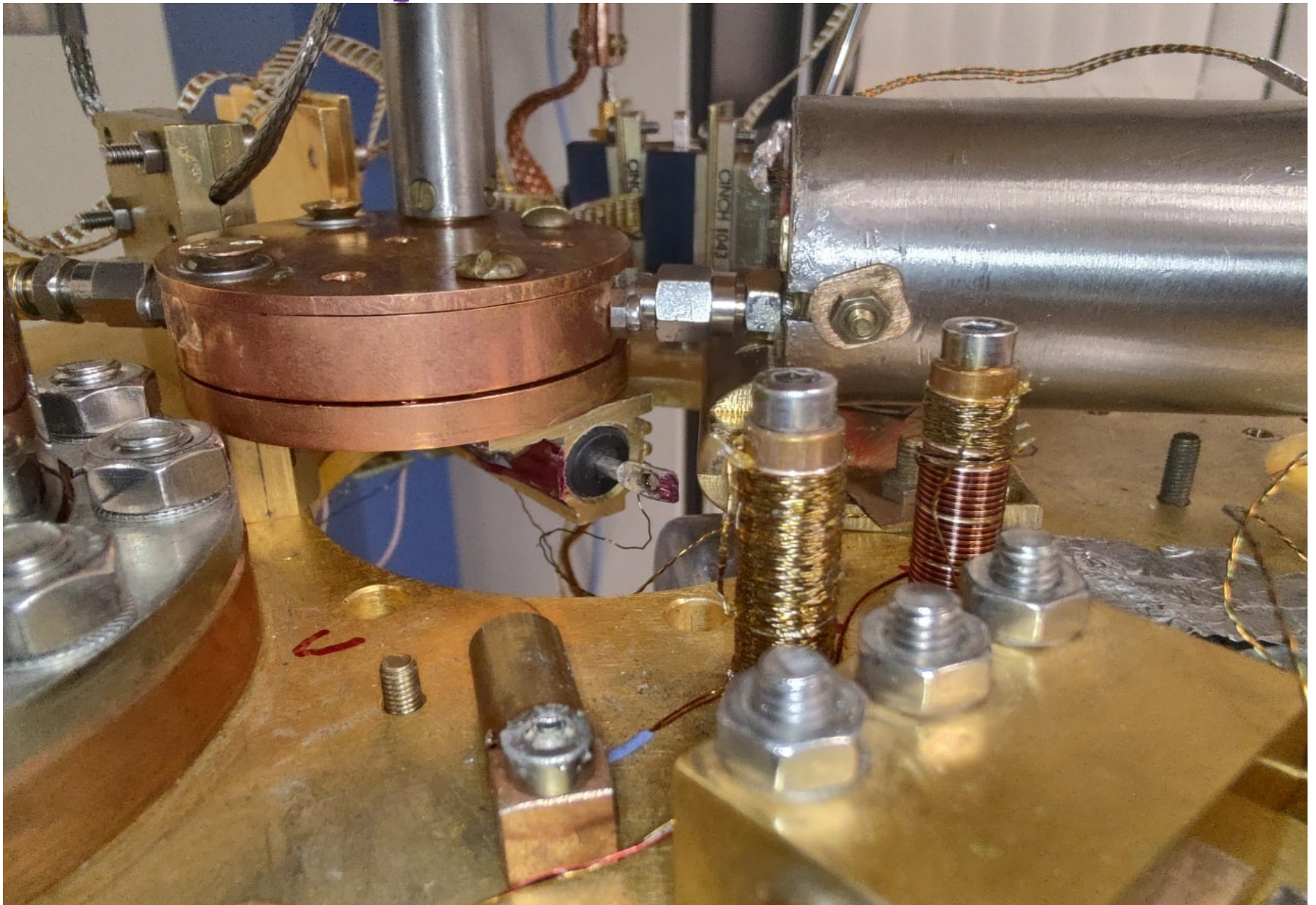
L.S. Revin, A.L. Pankratov, A.V. Gordeeva, A.A. Yablokov, I.V. Rakut, V.O. Zbrozhek, L.S. Kuzmin, [Beilstein J. Nanotechnol.](#) **11**, 960 (2020).

N -photon response for 10 GHz signal at 50 mK

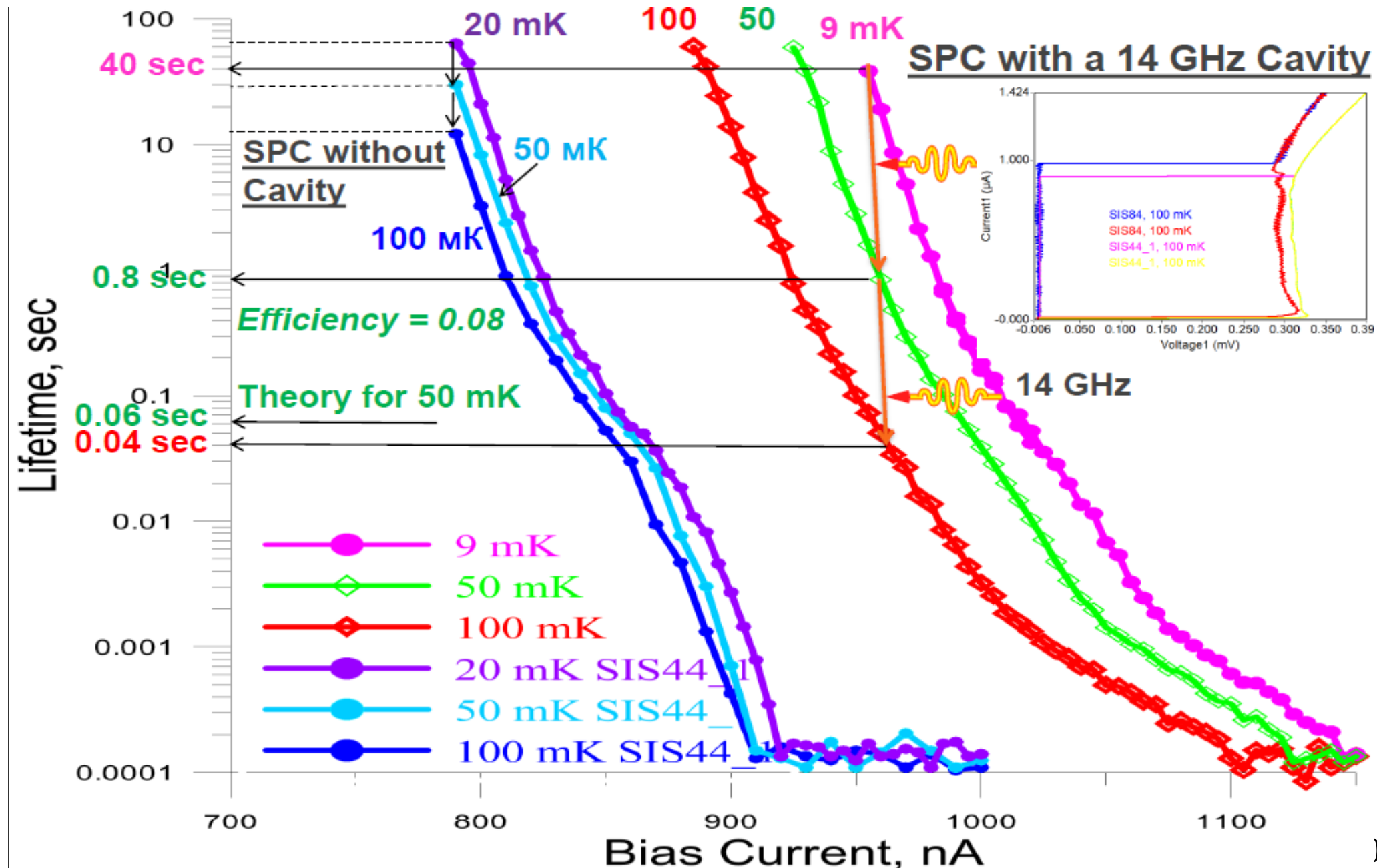


A. L. Pankratov, L. S. Revin, A. V. Gordeeva, A. A. Yablokov, L. S. Kuzmin & E. Il'ichev
Towards a microwave single-photon counter for searching axions, [npj Quantum Information](https://www.nature.com/articles/s41534-022-00569-5),
8, 61 (2022) <https://www.nature.com/articles/s41534-022-00569-5>

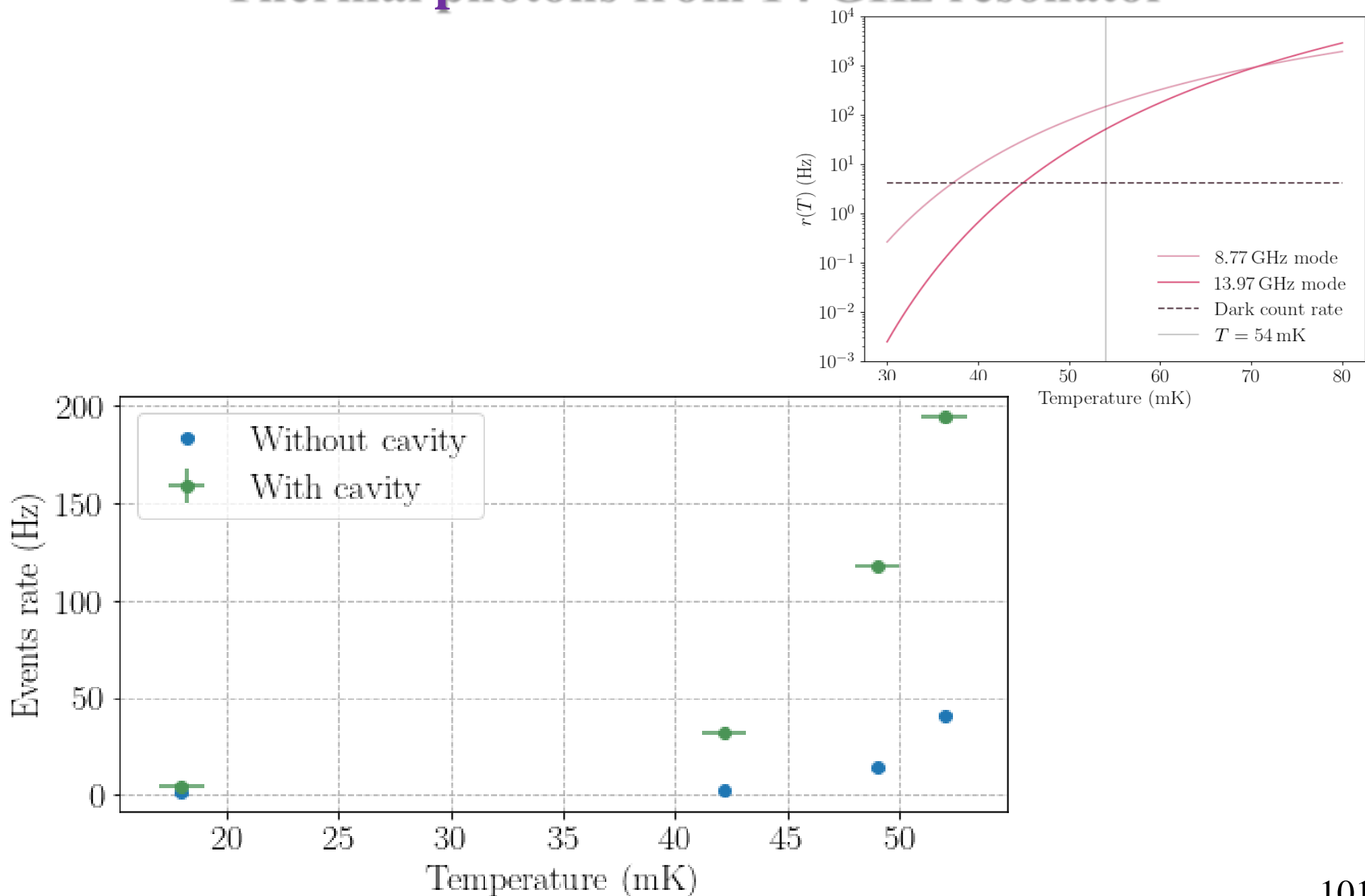
Thermal photons from 14 GHz resonator



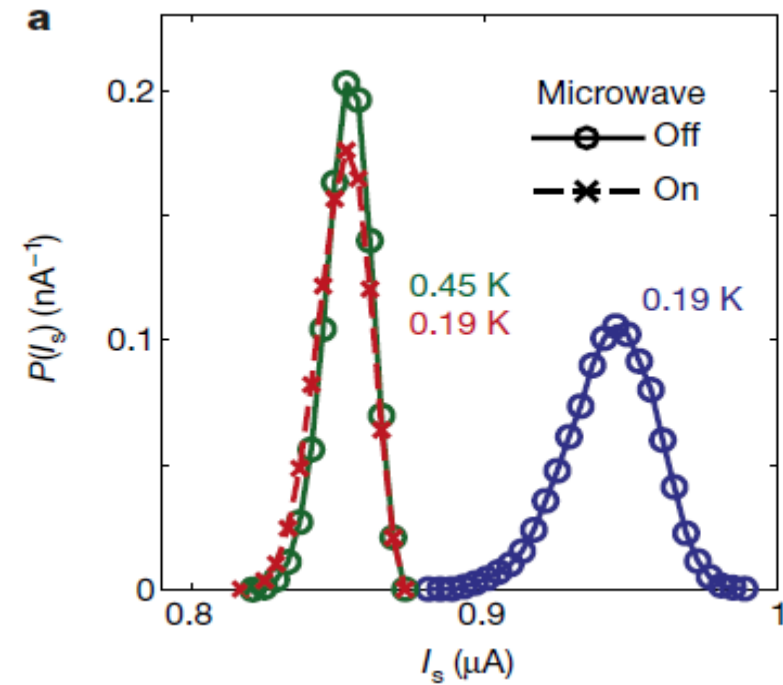
Thermal photons from 14 GHz resonator



Thermal photons from 14 GHz resonator

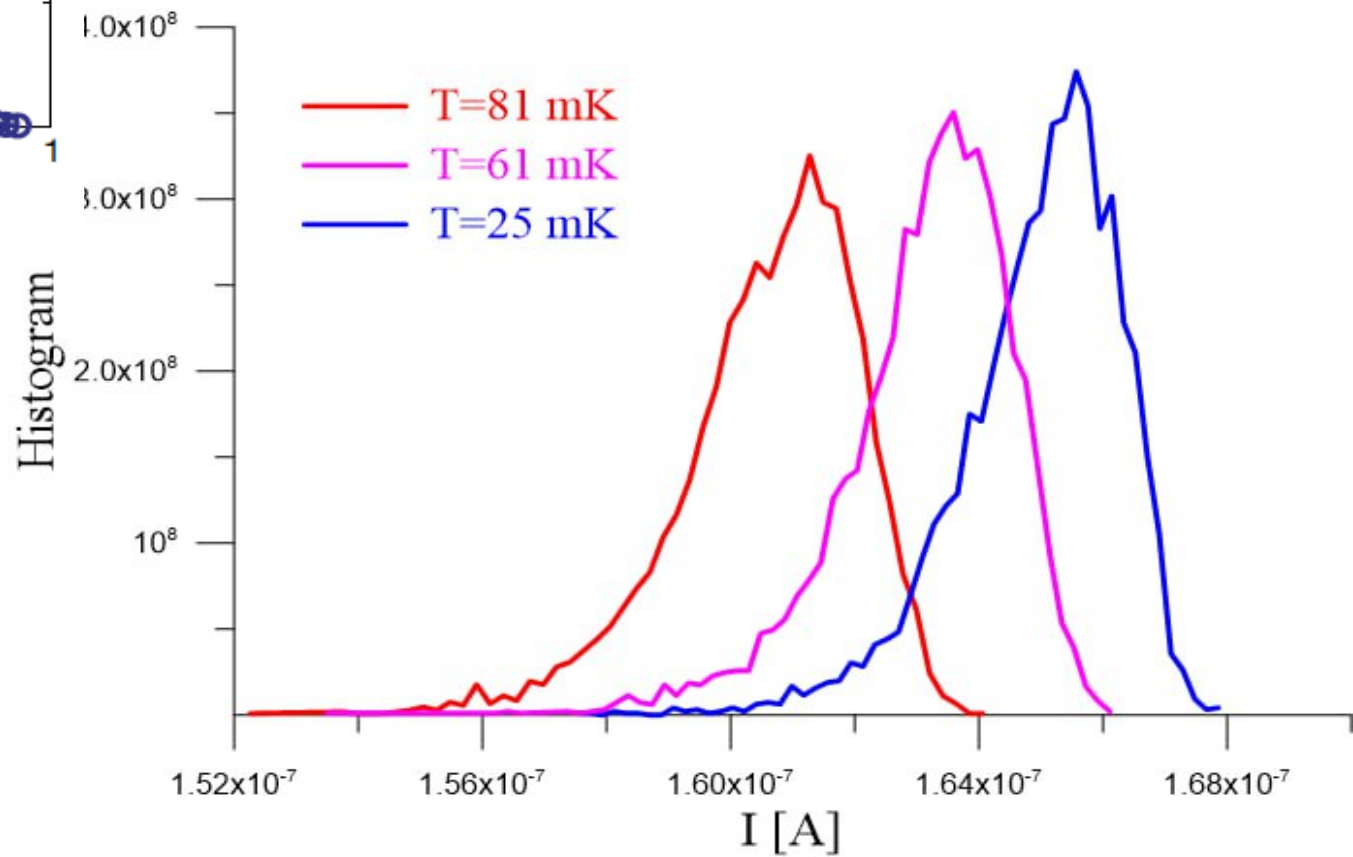


Thermal photons from 14 GHz resonator

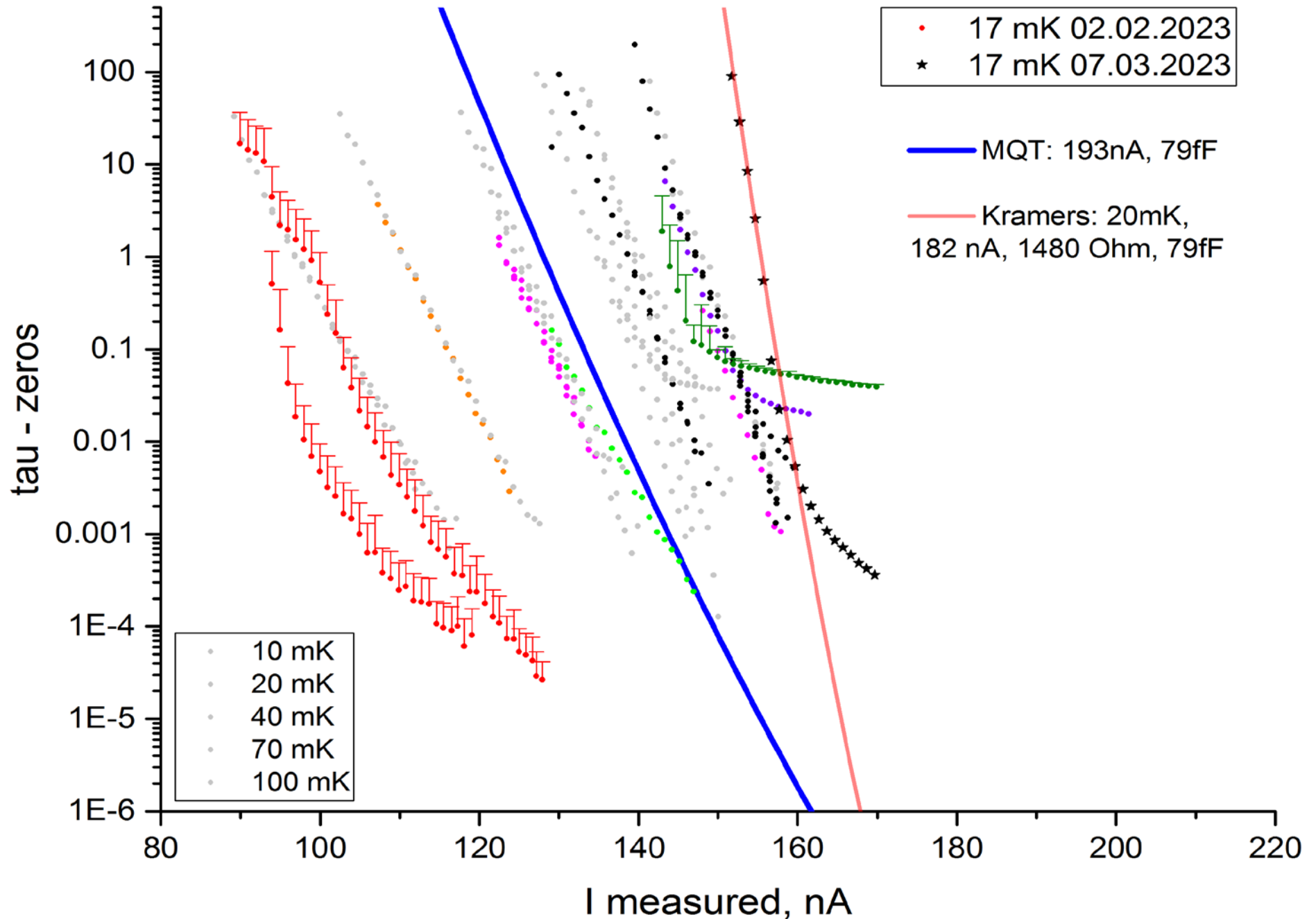


Lee, G.-H. et al. Graphene-based Josephson junction microwave bolometer.

Nature **586**, 42–46 (2020).



Improvement of the lifetime – exceeding theoretical limit



**Thank you
for attention!**